



## DESIGN AND SIMULATION OF PARALLEL MICROHEATER

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### ABSTRACT

This paper presents the design and simulation of a thin film microheater. This can have promising applications in bio-medical analysis, explosive detection, gas sensing, and micro-thrusters. An approach is presented to enhance the thermal uniformity of parallel microheater. The modeling of microheater is done using glass as a substrate material. The analysis is carried out with different resistive material for the heater. To study the response of the microheater to the different supply voltage, substrate thickness, and time interval, finite element simulation is carried out with commercial FEM analysis tool- COMSOL Multiphysics 5.2a. The proposed design in Model 1 have high contact resistance and it suffers from the contact-heating problem; however, Model 2 offers an excellent thermal uniformity with a tolerance of 1°C. There is a good agreement between the simulated and the theoretical results.

**Keywords:** Joule-heating, Microheater, Resistive-heating, Sensor, Temperature.

### 1. INTRODUCTION

Most of the bio-medical analysis and sensing applications require an elevated temperature. Therefore, systems like microfluidic Polymerase Chain Reaction (PCR) chip, gas sensors, and micro-chemical sensors need an integrated heating component with the device. Microheaters are one of the most important functional blocks for the systems such as microfluidic PCR chip for bio-medical analysis (Park *et al.*, 2011; Nie, *et al.*, 2014) humidity sensors for industrial application (Smetana and Unger, 2008; Dai, 2007), and Methanol sensors for chemical sensing (Ha *et al.*, 2005; Korotcenkov, 2014).

There are two types of microheater: the wire and the thin film based. The thin film microheaters are preferred over the wire microheaters due to their low thermal mass, less power consumption and ease of integration with other functional units of the system. At the early stage, heavily p-doped silicon microheaters were used because of its compatibility with integrated circuit fabrication process and its attractive mechanical properties. However, huge power consumption is the major drawback of the silicon microheaters. To overcome the problem of large power requirement, the proposed heaters are modeled on the Glass substrate, which offers low thermal conductivity ( $1.38 \text{ Wm}^{-1}\text{C}^{-1}$ ) and high electrical resistivity ( $1 \times 10^{14} \Omega\text{m}$ ); desirable to achieve better thermal uniformity and low power consumption.

The commonly used resistive materials for the microheater are Aluminum (Phanakun *et al.*, 2012), Copper (Pandya *et al.*, 2012), Gold (Kim, 2006), Nickel-Chromium (NiCr) alloy (Das and Akhtar, 2014), Platinum (Hsieh *et al.*, 2008), Titanium (Guan and Puers, 2010), and Tungsten (Santra *et al.*, 2010). Aluminum and Copper are susceptible to corrosion and oxidation; therefore, they are avoided as the resistive material for the microheater. Gold and Platinum are chemically inert materials but they are very expensive; therefore, to keep the device cost low, they are not used. The melting temperature of Titanium and Tungsten are higher compared to NiCr. Therefore, it is easier to

evaporate the NiCr compared to Titanium and Tungsten. Hence, this work uses NiCr as a resistive element for the microheater. Figure 1 shows the schematic of microheaters.

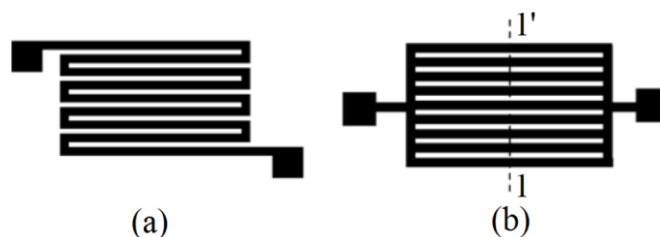


Fig. 1 Schematic of (a) series, and (b) parallel microheater

### 2. DESIGN AND GOVERNING EQUATIONS

Joule heating is the phenomena in which the current is passed through a resistive material to generate the heat. The heating power  $P$  of a microheater is produced by connecting a voltage source  $V$  across the two ends of a heating circuit with a resistance  $R$  due to the current  $I$ . The basic configurations of the heating circuit are categorized as series and parallel type, respectively. Figures 1(a) and 1(b), shows the series and parallel resistance microheater, respectively. In Fig. 1(a), the contact pad and the resistive elements are connected in series. Therefore, power dissipation of the heater is given by,

$$P = I^2 R \quad (1)$$

From Eq. (1) the power is directly proportional to the resistance of the heating element. Therefore, the higher resistance values are favorable in achieving the large heating power.

In Fig. 1(b) there is no voltage difference in the resistive element across the line 1-1' therefore the power across 1-1' line is given by,

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$$P = \frac{V^2}{R} \quad (2)$$

Hence, the smaller resistances are favorable in achieving higher heating power and results in the faster response for the parallel configuration.

Resistance plays a critical role in power dissipation calculation. The resistance of any thin-film having the length, width and thickness  $L$ ,  $w$ , and  $t$ , respectively is given by,

$$R = \frac{\rho L}{wt} \quad (3)$$

The  $\rho$  represents the resistivity of the material. If  $L=w$ , then Eq. (3) represent the sheet resistance ( $R_s$ ) of the resistive layer and can be written as,

$$R_s = \frac{\rho}{t} \quad (4)$$

Therefore, the resistance of any resistive thin film can be calculated as,

$$R = R_s \frac{L}{w} \quad (5)$$

The heat produced in a resistive element due to Joule heating is given by,

$$\Delta Q = I^2 R \Delta t \quad (6)$$

Here,  $\Delta t$  is the time. The heat generated by the microheater is dissipated in the surrounding medium. The thermal loss of microheater is divided into three types, viz., conduction in the device, convection cooling, and radiation. Therefore, to achieve steady state, the total heat produced by the microheater must be equal to the heat lost by conduction ( $Q_{cond}$ ), convection ( $Q_{conv}$ ), and radiation ( $Q_{rad}$ ).

$$I^2 R \Delta t = Q_{cond} + Q_{conv} + Q_{rad} \quad (7)$$

$$I^2 R = \frac{Q_{cond}}{\Delta t} + \frac{Q_{conv}}{\Delta t} + \frac{Q_{rad}}{\Delta t} \quad (8)$$

The rate of heat loss by conduction in the glass substrate is given by,

$$\frac{Q_{cond}}{\Delta t} = k_{glass} A_{glass} \frac{\Delta T}{\Delta x} \quad (9)$$

Here  $k_{glass}$ ,  $A_{glass}$ ,  $\Delta T$ , and  $\Delta x$ , represents the thermal conductivity, area of the cross-section of the glass substrate, a temperature difference of two opposite surfaces and the thickness of glass substrate, respectively. The rate of heat loss by conduction can be reduced by selecting the substrate material with a lower thermal conductivity and by decreasing the area of conduction.

The rate of heat loss by convection in the air is given by,

$$\frac{Q_{conv}}{\Delta t} = h A_{conv} \Delta T \quad (10)$$

Here,  $h$  is coefficient of convection, it depends on the geometrical factor, shape, and the orientation of the heated surface.  $A_{conv}$  and  $\Delta T$  represent the surface area through which convection is taking place and the temperature difference between the heater and the ambient, respectively.

The rate of heat lost by radiation is given by,

$$\frac{Q_{rad}}{\Delta t} = \epsilon \sigma A_{rad} \Delta T^4 \quad (11)$$

The  $\epsilon$ ,  $\sigma$ ,  $A_{rad}$ , and  $\Delta T$  are the emissivity, Stefan Boltzmann constant, surface area and the temperature difference between the heater and the ambient, respectively.

Therefore, the total power lost can be obtained by,

$$I^2 R = k_{glass} A_{glass} \frac{\Delta T}{\Delta x} + h A_{conv} \Delta T + \epsilon \sigma A_{rad} \Delta T^4 \quad (12)$$

The losses due to radiation can be neglected at the temperature range of interest of microheater and due to the very low emissivity of the materials involved (Courbat *et al.*, 2011). Therefore Eq. (12) can be rewritten as

$$I^2 R = k_{glass} A_{glass} \frac{\Delta T}{\Delta x} + h A_{conv} \Delta T \quad (13)$$

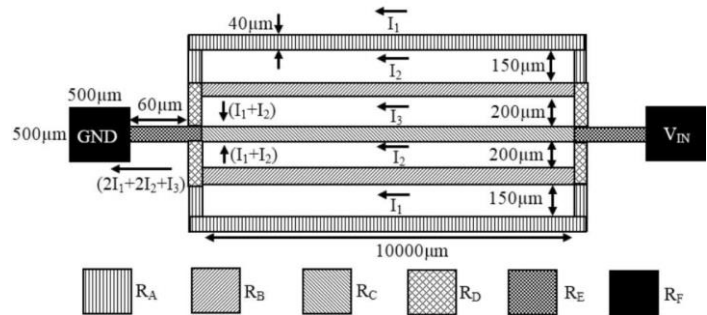


Fig. 2 Parallel microheater (Model 1)

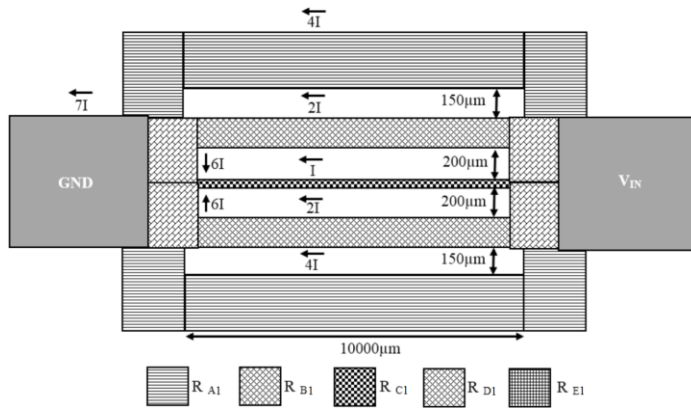
Figure 2 shows the parallel microheater Model 1, the width of all the resistive elements  $R_A$  to  $R_E$  is taken  $40\mu\text{m}$ . For the resistance calculation, the resistivity and thickness of all the resistive films are taken as  $1.10 \times 10^{-6} \Omega\text{m}$  and  $0.2\mu\text{m}$ , respectively. The dimension and theoretical resistance values of all the resistive element used in Model 1 are given in Table 1.

Table 1 Resistance of individual resistive elements of microheater Model 1.

Parameter	$L(\mu\text{m})$	$w(\mu\text{m})$	$L/w$	Resistance ( $\Omega$ )
$R_A$	10380	40	259.5	1427.25
$R_B$	10000	40	250.0	1375.00
$R_C$	10000	40	250.0	1375.00
$R_D$	240	40	6	33.00
$R_E$	100	40	2.5	13.75
$R_F$	500	500	259.5	5.50

It can be seen from Table 1 that  $R_A$  is having the highest resistance compared to all other resistive element. When a voltage source connected to the microheater circuit, it results in current flow through the resistive elements. As the current always takes the low resistance path, the minimum and the maximum current flowing through  $R_A$  and  $R_E$ , respectively, which leads to the minimum and maximum temperature near to circumferences of the heater and the resistive element  $R_E$ , respectively. It can be seen from the Fig. 2 that resistive elements  $R_B$  and  $R_C$  are having two neighbor resistive elements whereas  $R_A$  has the only neighbor. Due to more neighbor and conductive heat transfer in the glass substrate, the central region of heater acquires higher temperature. To overcome this problem, the separation between the resistive elements reduces as we move away in the top or bottom direction from the center of the heater. From Fig. 2, the separation

between  $R_C$  and  $R_B$  is  $200\mu\text{m}$  whereas the separation of  $R_B$  and  $R_A$  is  $150\mu\text{m}$ .



**Fig. 3** Modified parallel microheater (Model 2)

To overcome the problem of nonuniform heating of Model 1, a modified parallel microheater is proposed in Model 2 shown in Fig. 3. In the Model 2, the resistance of the resistive elements is selected in such that if a voltage source connected to the heater the minimum current ( $I$ ) flows through the resistance  $R_{C1}$ , and as we move away from the center in the top or bottom direction current gets doubled of its neighboring branch.

The heating power in resistive element  $R_{C1}$  can be calculated as,

$$P_{R_{C1}} = \frac{\rho L}{w_1 t} I^2 \quad (14)$$

Here  $L$  and  $w_1$  represent the length and width of resistance  $R_{C1}$ . Similarly, the power in resistive element  $R_{B1}$  due to current  $2I$  can be calculated as,

$$P_{R_{B1}} = \frac{\rho L}{w_2 t} 4I^2 \quad (15)$$

Here  $w_2$  represent the width of resistive element  $R_{B1}$ . By equating Eqs. (14) and (15), and solving for  $w_2$

$$w_2 = 4w_1 \quad (16)$$

Similarly, the width of all the resistive elements is calculated by taking a constant length  $10000\mu\text{m}$  and shown in Table 2.

**Table 2** Resistance of individual resistive elements of microheater Model 2 with a fixed length.

Parameter	$L(\mu\text{m})$	$w(\mu\text{m})$	$L/w$	Resistance ( $\Omega$ )
$R_{A1}$	10000	640	15.62	85.91
$R_{B1}$	10000	140	62.50	343.75
$R_{C1}$	10000	40	250.00	1375.00
$R_{D1}$	10000	1440	6.95	38.22
$R_{E1}$	10000	1960	5.10	38.30

Once the  $L:w$  ratio of all the resistances are known, then as per spacing between the resistive elements of Model 2 shown in Fig. 3, the dimensions of all the resistive members are calculated using Eq. (5), and given in Table 3.

As per the calculation, the length and width of  $R_{E1}$  are  $5355\mu\text{m}$  and  $1050\mu\text{m}$ , respectively. But to accommodate the heater on a  $30 \times 10\text{mm}^2$  glass substrate, the length of  $R_{E1}$  is fixed to  $1554\mu\text{m}$ . The major drawback of the design proposed in Model 2 is if the number of parallel branches increases the width of the resistive elements increases

exponentially. Hence for more than 5 parallel branches, the proposed design is not practical.

**Table 3** Resistance of individual resistive elements of microheater Model 2.

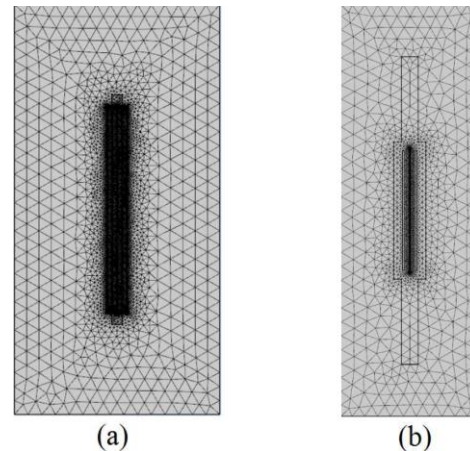
Parameter	$L(\mu\text{m})$	$w(\mu\text{m})$	$L/w$	Resistance ( $\Omega$ )
$R_{A1}$	11580	741.12	15.62	85.91
$R_{B1}$	9102	145.90	62.50	343.75
$R_{C1}$	9120	36.50	250.00	1375.00
$R_{D1}$	380	54.67	6.95	38.22
$R_{E1}$	5355	1050	5.10	38.30

### 3. SIMULATION

The simulations are carried out using a commercial FEM simulation tool COMSOL Multiphysics 5.2a. The specifications of the Model 1 and Model 2 are shown in Table 4.

**Table 4** Microheater specification.

Specification	Model 1	Model 2
Substrate ( $L \times w$ ( $\text{mm}^2$ ))	$20 \times 10$	$30 \times 10$
Substrate thickness(mm)	1.5	1.5
Substrate material	Glass	Glass
Contact pad ( $\text{mm}^2$ )	$0.5 \times 0.5$	$1.554 \times 1.050$
Minimum line width ( $\mu\text{m}$ )	40	36.5
Maximum line width ( $\mu\text{m}$ )	40	1050
Resistive material	NiCr	NiCr
Resistive layer thickness ( $\mu\text{m}$ )	0.2	0.2



**Fig. 4** Mesh model of microheater (a) Model 1, and (b) Model 2

All the material properties for the simulation are taken from the COMSOL material library. For all the simulations, the ambient temperature, and the convection coefficient  $h$  are considered  $20^\circ\text{C}$  and  $5 \text{ Wm}^{-2}\cdot^\circ\text{C}^{-1}$ , respectively. The design of microheater targets the biomedical application where the maximum operating temperature is below  $100^\circ\text{C}$ , therefore the input voltage for all the heaters are fixed in such that the steady state temperature will be  $90^\circ\text{C}$  -  $100^\circ\text{C}$ . To study the effect of substrate thickness on the heater behavior, the parametric sweep is used to vary the substrate thickness from  $300\mu\text{m}$  to  $1500\mu\text{m}$  in steps of  $300\mu\text{m}$ . A time-dependent simulation is carried out from 0s to 1600s in steps of 50s, to find out the transient response of the microheater. A predefined extra fine size free tetrahedral type mesh is used to simulate the microheater models. The meshes are very fine near the heater element and get coarser as we move away from the heater where high accuracy is not needed Figs. 4(a) and 4(b) show the meshes of Model 1 and Model 2, respectively.

#### 4. RESULT AND DISCUSSION

The simulation of Model 1 and Model 2 are carried out using Aluminium, Copper, Gold, Nickel-Chromium, Platinum, Titanium and Tungsten. For all the simulation Glass (1.5mm thick) is taken as substrate. To find the resistance of microheaters modeled with the different resistive material,  $IA$  current is applied as the input to each model and the voltage across each heater is measured. From Ohm's law, we know that  $V=IR$ , therefore, the voltage is equal to the resistance of the heater. Once the resistance is known, by applying the fixed voltage across the heater, the power is calculated for Model 1 and Model 2 and given in Tables 5 and 6, respectively.

**Table 5** Simulation outcome of Model 1.

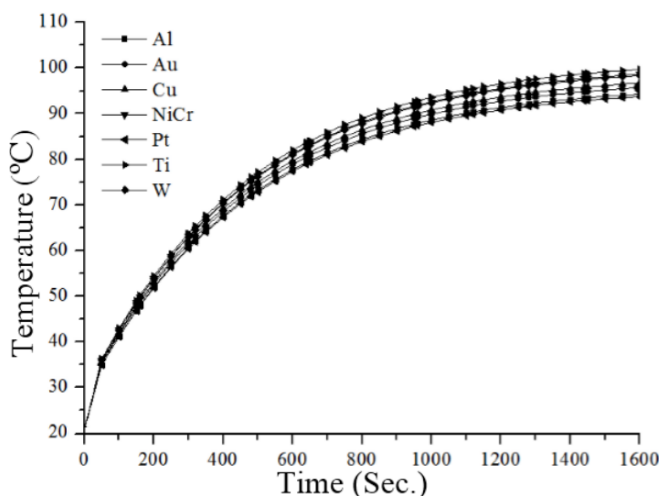
Material	Resistance( $\Omega$ )	Voltage(V)	Power(W)	Time(s)
Al	8.57	0.73	0.0621	1476
Au	6.67	0.58	0.0504	1410
Cu	5.24	0.68	0.0642	1455
NiCr	335.00	4.70	0.0659	1452
Pt	34.20	1.45	0.0614	1472
Ti	117.00	2.80	0.0670	1440
W	15.20	1.00	0.0657	1466

**Table 6** Simulation outcome of Model 2.

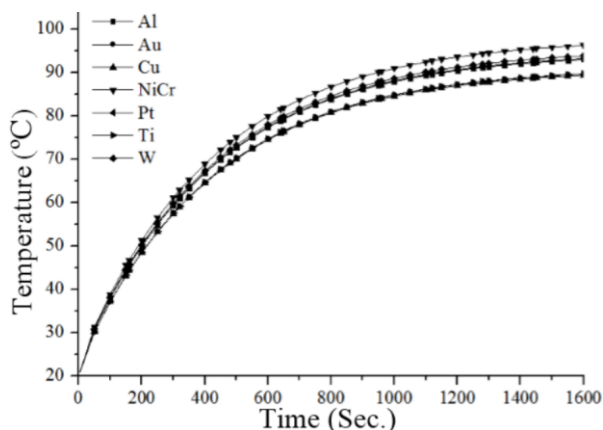
Material	Resistance( $\Omega$ )	Voltage(V)	Power(W)	Time(s)
Al	2.31	0.50	0.1082	1061
Au	1.80	0.43	0.1027	1085
Cu	1.41	0.38	0.1024	1092
NiCr	90.3	3.20	0.1134	1079
Pt	9.23	1.00	0.1083	1093
Ti	31.6	1.80	0.1025	1090
W	4.11	0.67	0.1092	1075

Once the power is known the time required to reach to the steady state temperature is calculated theoretically for microheater Model 1 and Model 2, and given in Table 5 and Table 6, respectively.

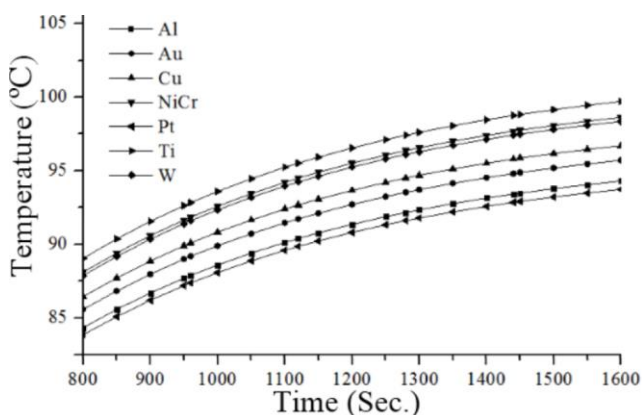
Figures 5 and 6 shows the time versus temperature plot for microheater Model 1 and Model 2, respectively. It is observed from the Tables 5, 6 and Figs. 5 and 6 that there is a good agreement between the theoretically calculated time required to reach to the given steady state temperature and the result obtained from the FEM simulation. Figures 7 and 8 shows the zoomed view of time versus temperature plot shown in Figs. 5 and 6, respectively. It is observed that to reach the steady state temperature microheater Model 1 takes longer time compared to Model 2 (Cengel and Ghajar, 2011).



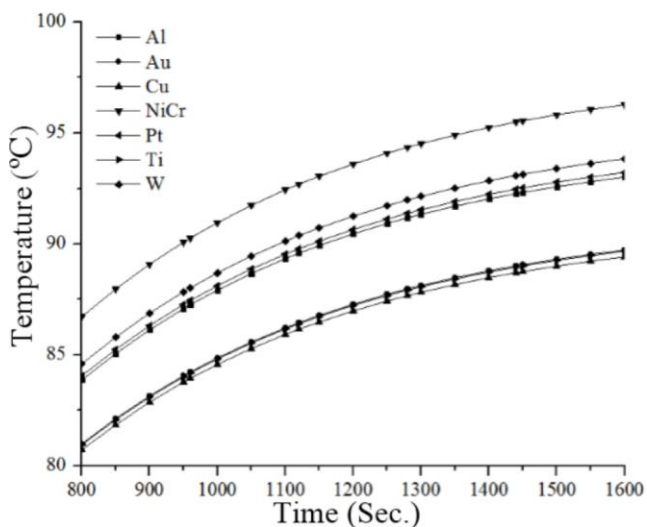
**Fig. 5** Time vs. temperature plot of Model 1



**Fig. 6** Time vs. temperature plot of Model 2



**Fig. 7** Zoomed view of time vs. temperature plot of Model 1

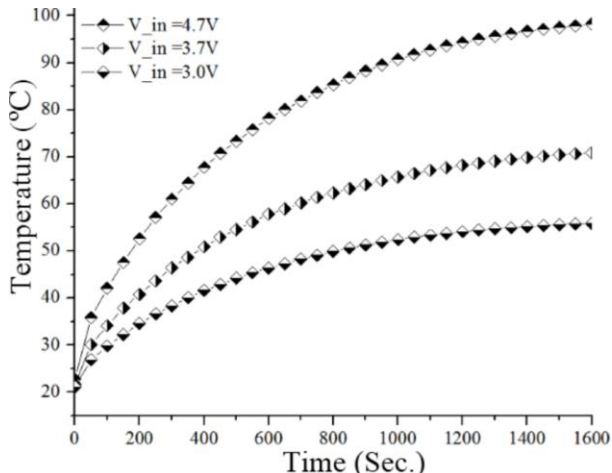


**Fig. 8** Zoomed view of time vs. temperature plot of Model 2

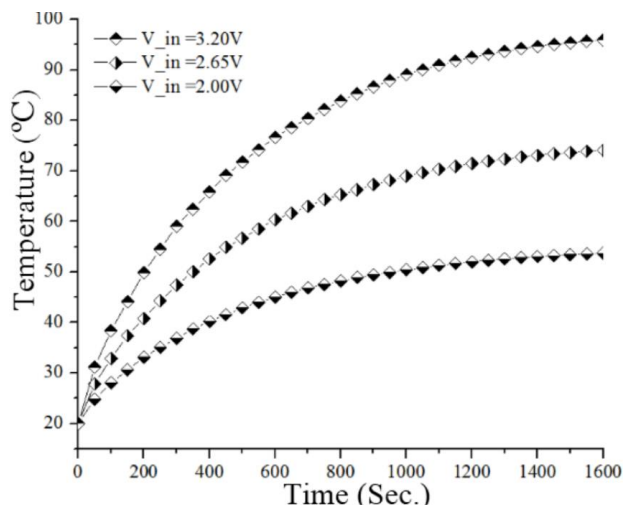
Focusing on PCR application, simulation have been carried out to find the time required to reach to the temperatures 90-95°C (denaturation), 50-55°C (annealing), and 70-75°C (extension) steady state temperature for the NiCr microheater Model 1 (Fig. 9) and Model 2 (Fig. 10), It is observed from the Figs. 9 and 10 that time required for lower steady state temperature is less compared to the elevated temperature and rate of change of temperature is more for the higher steady state temperature.

From Figs. 5 to 10, it is observed that the time required for both the microheater models to reach to its steady state temperature is greater than 1000s. Therefore, to achieve the steady state temperature quickly, initially 12V supply voltage applied to the heater (Model 1) and after the 50s the voltage is decreased to 4V. Similarly, for the heater (Model

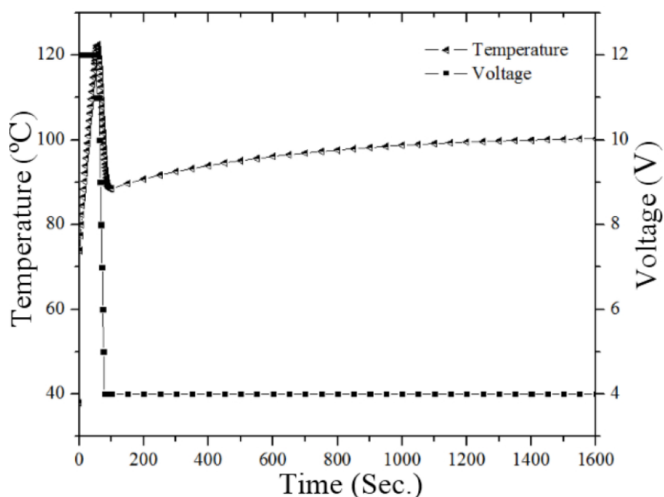
2) initially 9V input is applied and after the 50s it is reduced to 3V, the time versus temperature plot of Model 1 and Model 2 are shown in Figs. 11 and 12, respectively. From Figs. 11 and 12, it is observed that both the heaters achieve the 90 percent of steady state temperature in less than 200s. The problem involves in this approach is the kink in the temperature during the voltage transition. It is observed that Model 2 (Fig. 12) has smaller temperature kink compared to Model 1 (Fig. 11), it is due to larger size of contact-pad.



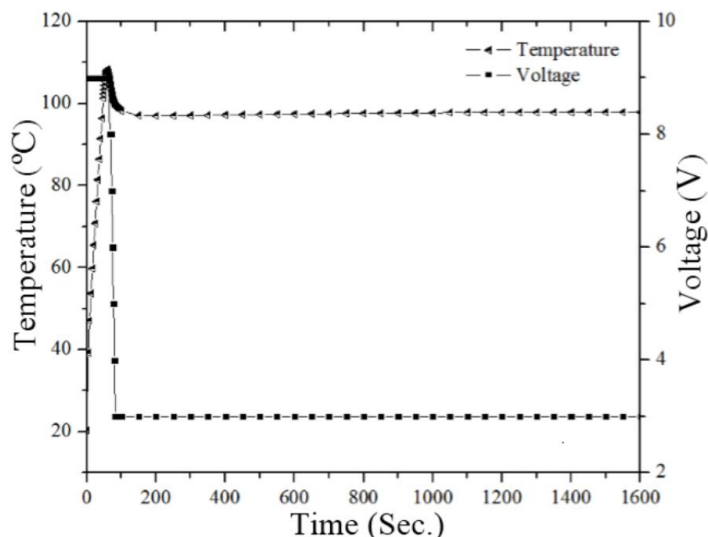
**Fig. 9** Time vs. temperature plot of NiCr microheater Model 1



**Fig. 10** Time vs. temperature plot of NiCr microheater Model 2

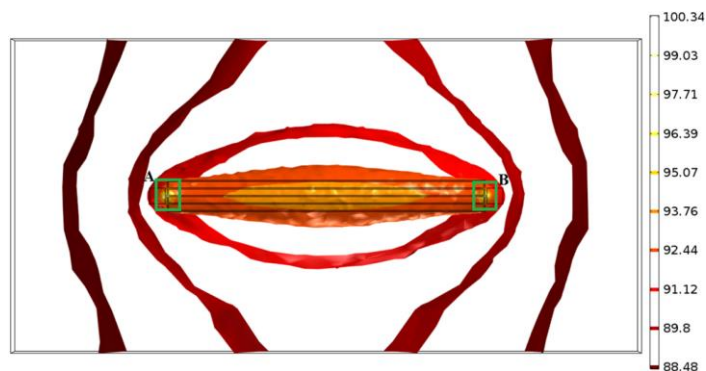


**Fig. 11** Time vs. temperature plot of NiCr microheater Model 1 for step input voltage

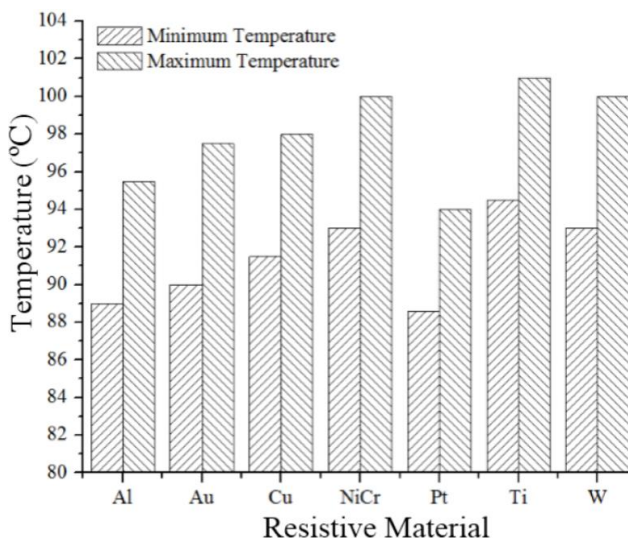


**Fig. 12** Time vs. temperature plot of NiCr microheater Model 2 for step input voltage

Figure 13 shows the isothermal contour plot of NiCr microheater Model 1, the two-green rectangle marked as A and B (resistor  $R_E$ , Fig. 2), are the hottest point of the heater and circumferences are at a minimum at minimum temperature. The Bar graph is shown in Fig. 14 shows the temperature of hottest and coolest region of microheater Model 1. It is observed the average temperature difference is around 6.5°C for the different resistive material based heater.



**Fig. 13** Isothermal contour of microheater Model 1



**Fig. 14** Maximum and minimum temperature vs resistive material for microheater Model 1

Figure 15 shows the isothermal contour of NiCr microheater Model 2. The bar graph is shown in Fig. 16 shows the temperature of hottest and coolest region of microheater Model 2. It is observed the average temperature difference is around 1°C for the different resistive material based heater. Hence modified parallel heater proposed in Model 2 offers excellent thermal uniformity with the tolerance of 1°C.

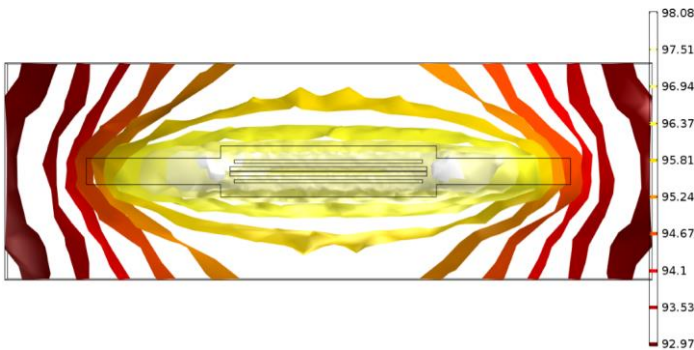


Fig. 15 Isothermal contour of microheater Model 2

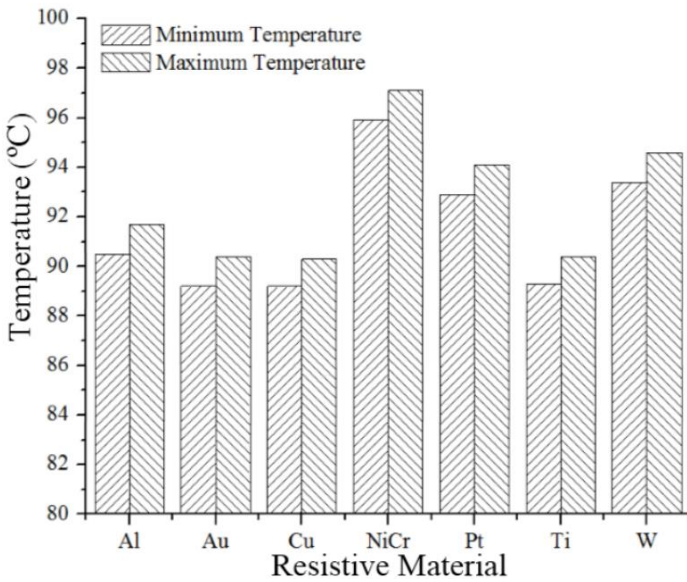


Fig. 16 Maximum and minimum temperature vs resistive material for microheater Model 2

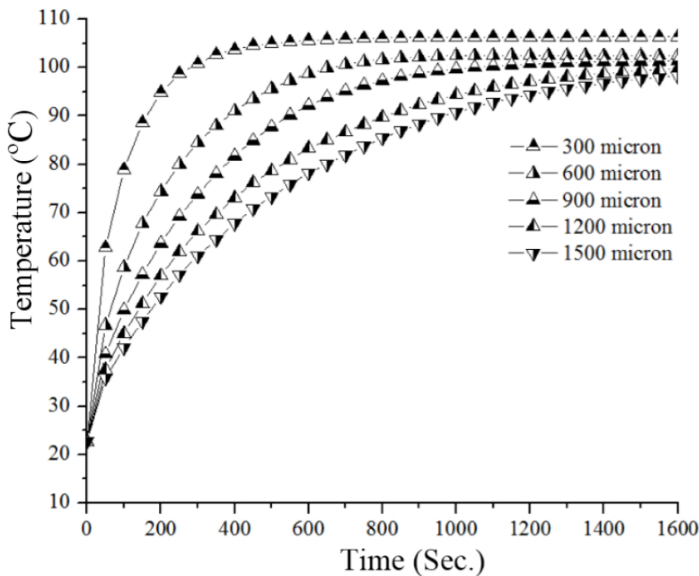


Fig. 17 Time versus temperature plot of Model 1 for different substrate thickness

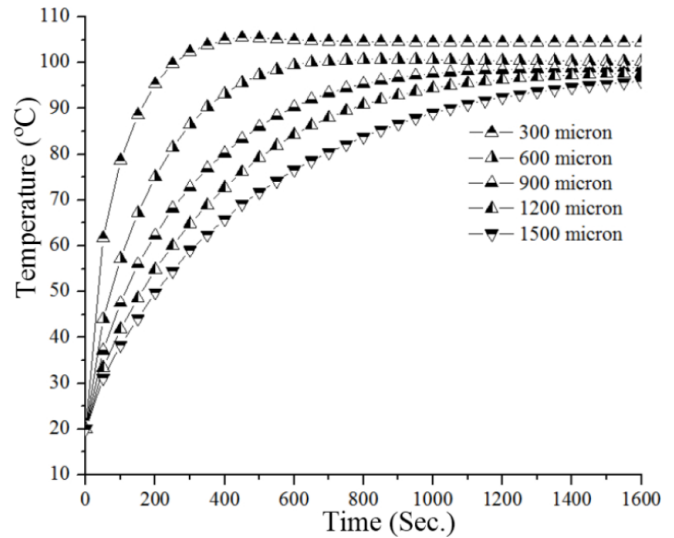


Fig. 18 Time versus temperature plot of Model 2 for different substrate thickness

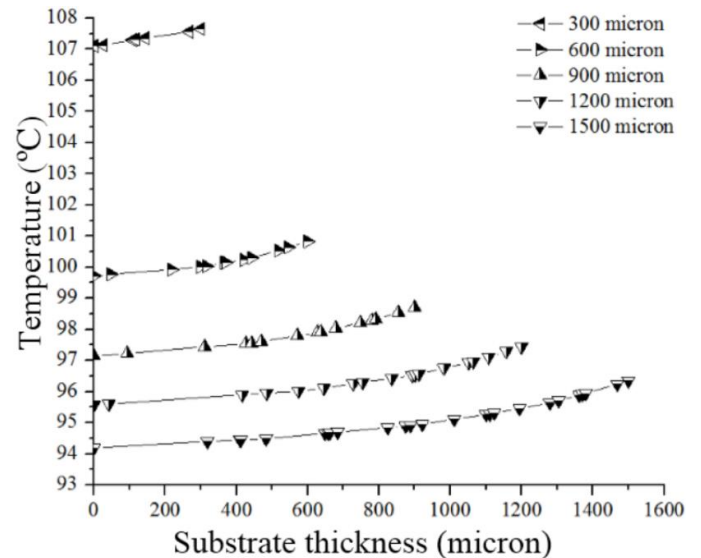


Fig. 19 Substrate thickness versus temperature plot for Model 1

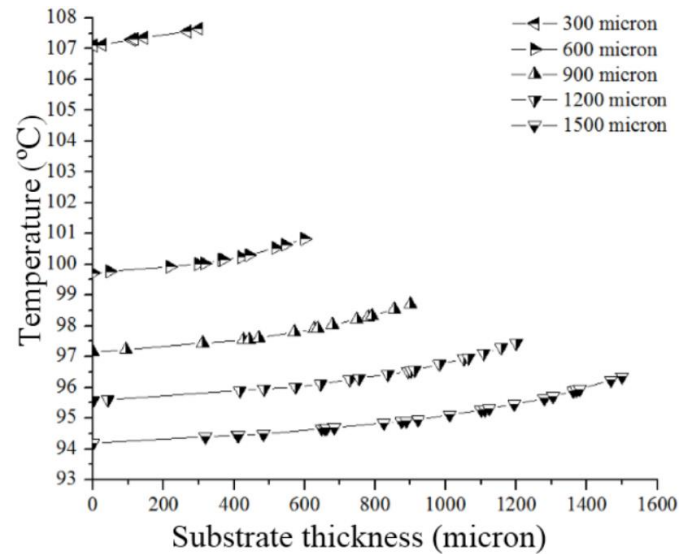


Fig. 20 Substrate thickness versus temperature plot for Model 2

For the applications such as PCR, the temperature control is very crucial, the heater and the microfluidic reservoir are fabricated at the opposite surface of the glass substrate. Therefore, it is necessary to carry out the transient analysis to find the time required for the heater to reach to the steady state temperature and the temperature difference of the two opposite faces of the glass substrate. Figures 17 and 18 show the time required to reach the steady state temperature for different substrate thicknesses for Model 1 and Model 2, respectively. It can be observed that as the substrate thickness increases the time required to reach the steady state temperature also increases. Therefore, thinner substrates are favorable for achieving steady state temperature quickly.

Figures 19 and 20 show the substrate thickness versus temperature plot for Model 1 and Model 2, respectively. In the Figs. 19 and 20,  $x=0$  represents the bottom surface of the glass substrate and the terminal value of the  $x$  represents surface where the heater is located. It is observed from the Figs. 19 and 20 that the thinner substrate gives the better temperature control.

Table 7 shows the comparison of the present work with the experimental work with respect to the substrate used, heating element, maximum operating temperature, and power. The proposed heater in Model 2 is the most power efficient.

**Table 7** Comparison of the present work with the experimental work

Work	Substrate	Heating material	T(°C)	Power(mW)
Present work	Glass	NiCr	98	65.9 (Model 1)
Present work	Glass	NiCr	98	113.0 (Model 2)
Hsieh <i>et al.</i> , 2008	Glass	Pt/Ti	94	240.0
Hwang <i>et al.</i> , 2011	Silicon	Poly-Si	460	250.0
Kundu <i>et al.</i> , 2014	Silicon	Boron diffused Si	127	1700.0

## 5. CONCLUSIONS

The design and the simulation of a microheater have been carried out with two microheater models. Higher values of the thermal and the electrical resistivity are the desirable ones for the substrate to achieve the better heat confinement. The Model 1 and the Model 2 are the parallel type of microheater. Simulations are carried out using varied materials and found that the NiCr microheaters are using comparatively high power but it is cost-effective compared to other material based microheaters. Model 1 suffers overheating of contact pads due to higher resistance and current near the contact pads. To solve this problem microheater Model 2 is proposed. This offers an excellent thermal uniformity with more than 72 percent area of the heater falling within the tolerance of 1°C and most suitable for applications such as stationary PCR.

## ACKNOWLEDGEMENTS

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## NOMENCLATURE

$A_{conv}$	surface area of convection (m <sup>2</sup> )
$A_{glass}$	area of conduction (m <sup>2</sup> )
$A_{rad}$	surface area of radiation (m <sup>2</sup> )
$I$	current (A)
$h$	coefficient of convection(W/m <sup>2</sup> .°C)
$k_{glass}$	thermal conductivity of glass (W/m.°C)
$L$	length of resistive material (m)
$P$	power (W)

$P_{RB1}$	power dissipation in resistance R <sub>B1</sub> (W)
$P_{RC1}$	power dissipation in resistance R <sub>C1</sub> (W)
$Q_{cond}$	heat loss due to conduction (J)
$Q_{conv}$	heat loss due to convection (J)
$Q_{rad}$	heat loss due to radiation (J)
$R$	resistance (Ω)
$R_A-R_F$	resistance of heater Model 1 (Ω)
$R_{A1}-R_{E1}$	resistance of heater Model 2 (Ω)
$R_S$	sheet resistance (Ωm)
$t$	thickness of resistive material (m)
$T$	temperature (°C)
$V$	voltage (V)
$w$	width of resistive element (m)
$w_1-w_2$	width of resistive element (m)
$\Delta Q$	total heat generated (J)
$\Delta t$	time (s)
$\Delta T$	temperature difference (°C)
$\Delta x$	thickness of glass substrate (m)

## Greek Symbols

$\epsilon$	total emissivity
$\rho$	resistivity (Ωm)
$\sigma$	Stefan-Boltzmann constant (W/m <sup>2</sup> .°C <sup>4</sup> )

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