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Fabrication and Simulation of TE Modules for a Feasibility Study on Harvesting Solar Heat Energy from Roof Tiles

Sakorn Inthachai¹, Supasit Paengson², Jindaporn Jamradloedluk^{1,*} and Tosawat Seetawan^{2,*}

¹Solar Energy and Energy Resources Research Unit, Faculty of Engineering, Maharakham University, Khamriang, 44150, Thailand

²Program of Physics, Faculty of Science and Technology, Thermoelectric Research Laboratory, Center of Excellence on Alternative Energy, Research and Development Institution, Sakon Nakhon Rajabhat University, Sakon Nakhon, 47000, Thailand

*Corresponding Authors: Jindaporn Jamradloedluk. Email: jindaporn.msu@gmail.com; Tosawat Seetawan.

Email: t_seetawan@snru.ac.th

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ABSTRACT

A novel roof tile thermoelectric generator (RT-TEG) was used to harvest electrical energy from a solar heat source. The RT-TEG was fabricated and simulated by flat and curved thermoelectric modules consisting of *p-n* junctions of *p*-Sb₂Te₃ and *n*-Bi₂Te₃, with an Al₂O₃ substrate at the top and bottom for heat absorption and heat rejection. The RT-TEG was installed in a roof tile to act as a generator. The electrical voltage and power values of the curved thermoelectric modules were higher than those of the flat thermoelectric module by 0.44 V and 80 mW, at a temperature difference (ΔT) of 100 K. In field tests, the RT-TEG produced a maximum electrical voltage of 33.70 mV and an electrical power of 46.24 μ W at $\Delta T \sim 7$ K under a load resistance of 1 Ω under good sunshine at 13.00 hours. The energy conversion efficiency of RT-TEG was found to be 2.24×10^{-4} .

KEYWORDS

Roof tiles micro-generator; alternative energy; thermoelectric module; harvesting energy; conversion energy

1 Introduction

Due to depletion and environmental effect of fossil fuels, renewable energy such as solar cell, wind [1], and bio-oil [2] has been more increasingly used. Thermoelectric (TE) is a device for a conversion of waste heat to electricity. It has various applications, i.e. wood stoves, natural gas use, vehicles, and solar heating [3–7]. A TE device is fabricated by using *p*- and *n*-type TE materials to form a *p-n* junction. The device has two applications: (1) A TEG, wherein electricity is generated by the Seebeck effect, and (2) Thermoelectric cooling (TEC), wherein an electrical current is applied to a *p-n* junction couple (the so-called Peltier effect). In both cases, the TE device offers the advantages of having no moving parts, no noise production, a long cycle duration, low maintenance cost, and environmental friendliness. A Bi₂Te₃-based TEG has been fabricated that operates in the low-temperature range (<623 K). Commercial preparation of bulk involves melting and quenching operations to create the desired phase composition in sealed quartz tubes, followed by crushing the materials to a powder and hot pressing [8–10]. High-performance TE materials have been obtained by preparing nanoparticles from raw materials: Rapid spark plasma sintering has been used to produce nanoparticles that exhibit increased phonon scattering and



decreased thermal conductivity [11–15]. The power factor of TE materials is defined as $PF = S^2/\rho$, where S^2/ρ , S , ρ , and T represent the power factor, the Seebeck coefficient, the electrical resistivity, and the absolute temperature, respectively.

A TE module is typically fabricated with a flat shape, where rigid ceramic substrate shapes, such as aluminum oxide (Al_2O_3) and aluminum nitride (AlN), are used to create a flat surface. However, a flat TE module cannot generate all the electricity available from a curved heat surface. Consequently, many flexible substrate materials, such as silk fabric, polyimide films, and glass fabric, are currently being developed for use with curved heat surfaces and conducting TE materials. Various approaches have been used to fabricate flexible substrates: Lu et al. fabricated a TE module by using silk fabric as a flexible substrate and Bi_2Te_3 mixed with a binder as TE materials to harvest electricity from the human body. A TE module consisting of 20 couples produced $2.08 \mu W$ at $\Delta T = 303$ K. When the flexible TEG was attached to the human body (at the chest), a power output of 178 nW was obtained at an ambient temperature of 278 K [16]. Francioso et al. successfully used RF magnetron cosputtering to fabricate a flexible TEG with a total size of 70×30 mm² by depositing Bi_2Te_3 and Sb_2Te_3 thin films on Kapton HN polyimide foil. The internal resistance of the device consisting of 100 thermocouples was 380 k Ω . An open-circuit voltage and a maximum output power of 430 mV and 32 nW, respectively, were generated at 313 K [17]. Kim et al. successfully prepared a flexible TEG by successively screen printing Bi_2Te_3 and Sb_2Te_3 pastes onto glass fabric, followed by annealing at 803 K and 773 K, respectively, in a N_2 atmosphere. The 11 as-prepared band-type flexible TEG thermocouples generated an open-circuit voltage and an output power of 2.90 mV and $3 \mu W$, respectively, when worn on human skin at an environmental temperature of 288 K [18]. Kim et al. fabricated a self-powered wireless sensor node driven by a flexible TEG for use with a heat pipe. A total energy of 272 mW were harvested over a curved area of 140×113 mm² from the heat pipe at a temperature of 343 K. They also tested a complete self-powered 34 WSN system for remote monitoring of heat pipe temperature, ambient temperature, humidity, CO_2 and volatile organic compounds [19]. However, the main problem encountered with using a flexible substrate was low heat transfer between the substrate and the surface at the cooling side and substrate deformation at nearly 573 K. Luo et al. conducted a study on a solar thermoelectric generator using phase change materials (PCMs) to absorb heat from solar radiation. A maximum voltage of approximately 2.697 V was obtained at $80^\circ C$ using the PCMs [20]. Muthu et al. investigated the performance of a solar-parabolic-dish thermoelectric generator based on PCMs. The solar parabolic dish exhibited a maximum temperature of approximately $120^\circ C$ with a solar beam radiation of $1,100$ W m⁻². A maximum power of 1 W was obtained from the TEG at an $80^\circ C$ temperature difference [21]. Lv et al. fabricated high-performance terrestrial solar thermoelectric generators without optical concentration for use on residential and commercial rooftops. The maximum peak exergy efficiency of the system reached a record value of 7.17% [22]. Maneewan et al. invented a TE-RSC composed of a transparent acrylic sheet, an air gap, a copper plate, thermoelectric modules, and a rectangular fin heat sink, which was tested under the design conditions. The test results showed that the TE-RSC generated approximately 1 W at a simulated solar intensity of 800 W m⁻² at ambient temperatures between 30 and $35^\circ C$. This TE-RSC could drive a fan to cool the cold side of thermoelectric modules [23]. Zheng et al. studied a thermoelectric cogeneration system (TCS) that enhances sustainability by improving energy efficiency in the domestic sector, which was compared with other components of a thermoelectric system. The thermoelectric block included 16 modules, a cold side, and a hot-side heat exchanger. Each module was made of Bi_2Te_3 with dimensions of $40 \times 40 \times 3.8$ mm³ and 127 thermocouples. The system viability was assessed in terms of the maximal recovery of available boiler waste heat and solar radiation. A maximum conversion efficiency of approximately 4% was obtained when the temperature difference increased to $130^\circ C$ [24].

In this study, a RT-TEG was fabricated by using a TE device made of p - Sb_2Te_3 and n - Bi_2Te_3 base materials. The thermoelectric properties of the TE materials were measured to comparatively analyze the

performance of curved and flat modules. The potential application of the RT-TEG was evaluated by measuring the electricity generated from different surfaces in a real environment.

2 Research Method

2.1 Simulation of TE Modules

TE curved and flat modules were simulated using ANSYS finite element (FE) software to predict the Joule heating value, the Seebeck coefficient, the Peltier coefficient, and the generated thermoelectricity [25]. The heat flow equations and the continuity equations of the electric charges in a system of TE devices are given by Eqs. (1) and (2) [25,26]:

$$\rho_d C_p \frac{\partial T}{\partial t} + \nabla \cdot \vec{q} = \dot{q} \quad (1)$$

where ρ_d is the density (kg m^{-3}), C_p is the specific heat capacity ($\text{J kg}^{-1} \text{K}^{-1}$), \vec{q} is the heat flux vector (W m^{-2}), and \dot{q} is the heat generation rate per unit volume (W m^{-3}); and

$$\nabla \cdot \left(\vec{J} + \frac{\partial \vec{D}}{\partial t} \right) = 0 \quad (2)$$

where \vec{D} is the electric flux density vector (C m^{-2}), and \vec{J} is the electric current density vector (A m^{-2}). The TE constitutive equation is presented by Eq. (3):

$$\vec{q} = [\Pi] \cdot \vec{J} - [\kappa] \cdot \nabla T \quad (3)$$

where Π is the Peltier coefficient matrix (V), and κ is the thermal conductivity matrix ($\text{W m}^{-1} \text{K}^{-1}$). The electrical current density generated by the Seebeck and Joule effects is given by Eq. (4):

$$\vec{J} = [\sigma] \cdot \vec{E} - [\sigma] \cdot [S] \cdot \nabla T \quad (4)$$

where σ is the electrical conductivity matrix (S m^{-1}), and S is the Seebeck coefficient matrix (V K^{-1}). The constitutive equation for a dielectric medium is $\vec{D} = \epsilon \cdot \vec{E}$, where ϵ is the dielectric permittivity matrix. Under a time-variant magnetic field, the electric field is given by: $\vec{E} = -\nabla \varphi$, where φ is the scalar electric potential. The thermoelectricity constitutive equations are then presented by Eqs. (5) and (6):

$$\rho C \frac{\partial T}{\partial t} + \nabla \cdot ([\Pi] \cdot \vec{J}) - \nabla \cdot ([\kappa] \cdot \nabla T) = \dot{q} \quad (5)$$

$$\nabla \cdot \left([\epsilon] \cdot \nabla \frac{\partial \varphi}{\partial t} \right) + \nabla \cdot ([\sigma] \cdot [S] \cdot \nabla T) + \nabla \cdot ([\sigma] \cdot \nabla \varphi) = 0 \quad (6)$$

The Galerkin method was used to convert the thermoelectric equation into a system of thermoelectric finite element (FEM) equations [27,28]. The temperature and scalar electric potential in the FEM system are approximated by $T = \vec{N} \cdot \vec{T}_e$ and $\varphi = \vec{N} \cdot \vec{\varphi}_e$, where \vec{T}_e is the nodal temperature vector, $\vec{\varphi}_e$ is the nodal electric potential vector and \vec{N} is the FEM shape function vector. The resulting system of FEM equations is shown in Eq. (7):

$$\begin{bmatrix} C^{TT} & 0 \\ 0 & C^{\varphi\varphi} \end{bmatrix} \begin{pmatrix} \vec{T}_e \\ \vec{\varphi}_e \end{pmatrix} + \begin{bmatrix} K^{TT} & 0 \\ K^{\varphi T} & K^{\varphi\varphi} \end{bmatrix} \begin{pmatrix} \vec{T}_e \\ \vec{\varphi}_e \end{pmatrix} = \begin{pmatrix} \vec{Q} + \vec{Q}^P + \vec{Q}^e \\ I \end{pmatrix} \quad (7)$$

where C^{TT} is the thermal damping matrix, $C^{\varphi\varphi}$ is the dielectric damping matrix, K^{TT} is the thermal stiffness matrix, $K^{\varphi T}$ is the Seebeck stiffness matrix, $K^{\varphi\varphi}$ is the electric stiffness matrix, \vec{Q} is the combined heat generation load vector, \vec{Q}^P is the Peltier heat load vector and \vec{Q}^e is the electric power load vector.

The FEM model was used to design a curved substrate for TE curved and flat modules with dimensions of $30 \times 30 \times 0.8 \text{ mm}^3$ and a $4 \times 4 \times 6 \text{ mm}^3$ p - n couple of 11 pairs. The element size of the TE curved and flat modules was set to 0.4 mm, for which the ANSYS simulation software automatically generated 411,177 nodes/81,228 elements and 369,025 nodes/72,255 elements, respectively, as shown in Figs. 1a and 1c. The basic calculation parameters of the TE modules were assigned in the materials model tabulated in Tab. 1. A temperature gradient of 274–373 K was applied to the top side of the TE modules, and the bottom-side temperature was set at 295 K, as depicted in Figs. 1b and 1d. A load resistance was connected the first p -type TE module and the last n -type TE module and used to determine the electrical power.

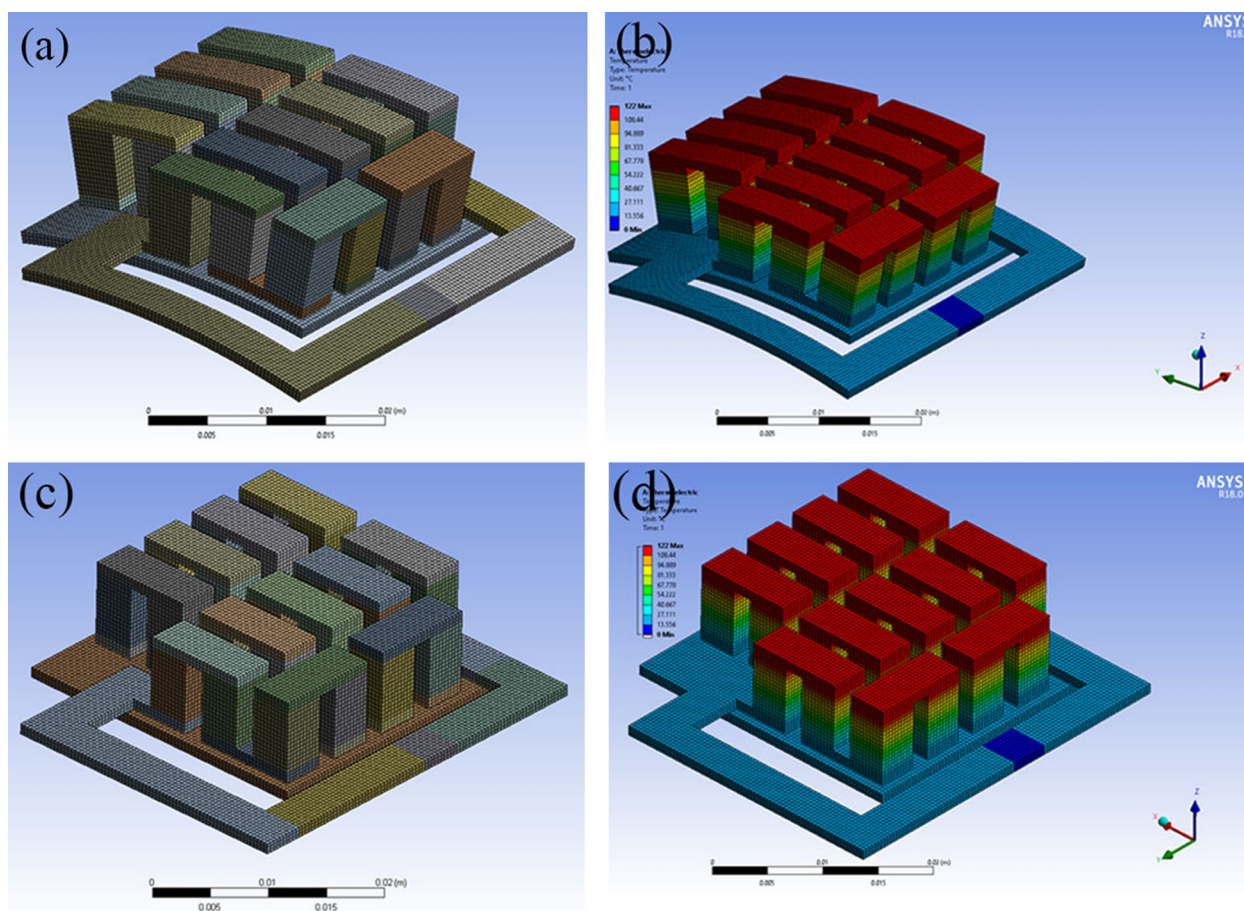


Figure 1: Design model of thermoelectric module: (a) Curved module and mesh, (b) Depiction of temperature gradient of curved modules, (c) Flat module and mesh, (d) Depiction of temperature gradient of flat modules; where calculations are performed using ANSYS for $T_H = 395 \text{ K}$ and $T_C = 295 \text{ K}$

2.2 Fabrication of TE Modules and Measurement of Electricity Power Generation

The TE curved and flat modules were fabricated from 11 pairs of p - Sb_2Te_3 and n - Bi_2Te_3 junctions with dimensions of $4.0 \times 4.0 \times 6.0 \text{ mm}^3$ (Wuhan Xinrong New Materials Co. Ltd. of China); Tab. 1 shows the TE properties measured at room temperature using a ZEM-3 (UNVAC-RIKO, Japan). Fig. 2a is a schematic circuit for TE modules designed by Solid Work 2020, consisting of 11 p - n pairs connected in series with a $4 \times 10 \times 0.05 \text{ mm}^3$ silver electrode. Curved and flat substrates were fabricated by pressing CaCO_3 under 60 MPa into a 0.8–1.0 mm thickness, followed by sintering at 1,573 K in air. An Ag electrode was fabricated on the substrates by screen coating Ag paste onto the ceramic substrate, followed by drying at 423 K for 1 h

and annealing at 1,073 K for 30 min in air. The TE legs and the Ag electrode were soldered with lead free-solder (Sn/96.5%, Ag/3%, and Cu/0.5%), where the fabricated TE modules as presented in Figs. 2b and 2c.

Table 1: Basic simulation parameters of TE modules

Parameters	Temperature (K)	p Bi ₂ Te ₃	n Sb ₂ Te ₃	Connector	CaCO ₃	Solder
Seebeck coefficient (V K ⁻¹)	300	2.04×10^{-4}	-1.72×10^{-4}	–	–	–
Resistivity (Ω m)	300	1.31×10^{-5}	1.12×10^{-5}	1.70×10^{-6}	–	1.23×10^{-10}
Thermal conductivity (W m ⁻¹ K ⁻¹) [29]	325	0.90	0.98	40.00	2.25	55.00
	375	0.83	0.93			
	425	0.85	0.93			
	475	1.15	1.08			
Semiconductor leg length/width/height (mm)	–	4/4/6	4/4/6	–	–	–
Plate thickness (mm)	–	–	–	0.20	1.00	–

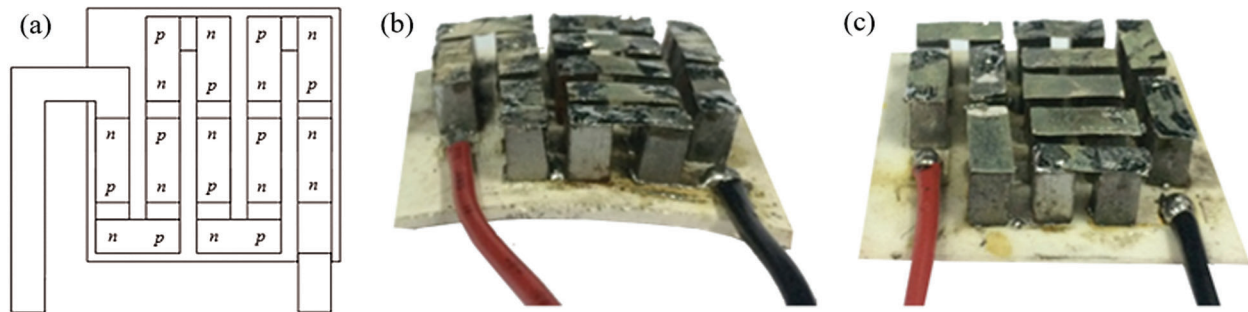


Figure 2: (a) Schematic circuit of TE modules; (b) Curved and (c) Flat fabricated TE modules

Fig. 3a is a schematic of an apparatus for measuring the electricity generated by the TE curved and flat modules that was designed using the thermoelectric consensual steady-state method. The measurement systems for the electricity generated by the TE curved and flat modules were set up following the schematic design for a ΔT range of 100 K with hot- and cold-side temperatures of 395 K and 295 K, respectively. Heating and cooling were controlled using a proportional integral derivative (PID) controller (error ± 5 K), which was installed following the shape of the TE substrate, as described in Figs. 3b and 4. Thermally conductive silicone was daubed on the top and bottom surfaces of the TE to reduce thermal contact resistance.

2.3 Fabrication of RT-TEG and Measurement of Electricity Power Generation

The RT-TEG was fabricated from curved and flat modules connected in series between p and n junctions that were filled with silicon to prevent heat loss and short circuiting; the bottom of the cold side was covered with aluminum foil to promote cooling as shown in Fig. 4(a). The RT-TEG was applied in a real situation, i.e., roof tile in a home. To consider the effects of the wind speed and temperature under the roof tile (See Fig. 4b), the experiments were conducted in triplicate for reliability.

2.4 Energy Conversion Efficiency of the System

One of the indicator to describe the performance of the RT-TEG is energy conversion efficiency. It was analyzed using Eq. (8).

$$\eta_c = \frac{\text{Power of the RT - REG}}{\text{Solar radiation} \times \text{Area of the RT - TEG}} \quad (8)$$

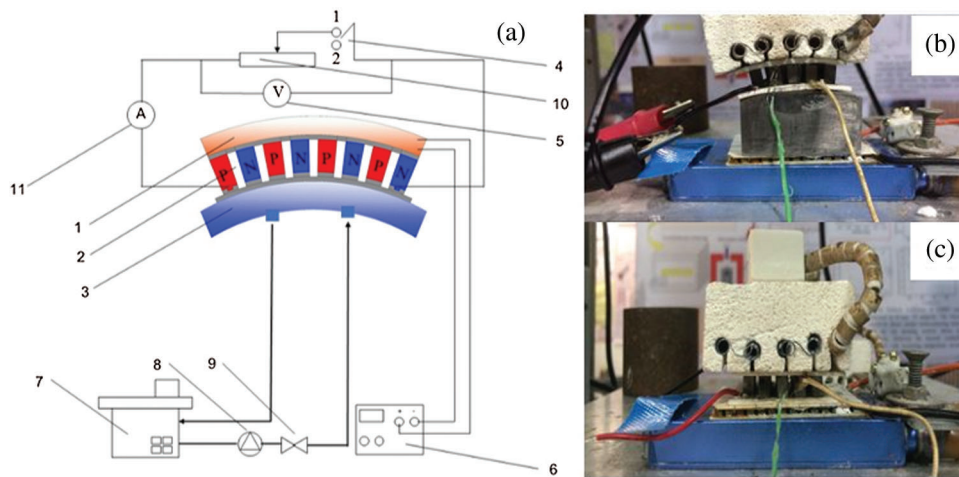


Figure 3: (a) Schematic for measuring electricity generation from flat and curved modules, where numbers denote system components: 1-heater, 2-TE module, 3-cooling system, 4-SPDT switch, 5-voltmeter, 6-PID electrical system, 7-constant temperature reservoir, 8-pump, 9-valve, 10-variable resistor, 11-amperemeter; (b) Curved module; and (c) Flat module

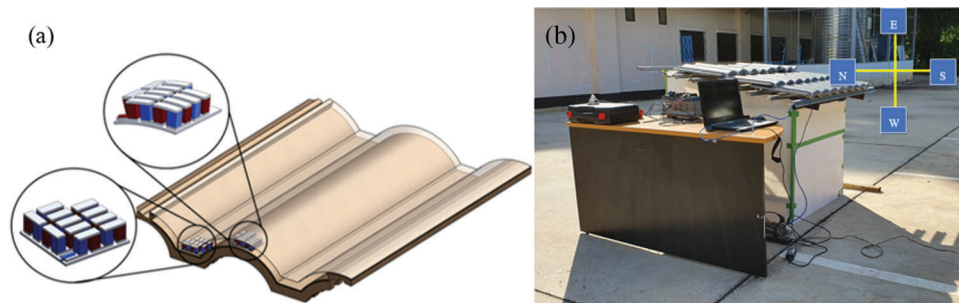


Figure 4: (a) TE consisting of curved and flat modules installed in roof tiles and (b) RT-TEG test station

3 Results and Discussion

3.1 Simulation and Experiments for TE Modules

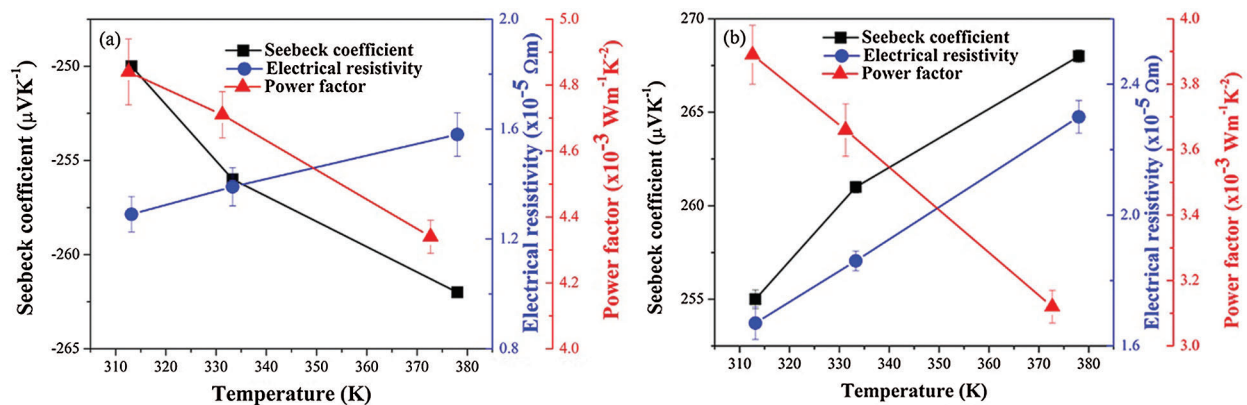
The comparative discussion on the results from curved and flat modules are presented in Tab. 2. It can be seen that voltage derived from both modules are comparable and electrical power obtained from the curved module are slightly higher than that obtained from the flat module. Such a higher power is because the curve module provides the larger temperature difference which is a driving force for power generation.

The temperature-dependent TE properties of the n -Bi₂Te₃ and p -Sb₂Te₃ materials are shown in Figs. 5a and 5b, respectively. In Fig. 5a, the S values of n -Bi₂Te₃ decrease with increasing temperature from $-250 \mu\text{V K}^{-1}$ at 310 K to $-263 \mu\text{V K}^{-1}$ at 380 K. However, these values are higher than those reported by Go-Eun Lee et al. [19]. In Fig. 5b, the S value of p -Sb₂Te₃ increased with the temperature from $255 \mu\text{V K}^{-1}$ at 310 K to $268 \mu\text{V K}^{-1}$ at 380 K. The negative and positive values of S reflected the semiconducting behavior of the n -type and p -type TE materials, respectively. By contrast, ρ of both samples increased slightly with the temperature, indicating degenerate semiconducting behavior. As shown in Figs. 5a and 5b, the electrical resistivity of the n -Bi₂Te₃ and p -Sb₂Te₃ materials is $1.58 \times 10^{-5} \Omega \text{ m}$ and $2.30 \times 10^{-5} \Omega \text{ m}$, respectively at 378 K. This behavior can be explained by considering the relationship between the Seebeck coefficient and the electrical resistivity, as defined by the Seebeck coefficient ($S = \Delta V / (T_H - T_C)$), which shows that

Table 2: The comparative discussion on the results from curved and flat modules tested at temperature difference of 373 K and load resistance of 1 Ω

Parameters	Curved module	Flat module
Simulation		
size (mm ³)	30 × 30 × 0.8	30 × 30 × 0.8
<i>p-n</i> couple	11 pairs	11 pairs
element size	0.4 mm	0.4 mm
nodes	411,177	369,025
elements	81,228	72,255
open circuit voltage	0.44	0.44
voltage	0.44	0.44
power (mW)	363.89	276.66
Fabrication		
open circuit voltage (V)	0.42	0.43
voltage (V)	0.43	0.40
power (mW)	80.67	77.68

S is inversely proportional to the carrier concentration. Consequently, the Seebeck coefficient increased with the electrical resistivity. The data presented in Figs. 5a and 5b are consistent with this equation. The power factors of *n*-Bi₂Te₃ and *p*-Sb₂Te₃ calculated by using $PF = S^2/p$ were $4.84 \times 10^{-3} \text{ W m}^{-1} \text{ K}^{-2}$ and $3.89 \times 10^{-3} \text{ W m}^{-1} \text{ K}^{-2}$, respectively, at 310 K.

**Figure 5:** Temperature-dependent Seebeck coefficient, electrical resistivity and power factor of (a) *n*-type and (b) *p*-type materials

The voltage distribution of the TE curved and flat modules was simulated by setting constant temperatures of 395 K at the hot side and 295 K at the cold side and a 1-ohm external load resistance, as depicted in Figs. 6a and 6b, respectively. Similar evenly distributed voltage distributions were obtained for both modules, in agreement with Kossyvakis' results [30].

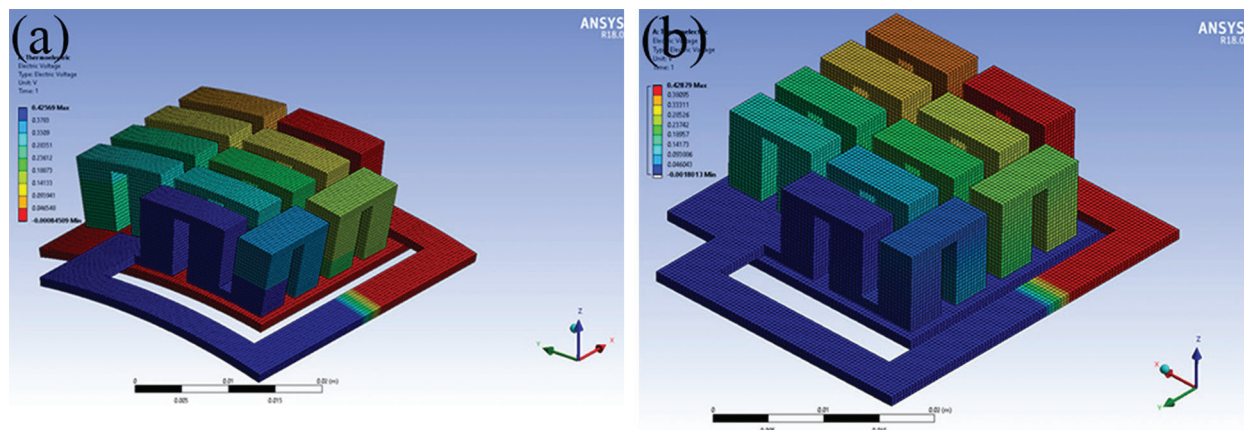


Figure 6: FEM results for voltage distribution of (a) Curved and (b) Flat modules for $T_H = 395$ K, $T_C = 295$ K and $R_L = 1 \Omega$

The simulated and experimental open circuit voltage for the curved TE module increased with the temperature and exhibited different maximum values of approximately 0.44V and 0.42V at 373 K, respectively, as shown in Fig. 7a. The simulated and experimental open circuit voltage for the flat TE module increased with the temperature and exhibited different maximum values of approximately 0.44 V and 0.43 V at 373 K, respectively, as shown in Fig. 7b. Thus, the simulated open circuit voltages for the curved and flat TE modules differed by approximately 5–10% from the experimental values. Performing the experiments in an ambient atmosphere introduces error into the voltage measurement of the TE modules. However, this measurement is used to predict the real voltage and power for use in field studies. Moreover, the curved TE module exhibits good harvesting of heat energy from a curved substrate, which is similar to that of the flat TE module and shows the feasibility of using a curved module with a curved substrate.

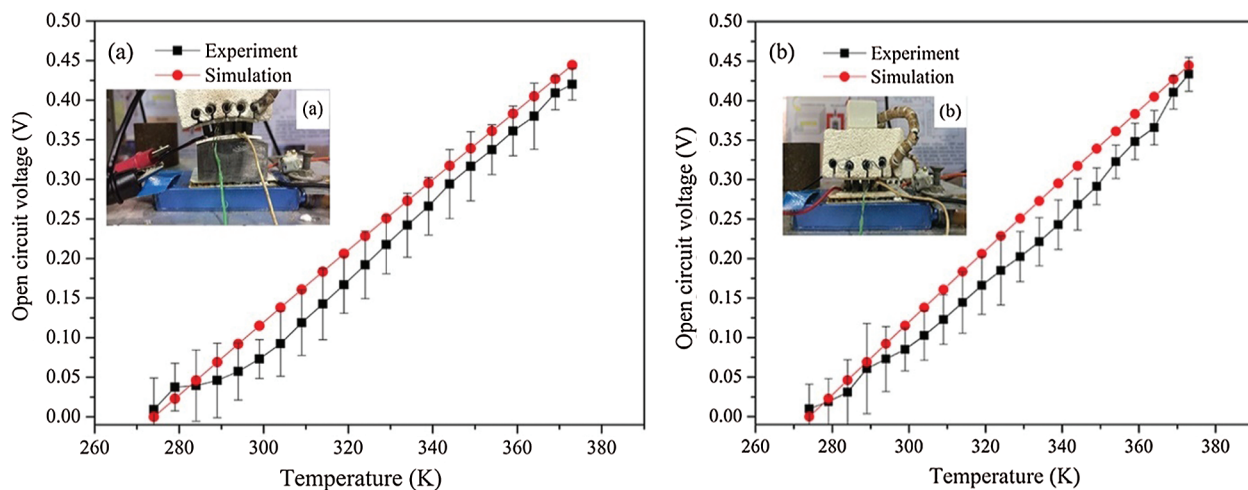


Figure 7: Comparison of measured and simulated results for open circuit voltage at outlet of (a) Curved modules and (b) Flat modules

The voltage and power of the curved and flat TE modules were measured at a ΔT of 373 K using a variable load resistance of 0–20 Ω and a fixed resistor. The electrical voltage of both modules increased with the load resistance, in agreement with results from the literatures [31–35] and the simulation, where maximum voltages of approximately 0.44 V and 0.42 V, respectively, were measured at a load resistance of 20 Ω , as presented in Fig. 8. The power of the curved and flat TE modules decreased as the load resistance increased, in agreement with the simulation results, and a maximum power of approximately 80 mW and 77 mW, respectively, was obtained at a load resistance of 1 Ω . These results showed that matching loads of approximately 1 Ω for the curved and flat TE modules, corresponding to an internal resistance of the TE modules of approximately 1.15 Ω .

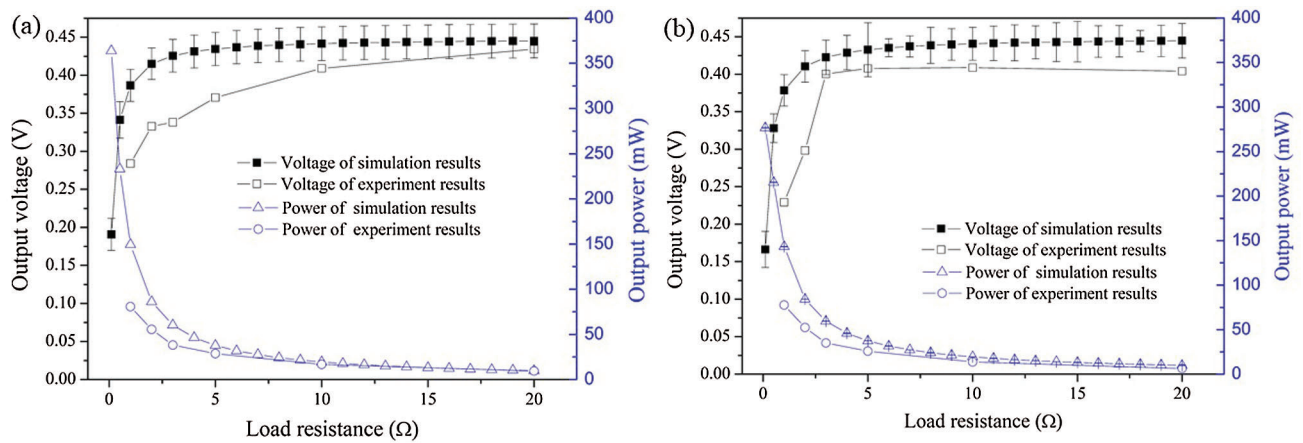


Figure 8: Comparison of numerically simulated and experimental voltage, power, and load resistance between (a) Curved and (b) Flat modules

Fig. 9 presents the daylight solar radiation and the corresponding temperature for roof tile during the experimental test, including the top-side temperature, the bottom-side temperature, and the induced temperature difference. The solar radiation at the start of daylight was approximately 200 Wm^{-2} at 06.00 hours, which induced a temperature difference of 1 K, and increased to a maximum of approximately 1,000 Wm^{-2} at 12.00–13.30 hours for a temperature difference of approximately 7 K. Clouds moved in at 14.30 hours, thereby decreasing the radiation intensity: The temperature was calculated using the Stefan-Boltzmann law for a diffuse black body system to be $T = \left(\frac{1059.4 \text{Wm}^{-2}}{\sigma_{SB}}\right)^{1/4} = 369.7 \text{ K}$, assuming that all the incoming radiation was absorbed and reemitted, which is in agreement with results reported by Bjørk et al. [36]. The hot-side temperature of the roof tile was calculated using Eq. (9)

$$T_{hot} = T_{absorb} - T_{reflect} \tag{9}$$

where T_{hot} , T_{absorb} , and $T_{reflect}$ are calculated values for the hot-side temperature, the temperature resulting from absorbed radiation, and the temperature resulting from reflected radiation (approximately 45% glossy reflection) from the roof tile, respectively, resulting in a maximum hot-side temperature of approximately 326.7 K [37–39]. However, the temperature difference was not only directly dependent on the solar radiation but also on the wind speed and ambient temperature, which produced a small variation of approximately 35% in the induced temperature difference during the field tests.

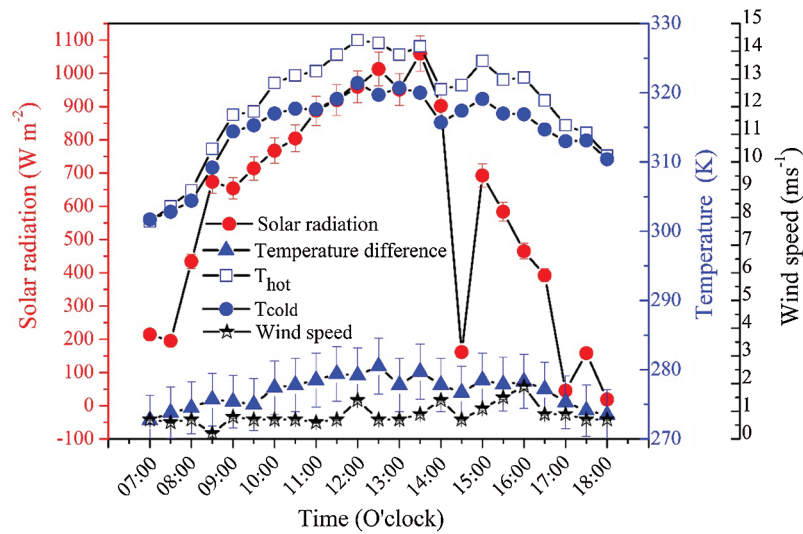


Figure 9: Relationship among solar radiation, temperature and wind speed obtained from field tests

Fig. 10 indicates how the different temperatures, power, and voltage of the RT-TEG varied during a field test conducted from 07.00–18.00 h. The different temperatures, power, and voltage increased with time until 13.00 h and then decreased. The maximum voltage and power of approximately 6.8 V and 46.24 μW , respectively, occurred at 13.00 h. Although, the power output was rather low, the results of the study are useful when using the large area, where the power output depends on the number of TE modules. Energy conversion efficiency of the system was also evaluated and it was found to be 2.24×10^{-4} .

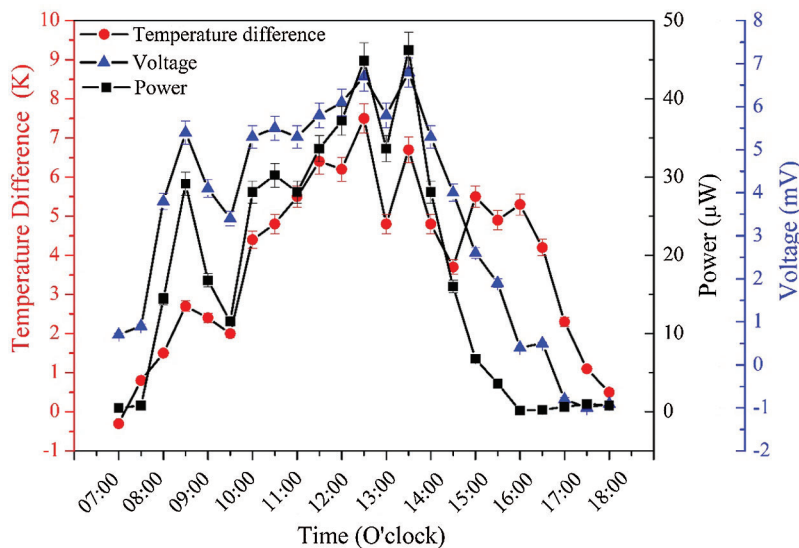


Figure 10: Electrical power and voltage of RT-TEG measured in field test

4 Conclusion

In this study, curved and flat modules were successfully fabricated from $p\text{-Sb}_2\text{Te}_3$ and $n\text{-Bi}_2\text{Te}_3$ materials. A single-phase microstructure was obtained, and the measured TE properties for the p - and

n-type materials corresponded with literature data. The maximum voltages of the curved and flat TE modules were approximately 0.44 V and 0.42 V, respectively, over a load resistance of 1–20 Ω . The power of the curved and flat TE modules decreased as the load resistance increased, in agreement with simulation results, and exhibited maximum values of approximately 80 mW and 77 mW, respectively at matching load resistances of 1 Ω . The solar intensity, electrical voltage, and power output of the RT-TEG measured in field tests increased with time until 1:30 pm and then decreased. The maximum voltage and power output of the RT-TEG were approximately 6.80 mV and 46.24 μ W, respectively, under a load resistance of 1 Ω and the solar intensity of 1,059.40 W m^{-2} . Thus, it is feasible to use curved and flat modules in roof tile: The number of modules can be increased to cover the entire surface area to increase electric power generation, and these modules could also be installed on other curved areas, such as in a furnace tube.

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Conflicts of Interest: The authors declare that they have no conflicts of interest to report regarding the present study.

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