



## An Enhanced Exploitation Artificial Bee Colony Algorithm in Automatic Functional Approximations

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### ABSTRACT

Aiming at the drawback of artificial bee colony algorithm (ABC) with slow convergence speed and weak exploitation capacity, an enhanced exploitation artificial bee colony algorithm is proposed, EeABC for short. Firstly, a generalized opposition-based learning strategy (GOBL) is employed when initial population is produced for obtaining an evenly distributed population. Subsequently, inspired by the differential evolution (DE), two new search equations are proposed, where the one is guided by the best individuals in the next generation to strengthen exploitation and the other is to avoid premature convergence. Meanwhile, the distinction between the employed bee and the onlooker bee is not made, unified as a bee and controlled by the probability  $P$ . The performance of proposed approach was examined on 14 benchmark functions, and results are compared with basic ABC and other ABC variants. As documented in the experimental results, the proposed algorithm has good optimization performance and can improve both the accuracy and the convergence speed.

**KEY WORDS:** Artificial bee colony algorithm, Bionic algorithms, search equation, optimization algorithm

### 1 INTRODUCTION

THE optimization problem is often met in the financial, economic, management, computer and other fields to seek the best solution in a finite or infinite feasible scheme. As a vital branch of applied mathematics and operational research, it has aroused wide concern and has been deeply infiltrated almost everywhere.

The traditional optimization methods include the simplex method (Dantzig, 1951), the steepest descent method (Chatterjee, 2013), etc. These approaches have shown excellent performance in solving some mathematical models, but the actual activities optimization model is established gradually to large-scale, multi-dimensional problem. Moreover, the traditional algorithms mostly depend on the initial point of objective function, continuity and differentiability of functions. Consequently, these

algorithms are often powerless for the large-scale complex optimization problems without explicit mathematical expression, which prompts people to quest for new algorithms. Later on, the biological behavior is abstracted into the mathematical model, and intelligent optimization algorithm is invented to the specific optimization problem, which shows strong vitality and adaptability. Such algorithms have no above requirements, and these advantages have attracted great attention.

The intelligent optimization algorithms mainly include genetic algorithm (GA) (Lin, et al., 2017), ant colony optimization algorithm (ACO) (Zhou, 2009), particle swarm optimization algorithm (PSO) (Tian, 2017), differential evolution algorithm (DE) (Mayer, et al., 2005), etc. The artificial bee colony algorithm (ABC) (You, et al., 2017) is also such an algorithm, proposed by Karaboga in 2005 and especially outstanding in intelligent optimization field. The ABC has been widely concerned because of its simplicity

and easy-implementation. It has been widely used in unconstrained numerical optimization, artificial neural network training, image segmentation, etc. Hence, study on algorithm improvement and theory analysis should be further work.

However, ABC also has deficiencies such as slow convergence speed and easy premature (Gao, et al., 2015). The reasons are as follows. The initial solution affects the quality of final solution to a certain extent. The more uniform the initial solution is, the wider the coverage is, and thus searching the neighborhood of the optimal solution is more likely. Yet, the basic ABC adopts random method which has blindness and is not conducive to find the optimal solution. In addition, we all know that exploration and exploitation for swarm intelligent optimization algorithm is indispensable but contradictory, with great influence on the optimization effect. When the two capabilities are in a suitable balance, the optimization effect can be the best. But the search equation of basic ABC is well exploratory, and the exploitation is poor. Subsequently, a generalized opposition-based learning strategy (GOBL) and two new search equations are applied to improve performance. That is the main contributions of this paper.

The rest of this paper is organized as follows. Section 2 depicts basic ABC and summarizes the related works. The modified ABC called EeABC is proposed and analyzed in Section 3. Section 4 discusses the experimental results. Finally, the conclusion is drawn in Section 5.

## 2 BASIC ABC ALGORITHM AND RELATED WORKS

### 2.1 Description of Basic ABC

THE artificial bee colony algorithm (Basturk, and Karaboga, 2006) divides the bees into employed bees, onlooker bees and scouter bees, and their roles in the optimization process are distinct.

Employed bees: correspond to the honey source, record information about nectar, and share information with other bees through swing dance. The nectar position is obtained by the following formula,

$$\mathbf{V}_{ij} = \mathbf{x}_{ij} + rand(\mathbf{x}_{ij} - \mathbf{x}_{kj}) \quad (1)$$

where  $\mathbf{V}_{ij}$  is the location of new nectar,  $\mathbf{x}_{ij}$  and  $\mathbf{x}_{kj}$  are  $i_{th}$  and  $k_{th}$  nectar's  $j_{th}$  position,  $rand$  is random number subjected to  $[-1,1]$ .

Onlooker bees: share the honey source information brought by employed bees. Choose a better nectar and search new source in the vicinity by Eq.(1).

Scouter bees: explore new nectar. If a nectar for a continuous generation is not updated, it will start scouter bees, randomly generated new honey instead of the original source.

The ABC algorithm searches for optimal solution through repeated search and conversion of the three bees.

Due to space limitations, a detailed description of the ABC is given by reference (Basturk and Karaboga, 2006) (Karaboga, 2005) (Karaboga and Basturk, 2007) (Karaboga and Basturk, 2008) (Karaboga and Akay, 2009).

### 2.2 Related Works about ABC

ABC is presented by Karaboga, a Turkish scholar in his technical report in 2005 (Karaboga, 2005). In 2006, Basturk and Karaboga(2006) first introduced ABC algorithm at the International Conference. In 2007, the research was published in academic journal for the first time, which described ABC algorithm, and compares with other well-known intelligent algorithms (Karaboga and Basturk, 2007). In 2008, Karaboga and Basturk(2008) were studied on optimization performance of ABC algorithm in detail, and then illustrated the performance]. In 2009, the ABC algorithm website (<http://mf.erciyes.edu.tr/abc>) was built to provide information for the researchers (Karaboga and Akay,2009). Since ABC was proposed, numerous scholars conducted researches. Zhu and Kwong(2010) proposed a gbest-guided ABC algorithm(denoted as GABC) which introduced current global optimal solution information into the search equation. Gao, Liu and Huang (2010) presented a modified ABC algorithm(denoted as ABC/best) inspired by DE algorithm, where novel search equation, chaotic systems and opposition-based learning method were introduced to enhance the global convergence. Gao and Liu(2012) improved the algorithm's exploitation capability by searching around current best solution. Kiran et al(2015) proposed the integration of multiple solution update rules with ABC, which adopted five search strategies to efficiently solve different types of optimization problems. Shan. Yasuda and Ohkura (2015) proposed a self-adaptive hybrid enhanced ABC algorithm to improve the convergence ability, search speed and control the balance between exploration and exploitation. Cui et al. (2016) introduced two novel search equations and a depth-first search (DFS) framework which was to allocate more computing resources for nectar and obtain better quality solution. Zhang et al. (2017) developed a distributed dynamic ABC based on fuzzy C-means clustering. In addition, a search equation based on the Gaussian attractor was proposed to further accelerate the diffusion of optimal solution.

The recent research on ABCs discussed above cannot be covered in this section. More recent studies can be found in related literature.

### 3 PROPOSED APPROACH

#### 3.1 The Generalized Opposition-Based Learning Strategy (GOBL)

THE uniformity of initial population distribution directly affects the convergence speed and the solution quality of the algorithm. Therefore, it plays a pivotal role to design a reasonable initialization method for improving optimization performance. In the initial phase, it is blind to the solution spatial distribution information, which requires the initial population is to be evenly distributed in the solution space so that the algorithm can uniformly search. Generally, the initial population is randomly generated, so it cannot guarantee the uniformity of population distribution. Consequently, this paper presents the generalized opposition-based learning strategy (GOBL), which can simultaneously generate a solution and the corresponding inverse solution and then ensure that the initial population is evenly distributed in the search space(Zhou, et al., 2015)(Wang, et al., 2011). The details are described as follows.

Let  $X_i = (x_{i,1}, x_{i,2}, \dots, x_{i,D})$  be a feasible solution of the current optimization problem, and its

corresponding inverse solution  $OX_i = (ox_{i,1}, ox_{i,2}, \dots, ox_{i,D})$  can be defined as:

$$ox_{i,j} = k(\mathbf{a}_j + \mathbf{b}_j) - \mathbf{x}_{i,j} \quad (2)$$

$$\mathbf{a}_j = \min(\mathbf{x}_{i,j}), \mathbf{b}_j = \max(\mathbf{x}_{i,j}) \quad (3)$$

$$i = 1, 2, \dots, SN, j = 1, 2, \dots, D$$

where  $\mathbf{x}_{i,j} \in [\mathbf{x}_{min,j}, \mathbf{x}_{max,j}]$ ,  $k \in [0,1]$  is the generalized coefficient,  $[\mathbf{a}_j, \mathbf{b}_j]$  is the dynamic boundary of the  $j^{th}$  dimension search space.

If the opposite solution is out of dynamic bounds, it is reset by randomly method:

$$ox_{i,j} = \text{rand}(\mathbf{x}_{min,j}, \mathbf{x}_{max,j}) \quad (4)$$

where  $\text{rand}(\cdot)$  is random number between  $\mathbf{x}_{min,j}$  and  $\mathbf{x}_{max,j}$ .

The pseudo-code description of GOBL is shown in Table 1.

**Table 1. The pseudo-code description of GOBL**

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|  |
|--|
| 01: $SN$ : Number of Foods   |
| 02: $D$ : Dimensionality of problem  |
| 03: // Initialization  |
| 04: for $i = 1$ to $SN$ do   |
| 05: for $j = 1$ to $D$ do  |
| 06: Randomly generated solutions $X_{ij}$ by $X_{ij} = x_{min,j} + \text{rand}(x_{max,j} - x_{min,j})$ ; |
| 07: end  |
| 08: end  |
| 09: Set the individual counter $i = 1, j = 1$ ;  |
| 10: for $i = 1$ to $SN$ do   |
| 11: for $j = 1$ to $D$ do  |
| 12: Generate opposite solutions $OX_{ij}$ by Eq. (2);  |
| 13: end  |
| 14: end  |
| 15: Selecting $SN$ best individuals from the set $\{X_{ij}, OX_{ij}\}$ as initial population.            |

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By this strategy, a feasible solution to be optimized is calculated and its opposite solution is evaluated, and then the better solution is chosen as the candidate solution. The method can improve the probability of finding the global optimal solution. What's more, the literature (Rahnamayan, et al, 2008) has mathematically proved that the GOBL strategy is a good method to estimate the original candidate solution.

#### 3.2 Novel Search Mechanism

The imbalance of search ability leads to decline the algorithm's performance, so the trade-off of exploitation and exploration is in urgent need. In formula 1, it is clear that  $\text{rand}$  is a coefficient randomly obtained in between  $[-1,1]$ , and the parameters  $j$  and  $k$  are random numbers in  $[1, D]$ , the random factors causes lack exploitation. In a word, the

basic ABC does well in exploration, but badly in exploitation. To balance the exploitation and exploration, two new search equations are designed based on the DE algorithm(Price, 2005). In the process of algorithm implementation, the distinction between the employed bee and the onlooker bee is not made, unified as a bee. Meanwhile, the probability  $P$  is used to control the above two equations and the parameter is determined by the benchmark functions(Gao and Liu, 2012). New search strategies are given as follows:

$$\mathbf{v}_i^j = \mathbf{x}_{best}^j + \phi_i^j (\mathbf{x}_{best}^j - \mathbf{x}_{rl}^j) \quad (5)$$

$$\mathbf{v}_i^j = \mathbf{x}_i^j + \phi_i^j (\mathbf{x}_i^j - \mathbf{x}_{r2}^j) \quad (6)$$

where the index  $r_1$  and  $r_2$  are random integer which belongs to  $\{1, 2, \dots, SN\}$ , and varies with  $i$ . The implication of  $i$  and  $j$  is as in the above case of Eq.(1).

The coefficient  $\varphi_i^j$  is chosen from the range of  $[-1,1]$ .

The variable  $x_r^j$  is the  $j^{\text{th}}$  dimension of  $r^{\text{th}}$  particle. The variable  $x_{best}^j$  refers to the  $j^{\text{th}}$  dimension of best

particle, guided the next iteration individual's evolution direction, which can improve exploitation.

### 3.3 Main Steps of EeABC

Based on the above explanation of improvement strategy, the pseudo-code of the EeABC algorithm is given as Table 2:

**Table 2. The pseudo-code of the EeABC algorithm**

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```

01: Data: set control parameters and concepts
02: SN: Number of Foods
03: D: Dimensionality of problem
04: limit: Maximum numbers of trial for abandoning a nectar
05: MCN: Maximum numbers of cycle
06: MFE: Maximum number of fitness evaluations, where  $MFE = D * MCN$ 
07: Begin
08: // Initialization
09: FES = 0;
10: Generate initial population by Algorithm 1;
11: trial(j) = 0;
12: FES = FES + SN;
13: i = 1;
14: Repeat
15:     While  $i < SN$  do
16:         Generate a new solution  $X(i)$  by Eq. (5);
17:         Evaluate new solution  $fit(X(i))$ ;
18:         FES ++;
19:         if  $fit(X(i)) < fit(X(j))$  then
20:              $X(j) = X(i)$ ;
21:             trial(j) = 0;
22:             if FES == MFE
23:                 Record the best solution achieved so far and exit main repeat;
24:             end
25:         else then
26:             if  $rand < p$  then
27:                 Generate a new solution  $X(j)$  by Eq. (6);
28:                 Evaluate new solution  $fit(X(j))$ ;
29:                 FES ++;
30:                 if  $fit(X(j)) < fit(X(i))$  then
31:                      $X(i) = X(j)$ ;
32:                     trial(j) = 0;
33:             else
34:                 trial(j) ++;
35:             end
36:         end
37:     end
38:     if FES == MFE
39:         Record the best solution achieved so far and exit main repeat;
40:     end
41: end
42: // Scouter bee phase
43: if  $\max(\text{trial}(j)) > \text{limit}$  then
44:     Replace  $X(i)$  with a new randomly produced solution by
45:      $X(i) = X_{min} + rand(X_{max} - X_{min})$ ;
46: end
47: until FES = MFE;
48: end

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**Table 3. Benchmark Function**

| Number | Name           | C | Search Range      |
|--------|----------------|---|-------------------|
| F1     | Sphere         | U | $[-100, 100]^D$   |
| F2     | Elliptic       | U | $[-100, 100]^D$   |
| F3     | SumSquares     | U | $[-10, 10]^D$     |
| F4     | SumPower       | M | $[-10, 10]^D$     |
| F5     | Schwefel2.22   | U | $[-10, 10]^D$     |
| F6     | Schwefel2.21   | U | $[-100, 100]^D$   |
| F7     | Quartic        | U | $[-0.5, 0.5]^D$   |
| F8     | QuarticWN      | U | $[-1.28, 1.28]^D$ |
| F9     | Ackley         | M | $[-32, 32]^D$     |
| F10    | Penalized1     | M | $[-50, 50]^D$     |
| F11    | Penalized2     | M | $[-50, 50]^D$     |
| F12    | Alpine         | M | $[-10, 10]^D$     |
| F13    | Levy           | M | $[-10, 10]^D$     |
| F14    | Shifted sphere | U | $[-100, 100]^D$   |

## 4 EXPERIMENTAL RESULTS

### 4.1 Benchmark functions

IN this paper, 14 benchmark functions with dimensions  $D=30$  are selected to validate the performance of proposed algorithm (EeABC), as listed in Table 1. These functions are divided into two categories: unimodality (U), multimodality (M), where the function characteristic are given in column C of Table 3(Kiran, 2015).

### 4.2 Experimental Comparison with Basic ABC

To validate the performance of proposed algorithm (EeABC), we compare the experimental results of EeABC with that of ABC. When experiments are to be made, the population size  $SN=40$ ,  $limit=100$ , the maximum number of fitness evaluations  $MFE=5000D$ . Through the simulation experiment, it is found that the better experimental results are obtained when  $p=0.7$ . Accordingly,  $p$  is taken as 0.7. The two algorithms run 30 times on each function independently, recording the mean and standard deviations of the results.

Table 4 presents the comparison results between the ABC and the EeABC with  $D=30$ . It can be seen: For the unimodal function, the two algorithms can obtain the theoretical optimal value of F1 and F14, and for other unimodal functions, the EeABC is superior to the ABC in the accuracy and stability. For the multimodal function, the EeABC is as efficient as ABC algorithm about F9, and the former outperforms the latter in both the accuracy and stability for other complex multimodal function.

Besides the solution quality and stability, the convergence curves are another essential measure of the performance. The convergence curves for some benchmark functions are shown in Figure 1. It can be seen that the convergence curve of EeABC is faster and can converge to a higher precision solution.

### 4.3 Experimental Comparison with ABC Variants

The experimental results of EeABC are compared with gbest-guided ABC(GABC)(Zhu and Kwong, 2010), ABC/Best/1 (Gao, et al., 2012), ABC/Best/2 (Gao, et al., 2012), and modified ABC (MABC)(Gao and Liu, 2012). These ABC variants are chosen for comparison because all the above mentioned algorithms are improved about the search equation. In the GABC algorithm, global best solution is adopted to update individuals of employed bee and onlooker bee phase. The ABC/Best/1 and ABC/Best/2 algorithms utilize various update strategy to enhance the optimization effect. Through analysis to the above algorithms, two of these strategies are picked to generate candidate solutions, combining with generalized opposition-based learning strategy (GOBL) to initial population. The comparison results illustrate that the proposed algorithm is better than the compared algorithms with regard to solution quality.

To make a clear and fair comparison, the setting parameters are in keeping with those of their corresponding papers, and the termination condition is to meet the maximum number of fitness evaluations ( $MFE$ ), setting to  $5000D$ . For EeABC algorithm, the population size  $SN=40$ ,  $limit=100$ . In the comparison tables, the mean and the standard deviation of the algorithms are given, and the contrast effect is recorded as “+/-” which means that the performance is better than, equal to, and worse than the corresponding ABCs, respectively. For the other four contrast algorithms, the experimental data are taken directly from the literature (Kiran, et al., 2015).

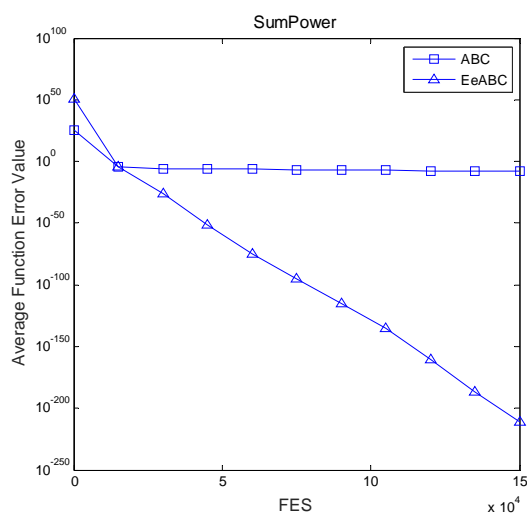
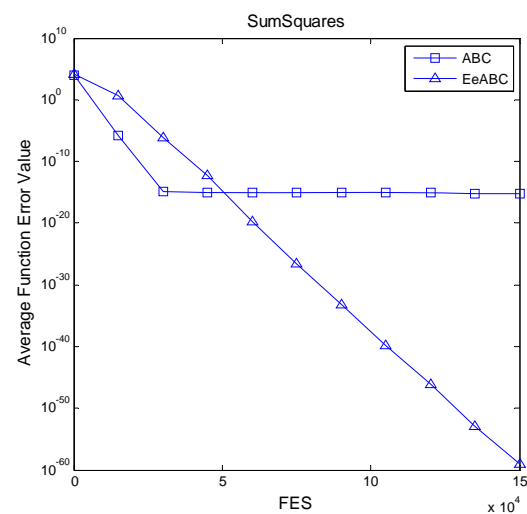
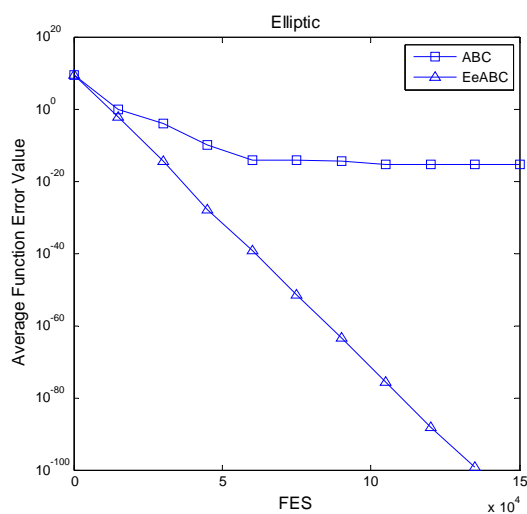
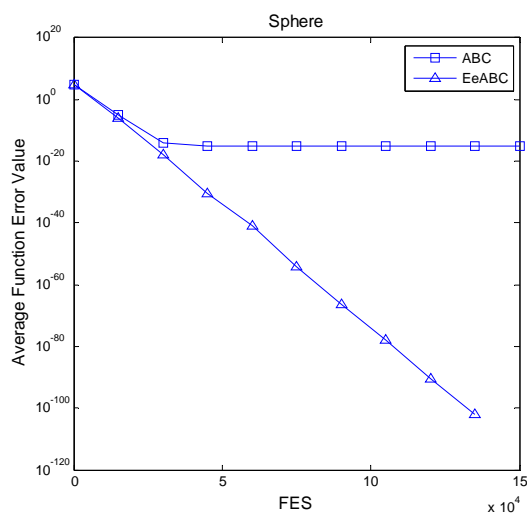
Table 5 presents the comparison results between the ABC variants and the EeABC with  $D=30$ . For F1-F5, F7, the proposed algorithm is superior to all other comparison algorithms in accuracy and stability. Especially, the EeABC can achieve the theoretical optimal value on F1. For F6, the proposed algorithm is ahead of ABC/Best/1, ABC/Best/2 and MABC, and has the same effect with GABC. For F8, F9 and F14, the EeABC is as efficient as the comparison algorithm. Especially, the proposed algorithm can

**Table 4. Experimental Results(EeABC & ABC)**

|       |      | F1       | F2        | F3        | F4        | F5       | F6       | F7        |
|-------|------|----------|-----------|-----------|-----------|----------|----------|-----------|
| ABC   | Mean | 5.10E-16 | 4.79E-16  | 5.06E-16  | 2.85E-17  | 1.28E-15 | 7.27E-01 | 2.01E-16  |
|       | SD   | 8.40E-17 | 9.88E-17  | 9.20E-17  | 9.69E-18  | 1.44E-16 | 3.25E-01 | 4.74E-17  |
|       | Sig. | +        | +         | +         | +         | +        | +        | +         |
| EeABC | Mean | 0        | 7.86E-102 | 1.84E-106 | 6.49E-223 | 1.43E-54 | 4.46E-02 | 2.40E-212 |
|       | SD   | 0        | 1.88E-101 | 4.07E-106 | 0         | 2.11E-54 | 1.74E-02 | 0         |

|       |      | F8       | F9       | F10      | F11      | F12      | F13      | F14      |
|-------|------|----------|----------|----------|----------|----------|----------|----------|
| ABC   | Mean | 4.86E-02 | 3.79E-14 | 5.08E-16 | 4.88E-16 | 8.82E-10 | 4.21E-16 | 4.91E-16 |
|       | SD   | 1.49E-02 | 3.99E-15 | 5.15E-17 | 7.45E-17 | 2.19E-09 | 8.31E-17 | 7.25E-17 |
|       | Sig. | +        | =        | +        | +        | +        | +        | +        |
| EeABC | Mean | 1.62E-02 | 3.29E-14 | 1.57E-32 | 1.35E-32 | 9.83E-16 | 1.18E-31 | 0        |
|       | SD   | 3.50E-03 | 1.15E-14 | 5.74E-48 | 5.47E-48 | 1.17E-15 | 6.56E-47 | 0        |



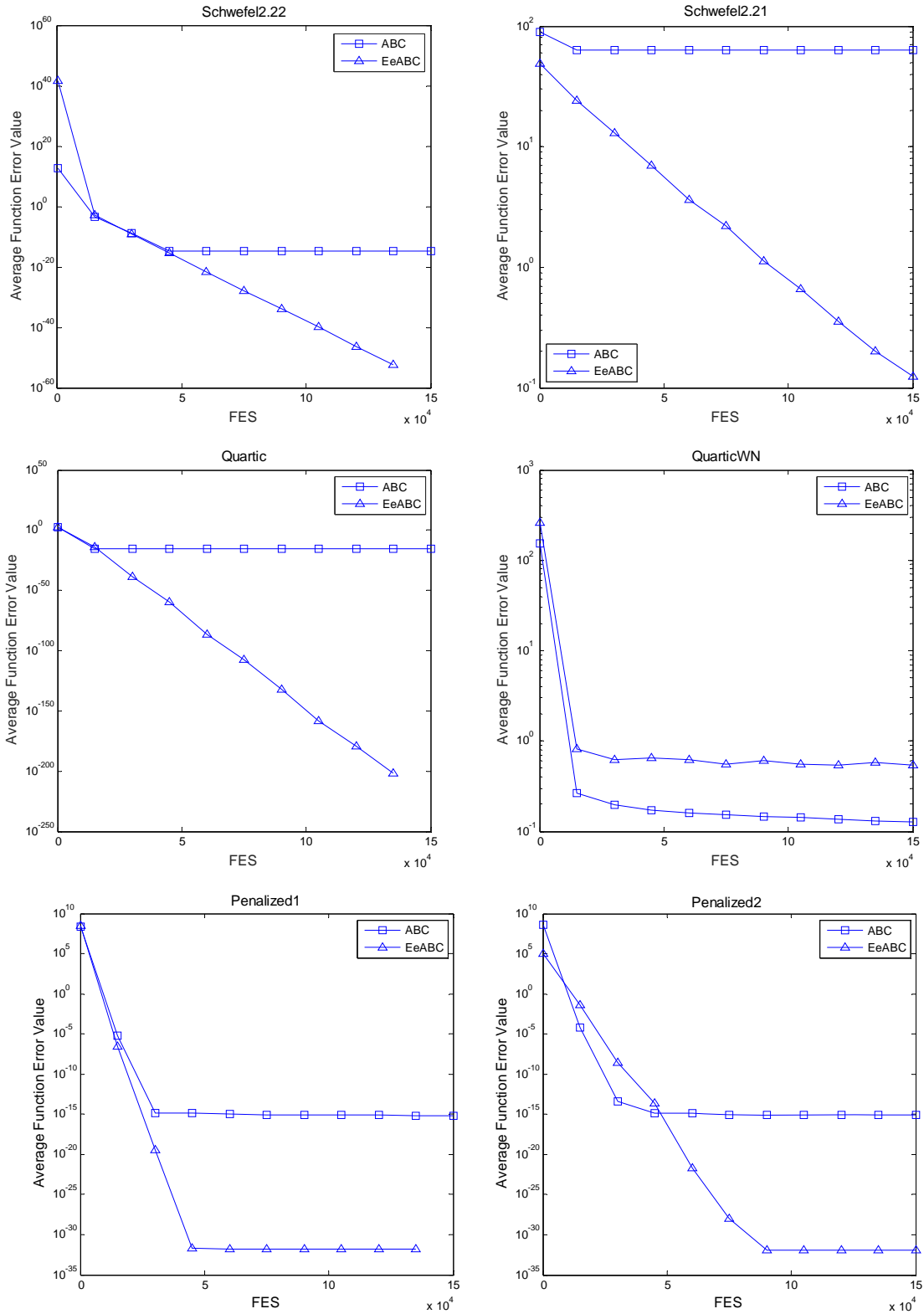


Figure 1. Partial Convergence Curve

**Table 5. Experimental Results for EeABC & ABC**

| Func | GABC     |          |      | ABCBest1 |          |      | ABCBest2 |          |      | MABC     |          |      | EeABC     |           |
|------|----------|----------|------|----------|----------|------|----------|----------|------|----------|----------|------|-----------|-----------|
|      | Mean     | SD       | Sig. | Mean     | SD       | Sig. | Mean     | SD       | Sig. | Mean     | SD       | Sig. | Mean      | SD        |
| F1   | 4.62E-16 | 7.12E-17 | +    | 3.11E-47 | 3.44E-47 | +    | 5.96E-35 | 3.61E-35 | +    | 9.43E-32 | 6.67E-32 | +    | 0         | 0         |
| F2   | 3.62E-16 | 7.88E-17 | +    | 5.35E-44 | 4.91E-44 | +    | 1.70E-28 | 2.35E-28 | +    | 3.66E-28 | 5.96E-28 | +    | 7.86E-102 | 1.88E-101 |
| F3   | 4.56E-16 | 7.00E-17 | +    | 6.50E-48 | 6.04E-48 | +    | 5.55E-36 | 3.36E-36 | +    | 2.10E-32 | 1.56E-32 | +    | 1.84E-106 | 4.07E-106 |
| F4   | 1.64E-17 | 8.07E-18 | +    | 1.77E-86 | 7.02E-86 | +    | 3.00E-46 | 1.07E-45 | +    | 2.70E69  | 5.38E-69 | +    | 6.49E-223 | 0         |
| F5   | 1.35E-15 | 1.36E-16 | +    | 2.10E-25 | 9.08E-26 | +    | 1.36E-18 | 4.27E-19 | +    | 2.40E-17 | 9.02E-18 | +    | 1.43E-54  | 2.11E-54  |
| F6   | 2.18E-01 | 4.01E-02 | =    | 2.18E+00 | 3.27E-01 | +    | 3.55E+00 | 4.79E-01 | +    | 1.02E+01 | 1.49E+00 | +    | 4.46E-02  | 1.74E-02  |
| F7   | 1.21E-16 | 3.99E-17 | +    | 2.63E-97 | 3.75E-97 | +    | 3.10E-76 | 2.89E-76 | +    | 1.45E-67 | 2.28E-67 | +    | 2.40E-212 | 0         |
| F8   | 2.03E-02 | 5.74E-03 | =    | 2.06E-02 | 4.75E-03 | =    | 2.53E-02 | 4.67E-03 | =    | 3.71E-02 | 8.53E-03 | =    | 1.62E-02  | 3.50E-03  |
| F9   | 3.20E-14 | 3.36E-15 | =    | 3.01E-14 | 2.91E-15 | =    | 3.07E-14 | 3.43E-15 | =    | 4.13E-14 | 2.17E-15 | =    | 3.29E-14  | 1.15E-14  |
| F10  | 4.12E-16 | 8.36E-17 | +    | 1.57E-32 | 5.57E-48 | =    | 1.57E-32 | 5.57E-48 | =    | 1.90E-32 | 3.70E-33 | =    | 1.57E-32  | 5.74E-48  |
| F11  | 4.01E-16 | 8.19E-17 | +    | 1.35E-32 | 5.57E-48 | =    | 1.35E-32 | 5.57E-48 | =    | 2.23E-31 | 1.46E-31 | =    | 1.35E-32  | 5.47E-48  |
| F12  | 3.41E-09 | 1.13E-08 | +    | 3.00E-16 | 8.99E-16 | +    | 3.23E-14 | 9.14E-14 | +    | 1.58E-16 | 2.48E-16 | =    | 9.83E-16  | 1.17E-15  |
| F13  | 3.28E-16 | 5.03E-17 | +    | 1.35E-31 | 6.68E-47 | =    | 1.35E-31 | 6.68E-47 | =    | 1.48E-31 | 2.30E-32 | =    | 1.18E-31  | 6.56E-47  |
| F14  | 4.38E-16 | 8.43E-17 | =    | 0        | 0        | =    | 0        | 0        | =    | 0        | 0        | =    | 0         | 0         |



achieve the theoretical optimal value on F14. For other functions, the performance of EeABC is suboptimal or equivalent to other algorithms.

On the basis of the above experimental results, the EeABC can be a very promising algorithm. And the experiments on  $D=60$  are not listed as a result of space issues.

## 5 CONCLUSION

TO sort out the issue of artificial bee colony algorithms, such as slow convergence speed and weak exploitation capacity, an enhanced exploitation artificial bee colony algorithm is proposed, called EeABC. The GOBL strategy is applied to obtain uniform initial population, and modified solution search equations are introduced to achieve a relative balance between exploitation and exploration. In addition, the performance of proposed approach was examined on 14 benchmark functions, and results are compared with basic ABC and other ABCs. As documented in the experimental results, the proposed algorithm has good optimization performance. As a consequence, EeABC may be a promising and viable tool to deal with numerical optimization problems. It is advisable to further adopt EeABC to deal with real-world problems. The studies on how to extend EeABC to handle classification of textile defects and to solve multi-objective optimization problems are our ongoing projects.

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