

Adaptive Fuzzy Logic Despeckling in Non-Subsampled Contourlet Transformed Ultrasound Pictures

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Abstract: Signal to noise ratio in ultrasound medical images captured through the digital camera is poorer, resulting in an inaccurate diagnosis. As a result, it needs an efficient despeckling method for ultrasound images in clinical practice and telemedicine. This article proposes a novel adaptive fuzzy filter based on the directionality and translation invariant property of the Non-Sub sampled Contour-let Transform (NSCT). Since speckle-noise causes fuzziness in ultrasound images, fuzzy logic may be a straightforward technique to derive the output from the noisy images. This filtering method comprises detection and filtering stages. First, image regions classify at the detection stage by applying fuzzy inference to the directional difference obtained from the NSCT noisy image. Then, the system adaptively selects the better-suited filter for the specific image region, resulting in significant speckle noise suppression and retention of detailed features. The suggested approach uses a weighted average filter to distinguish between noise and edges at the filtering stage. In addition, we apply a structural similarity measure as a tuning parameter depending on the kind of noise in the ultrasound pictures. The proposed methodology shows that the proposed fuzzy adaptive filter effectively suppresses speckle noise while preserving edges and image detailed structures compared to existing approaches.

Keywords: Image processing; fuzzy logic; directional differences; classification; ultrasound technology

1 Introduction

Medical images are increasingly being used for diagnostic purposes, posing preservation, image enhancement, analysis, and transmission problems. Medical acoustic imaging, in particular, is widely used due to its safety, non-invasiveness, utilizes non-ionizing radiation, and inexpensive cost. Even though photo quality in ultrasound B-mode has markedly enhanced in recent times. The main shortcoming in ultrasound imaging is poor image quality due to the minor variations in acoustic



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impedance and backscattered echo signals of distinct soft tissues called speckles [1]. Speckle noise reduces image contrast and distorts image features, making registration and segmentation more difficult.

Moreover, poor image quality makes it difficult for the physician to diagnose and classify the different regions in the image using computer-based systems [2,3]. Hence, speckle filtering is an essential step in the pre-processing process of ultrasound images. However, the speckle noise may include crucial diagnostic information in other cases, and removing it too much might obstruct medical analysis. Therefore, researchers developed various approaches for speckle reduction [4-6]. These methods use the local statistics of images for speckle reduction and perform well in uniform regions but fail to reduce noise in lines, textures, and edges. Therefore, many partial differential equation-based methods were proposed [7,8]. Even though these techniques are more effective at speckle removal and edge-preserving, over smoothening and fine details in the image may still be lost. However, these diffusion-based iterative approaches have difficulty distinguishing the signal from the image noise. Therefore, multi-scale analyses have been proposed [9,10]. Some real-time application of ultrasound is used in healthcare for various purposes, including obstetric sonography, diagnostic testing, blood supply assessment, and directed surgeries. These photos were taken on a real-time basis and did not contain any ionizing radiation. Ultrasound imaging is a cost-effective, accessible, and easy imaging technique. They are, nevertheless, susceptible to disturbances during capture and processing. Visual clarity is harmed by noise because it obscures image features and reduces sharpness. In ultrasound imaging, the most common noise is exponential noise, often known as speckle. While these techniques effectively remove the noises and enhance the edges, facing an artificial appearance of an image may appear in the reconstructed image.

2 Related Works

Krissian et al. [11] developed a speckle reduction filter using a matrix diffusion scheme. They use the larger window to estimate coefficient and speckle scale function variation. This method is an iterative process and achieves smooth images after despeckling, and during iterations, it removes the essential structural details. Pizurica et al. [12] used a non-homomorphic filtering scheme, in which it filters the transformed coefficients by the generalized likelihood (GenLike) method based on the likelihood ratio of local neighbors. Coupe et al. [13] anticipated a despeckling filter by Bayesian formulation to adapt a non-local mean filter (OBNLM). Automatic tuning of filter parameters needs for despeckling. Bhuiyan et al. [14] offered a despeckling filter based on a distribution modeling of noise and signal from which the noise-free signal estimate using Maximum a Posteriori Probability (MAP). Farzana et al. [15] presented a speckle reduction filter for iteratively estimating filtering parameters. It uses homogeneity metrics by modifying the bilateral filter with image denoising. Cunha et al. [16] evaluated the Nonsubsampled Contourlet Transform (NSCT) on images affected by additive noise. In terms of image enhancement, this approach outperforms the undecimated wavelet transform.

Fuzzy logic-based many despeckling filters have been proposed [17–20] for synthetic aperture radar and ultrasound images. Fuzzy edges and weights of each pixel compute from the local squared window. The main limitation is its iterative process; this estimation of filtering parameters is complex. A modified despeckling filter developed by Guo et al. [21] comprised two stages: the first step determines the maximum likelihood estimator noise-free pixel. Then, restore the details using a non-local means algorithm. The main drawback is optimizing the filtering parameter in the maximum likelihood estimator. A noise filter based on discrete topological derivatives proposes by Nedumaran et al. [22]. This technique is capable of reducing speckle noise and improving image quality. Tsakalakis et al. [23] designed a despeckling filter by combining spatial and frequency domain signals derived from the multi- transducer. The primary disadvantage is reconstructing images collected from the multiple sensors, necessitating an image registration process. Jai Jaganath Babu et al. [24] anticipated a despeckling method related to the adaptive binary morphological

operations applied on NSCT coefficients with a good edge preservation index. Still, the contrast of the denoised image is low. Singh et al. [25] developed a method by combining directional smoothing filter and wavelet thresholding by the modified Bayesshrinkage rule. This method removes the speckle noise very well. Leal et al. [26] proposed a new orthonormal wavelet relation for image denoising. Different wavelets were analyzed and performed better in edge preservation and speckle reduction. Jain et al. [27] employed a rule-based thresholding technique applied to noisy transformed images for speckle reduction.

This article proposes a novel denoising filter based on the Nonsubsampled Contourlet Transform (NSCT) and directional derivative of the transformed noisy ultrasound images. Integrates adaptiveness into two phases; in the first stage, fuzzy is applied on directional the difference features derived from NSCT coefficients to classify the regions in the transform domain. Then, the appropriate filters are applied to the classified areas using a weighted average filter to distinguish the edges and noise in the second stage. The projected algorithm is widely studied and compared with previous denoising filters on different images like standard images, simulated images, and clinical ultrasound images.

We organized this paper as follows: We cover the theoretical basis in Section 2. In Section 3, the noise model, multi-scale transform, fuzzy logic model, direction difference features fuzzy inference, and present the design of the weighted average filter. Then, Section 4 describes quantifying the outcomes of the experiments selected for the study. Finally, we conclude this study in Section 5.

3 Theoretical Backgrounds

It makes many attempts to reduce speckle noise in ultrasound pictures, which only reduces or eliminates noise and dilutes the essential features. Moreover, the techniques cannot discriminate the edge information and noises, causing sharp and weak edges to be suppressed and assuming them as noise. As a result, a method needs to reduce speckles ultimately and effectively preserve the edges and retain fine superior points in the image. The Viola-Jones technique is a method described in [28–30] for detection purposes, as the detection framework checks for features such as the total of image pixels within rectangular sections. It is highly sophisticated because it involves well over one rectangle characteristic within the approach, although it is simple to apply with a limited dataset. It can also help to minimize or remove distortion in real-world images. However, our technique is designed specifically for medical images, such as ultrasound images. Therefore, we're taking steps to improve medical image quality by reducing distortion in ultrasound images. In this article, based on the parameters extracted from NSCT transformed noisy image, fuzzy logic is applied to directional features to define each class. The proposed technique's filtering stage adapts suitable filtering methods that classify the regions to preserve details, sharp and weak edges.

3.1 Modeling of Speckle Noise

In an ultrasound picture, speckle noise displays a granular texture, and it is due to constructive and destructive ultrasound waves with objects from sub-resolution scatters [31]. The presence of speckle noise can explain using statistical and probabilistic approaches. Assume the ultrasound picture is distorted in size by multiplicative and additive noise. The noisy image before logarithmic compression described as,

$$\mathbf{R}(\mathbf{a}, \mathbf{b}) = \mathbf{I}(\mathbf{a}, \mathbf{b}) \times \mathbf{n}(\mathbf{a}, \mathbf{b}) + \mathbf{\eta}(\mathbf{a}, \mathbf{b}) \tag{1}$$

I(a, b) is the true image. It acknowledges that additive noise (sensor noise) has less influence than multiplicative noise due to coherent interference. Eq. (1) simplifies to

$$\mathbf{R}(\mathbf{a}, \mathbf{b}) = \mathbf{I}(\mathbf{a}, \mathbf{b}) \times \mathbf{n}(\mathbf{a}, \mathbf{b}) \tag{2}$$

Arsenault et al. [30] demonstrated that the speckle noise is approximately correlated with Gaussian noise when the image transforms logarithmically. By applying the logarithmic transformation, we can rewrite Eq. (2) as,

$$R'(a, b) = \log [I(a, b)] + \log [n(a, b)]$$
 (3)

NSCT uses despeckling in ultrasound images. When compared with contourlet transform, it observes that the NSCT is entirely shifting invariant, multi-scale, and multi-direction.

We develop NSCT by combining the Non-subsampled Directional Filter Banks (NSDFB) and Nonsubsampled Pyramid (NSP) to provide multi-scale properties and variable angles. For example, let R_j be the input image at *j* level. Then, NSP uses two non-sampling filters, H_0 and H_1 , to separate the input image R_j into lowpass subband R_j^0 and highpass subband R_j^1 .

$$\mathbf{R}_{\mathbf{j}}^{\mathbf{i}} = \mathbf{H}_{\mathbf{i}} \ast \mathbf{R}_{\mathbf{j}} \tag{4}$$

* is the convolution operator. The highpass subband is R_j^1 decomposed into multiple directional subbands by NSDFB. U_k^{equ} and $Y_{j,k}$ is the equivalent filter for the process mentioned above. The output of NSDFB Y_{ik} is,

$$Y_{jk} = U_k^{equ} * R_j^1$$
, where $k = 1, 2, 3...2^{lj}$ (5)

The above process works on the low-pass sub-band R_i^0 by setting

$$R_{j+1} = R_j \tag{6}$$

Then, the 'max-flat' and 'dmaxflat7' filters implement NSP and NSDFB [31]. Assume G_0 , G_1 and V_k^{equ} be the reconstruction filters of H_0 , H_1 and U_k^{equ} respectively, for reconstruction.

$$\hat{\mathbf{R}}_{j} = \mathbf{G}_{0} \ast \hat{\mathbf{R}}_{j}^{0} + \mathbf{G}_{1} \ast \hat{\mathbf{R}}_{j}^{1}$$
(7)

$$\hat{\mathbf{R}}_{\mathbf{j}}^{0} = \hat{\mathbf{R}}_{\mathbf{j}+1} \tag{8}$$

$$\hat{R}_{j}^{1} = \sum_{k=1}^{2^{ij}} V_{k}^{equ} * Y_{jk}, \text{ where } j = 1, 2, 3 \dots J$$
 (9)

The input image may then restore using the above process, which is carried out iteratively from the jth to the 1st level. The primary objective of this study is to use adaptive fuzzy logic filtering with a directional difference to denoise each directional subband.

3.2 Fuzzy Logic Model

The speckle noise influences the image pixels in ultrasound imaging and classifies regions as homogeneous, detail, or edge. So defined class has its distinct characteristics and varied membership function. As a result, we need to categorize each transformed coefficient in each directional subband as a suitable reasoning approach. As a result, we use fuzzy logic to classify each directional subband's noisy coefficient into three classes based on the degree of membership function. There are two stages in the method proposed, i.e., detection and filtering. First, the image parameter directional difference was used in the detection stage to classify each level of transformed coefficient in each directional subband for detection [32]. Then, three different filters are used on the defined classes to improve the visual quality and eliminate speckle noise.

3.2.1 Directional Difference Features

This stage's primary goal is to separate the noisy coefficients into homogeneous picture structures or edges. The neighbor reflects the features of every coefficient in the converted noisy picture. Directional Differences (DD) between altered coefficients and it identifies the neighbors to find the attributes of each coefficient in the transformed noisy image. The lesser the differential value, the more regular or homogeneous the noise coefficient is. The bigger the differential value, the more likely the noisy factor is to be considered an edge. Finally, the direction flow depicted in Fig. 1 provides the most data about the image's morphological characteristics.



Figure 1: Sliding window with four directions

We represent the coefficient and coordinates in each direction. The absolute deviation with all coefficients in every direction presents in the chosen size frame. Then average values of all differences [32] in each direction have been seen in Eq. (10).

$$D_{l} = \frac{1}{4} \sum_{x \in D_{l}} |x - x_{i,j}|$$
(10)

where, l = 1, 2, 3, 4

Above Eq. (10), these average difference values map into the fuzzy domain in each direction. As noise spreads over the transformed image, it cannot eliminate noise in the image filtering process. As a result, the Gaussian membership function integrates directional difference features into the fuzzy domain and defines Eq. (11).

$$\mu_{\rm m}^{\rm i}({\rm D}_{\rm l}) = e^{\left(\frac{-({\rm D}_{\rm l}-{\rm c}_{\rm i})^2}{2\sigma_{\rm i}^2}\right)} \tag{11}$$

Eq. (11) is the membership function of different classes with mean and variance and denotes other regions defined in the method. The graphical representation of the membership function for the various courses depicts in Fig. 2.



Figure 2: Gaussian membership functions with different class

We obtain a, b, and c values using Eq. (12) to classify different regions.

$$\mu_{\rm m}^{\rm i}({\rm D}_{\rm l}) = \begin{cases} {\rm homogenous}, & {\rm u} < b \\ {\rm detail}, & {\rm u} \ge {\rm a} \text{ and } u \le c \\ {\rm edges}, & {\rm u} > b \end{cases}$$
(12)

The coefficients with lower directional difference values belong to the uniform region. We choose the minimum value of the directional difference from $X_{\theta}^{L}(x, y)$ to set point 'a'. Coefficients with maximum directional difference value are considered edges. We determine the threshold 'c' by defining edge defined class. Edges are distinguished efficiently by gradient operation and computed from $X_{\theta}^{L}(x, y)$. To set the point 'c,' the maximum value of the directional difference is chosen. Finally, the average weight of 'a', 'c,' and 'b' values is selected.

Eqs. (13)–(17) gives the threshold calculation equations for each direction.

$$a_l = \min[R_l], \quad \text{where } l = 1, 2, 3, 4$$
 (13)

$$\mathbf{R}_{l} = \mathrm{DD}[\mathbf{X}_{\theta}^{\mathsf{L}}(\mathbf{a}, \mathbf{b})]_{\mathsf{W}\times\mathsf{W}} \tag{14}$$

$$c_{l} = peak[R_{l}^{'}]$$

$$(15)$$

$$\mathbf{R}_{1}^{'} = \mathrm{DD}[\mathrm{grad}(\mathbf{X}_{\theta}^{\mathrm{L}}(\mathbf{a}, \mathbf{b})]_{\mathrm{W}\times\mathrm{W}}$$
(16)

$$\mathbf{b}_{\mathbf{l}} = \operatorname{average}[\mathbf{a}_{\mathbf{l}}, \mathbf{c}_{\mathbf{l}}] \tag{17}$$

As a result, thresholds a, b, and c values noisy coefficients combine into different classes stated and adaptively varied in each direction based on the quantity of noise present in the ultrasound picture. Tab. 1 comprises thresholds for natural and accurate ultrasound images in different directions, and we depict them graphically in Fig. 3.

Image type	Threshold	Noise level (σ_n)					
		D1	D2	D3	D4		
Grayscale 8-bit 256 × 256 Lena picture	0.40						
	а	0.0549	0.0353	0.0510	0.0314		
	b	0.2922	0.2824	0.2902	0.2804		
	с	0.5294	0.5294	0.5294	0.5294		
	0.70						
	а	0.0902	0.0588	0.0902	0.0510		
	b	0.3098	0.2902	0.3078	0.2922		
	с	0.5294	0.5216	0.5255	0.5333		
	1.00						
	а	0.1373	0.0863	0.1059	0.0784		
	b	0.3314	0.3059	0.3176	0.3020		
	С	0.5255	0.5255	0.5294	0.5255		

Table 1: a, b, c values, arrived in four directions



Figure 3: Membership function for Lena image and ultrasound image1

3.2.2 Fuzzy Inference for Defining Class

We frame fuzzy rules to define noisy coefficients as detail, edge, and homogenous. 'Large' and 'Small' represent the connection level in each class. For the classification of each coefficient in three different classes, six rules are framed based on directional differences, as given below.

Rule 1: If $\mu_m^1(D_1)$ is large and If $\mu_m^1(D_2)$ is large and If $\mu_m^1(D_3)$ is large and If $\mu_m^1(D_4)$ is large then noisy coefficient in homogenous class **Rule 2:** If $\mu_m^2(D_1)$ is large and If $\mu_m^2(D_2)$ is large and If $\mu_m^2(D_3)$ is large and If $\mu_m^2(D_4)$ is large then noisy coefficient in detail class **Rule 3:** If $\mu_m^3(D_1)$ is large and If $\mu_m^3(D_2)$ is large and If $\mu_m^3(D_3)$ is large and If $\mu_m^3(D_4)$ is large then noisy coefficient in edge class **Rule 4:** If $(\mu_m^1(D_1)$ is large and If $\mu_m^1(D_3)$ is large) or If $(\mu_m^2(D_1)$ is large and If $\mu_m^2(D_3)$) islarge or If $(\mu_m^3(D_1)$ is large and If $\mu_m^3(D_3)$ is large) then noisy coefficient in detail class **Rule 5:** If $(\mu_m^1(D_2)$ is large and If $\mu_m^1(D_4)$ is large) or If $(\mu_m^2(D_2)$ is large and If $\mu_m^2(D_4)$ is large) If $(\mu_m^3(D_2)$ is large and If $\mu_m^3(D_4)$ is large) then noisy coefficient in detail class **Rule 6:** (If $\mu_m^1(D_1)$ is large and $\mu_m^2(D_1)$ is large and $\mu_m^3(D_1)$) is large) or (If $\mu_m^1(D_3)$ is large and $\mu_m^2(D_3)$ is large and $\mu_m^3(D_3)$) is large) or (If $\mu_m^1(D_4)$ is large and $\mu_m^2(D_4)$ is large and $\mu_m^3(D_4)$) is large) then noisy coefficient in edge class

These rules may use to easily differentiate all distinct classes of coefficients and perform effective fuzzy inference.

3.3 Speckle Denoising Filters

Let R'(a, b) be the log-transformed picture. Then, employing NSCT on R'(a, b) for "L" scales and " θ " directions per scale, the transformed picture obtains when it comes to scale and direction is X(s, L, θ).

Where, $\theta = 2^L$, $L = 2, 3, 4, \ldots$

In defining three different classes, each coefficient is $X(s, L, \theta)$ is mapped based on directional features. In the reasoning step, each coefficient is examined and classified as homogeneous, detailed, and edge regions. A suitable filter is necessary for denoising, removing the noise without altering the image's structural information. As a result, appropriate filters apply to the defined classes.

3.3.1 Homogeneous Class

For the homogenous class region, for every scale 'L' and every direction ' θ ,' a simple mean filter of size $(2K+1) \times (2K+1)$ is enough because nearby pixels are more correlated, and it is suitable to average them together by preserving details and suppressing noise away, and we define it by Eq. (18),

$$F_{\theta}^{L}(a, b) = \frac{1}{(2K+1)^{2}} \sum_{r=-K}^{K} \sum_{p=-K}^{K} X_{\theta}^{L}(a+r, b+p)$$
(18)

where, $K = 1, 2 \dots$ is an integer

3.3.2 Detail Class

Fine details carry some helpful information, and if preserved, it cannot apply a mean filter on the coefficients classified as detail region $X(s, L, \theta)$. One of the non-linear and order static filters, the median filter, can preserve edges and retains desirable information for analysis given below in Eq. (19)

$$F_{\theta}^{L}(a, b) = median(X_{\theta}^{L}(a+r, b+p)), \quad where - K \le (r, p) \le K$$
(19)

3.3.3 Edge Class

In this class, we define the transformed coefficients with maximum directional difference value as edges, and there is a chance of having noise or sharp edges. Therefore, an adaptive weighted average filter must preserve essential details in a transformed image by suppressing noise, given in Eq. (20). Based on the observation, we assign higher and lower weights for edges and noise, respectively—the weight $w_{\theta}^L(x, y)$ function is given in Eq. (21).

$$F_{\theta}^{L}(a, b) = \frac{\sum_{r=-K}^{K} \sum_{s=-K}^{K} w_{\theta}^{L}(r, p) \times X_{\theta}^{L}(a+r, b+p)}{\sum_{r=-K}^{K} \sum_{p=-K}^{K} w_{\theta}^{L}(r, p)}$$
(20)

$$w_{\theta}^{L}(a, b) = m_{\theta}^{L}(a, b) \times z(a, b)$$
(21)
where $z(a, b)$ and $m_{\theta}^{L}(a, b)$ are the similarities defined in [22] have denominative and spatial

where z(a, b) and $m_{\theta}^{L}(a, b)$ are the similarities defined in [33] based on amplitude and spatial.

$$m_{\theta}^{L}(a, b) = \exp\left(-\left(\frac{X_{\theta}^{L}(a, b) - X_{\theta}^{L}(a + r, b + p)}{\delta}\right)^{2}\right)$$
(22)

$$z(a, b) = \exp\left(-\left(\frac{r^2 + p^2}{(2K+1)^2}\right)\right)$$
(23)

where $X_{\theta}^{L}(a, b)$ and $X_{\theta}^{L}(a + r, b + p)$ is coefficient to be altered based on its neighboring coefficient defined $(2K + 1) \times (2K + 1)$ of square window size, $r, p \in [-K \text{ to } K]$. $\delta = C \times \hat{\sigma}_n$, tuning parameter (C') and noise variance $(\hat{\sigma}_n)$. It must select the tuning value 'C' specifically to filter and preserve essential details effectively. 'C' is estimated using the Structural Similarity Index Measure (SSIM), and it defines as:

$$\rho = \frac{\text{SSIM}(n+1) - \text{SSIM}(n)}{\text{SSIM}(n)}$$
(24)

Fig. 4 shows the plot between C' and ρ' for different noise levels, 0.4 and 0.7. We choose the C_{opt} value when difference value approaches below zero.



Figure 4: Tuning parameter plot for standard image

Tab. 2 shows the optimal 'C' value for standard and real images with varied noise standard deviations. As a result, the weights applied by the proposed weighted averaging filter differ depending on the picture type and the quantity of noise distorting the image.

Table 2. Copt for unrefert type s mages						
Image type	Noise levels (σ_n)					
	0.40	0.70	1.00			
Lena	0.18	0.3	0.44			
House	0.12	0.16	0.24			
Ultra sound image1	0.1	0.12	0.14			

Table 2: Cont for different type's images

Algorithm

Detection stage

Step 1: Apply log transform on observed image R(a, b) of size $M \times N$ to get R'(a, b).

Step 2: Apply NSCT on R'(a, b) to obtain $X(s, L, \theta)$

Step 3: Compute $DD[X_{\theta}^{L}(a, b)]_{W \times W}$, where $W \in [M, N]$

Step 4: Using Eqs. (13)–(17), calculate threshold values of a, b and c.

Step 5: Apply Fuzzy logic $DD[X_{\theta}^{L}(a, b)]_{W \times W}$ for the defined class using Eq. (11).

Step 6: Apply fuzzy rules to classify each transformed coefficient into three other defined regions.

Filtering stage

Initiate the tuning parameter

For each scale 'L' and each direction ' θ '

Step 1: for a = 1:M

Step 2: for b = 1:N

Step 3: if $X^L_{\theta}(a, b)$ in homogenous region

Step 4:
$$F_{\theta}^{L}(a, b) = \frac{1}{(2K+1)^2} \sum_{r=-K}^{K} \sum_{p=-K}^{K} X_{\theta}^{L}(a+r, b+p)$$

Step 5: elseif $X_{\theta}^{L}(a, b)$ in detail region
Step 6: $F_{\theta}^{L}(a, b) = median(X_{\theta}^{L}(a+r, b+p))$

Step 7: elseif $X^L_{\theta}(a, b)$ in edge or noisy region

Step 8:
$$F_{\theta}^{L}(a, b) = \frac{\sum_{r=-K}^{K} \sum_{p=-K}^{K} w_{\theta}^{L}(r, p) \times X_{\theta}^{L}(a+r, b+p)}{\sum_{r=-K}^{K} \sum_{p=-K}^{K} w_{\theta}^{L}(r, p)}$$

Apply inverse NSCT on $F_{\theta}^{L}(a, b)$ to get $\hat{F}(L, \theta)$ and apply exponential transform on $\hat{F}(L, \theta)$ to get filtered image $\hat{F}'(a, b)$. Perform relative difference in SSIM, ρ using Eq. (24). Check for the stopping condition; if $\rho(n+1) - \rho(n) < 0$, then $C = C_{opt}$ else choose another C value and repeat steps from 6 to 8.

4 Results and Discussions

All despeckling filters apply to all types of ultrasound images and analyze with other speckle reduction techniques. In this study, a speckled image obtains as defined in [34]. The quality of the denoised images evaluates using the standard metrics signal-to-noise ratio (SNR) and edge preservation (EPI) performance. To study structural similarity (SSIM) and use the quantity of filtering in the simulated pictures (USDAI). The investigational results of existing methods are obtained based on the filter parameters defined in the article. The filtered outputs of various processes for a standard noisy Lena picture with a standard deviation of 0.75 depicts in Fig. 5. With the use of existing despeckling filters, it is clear that the projected adaptive fuzzy filter with a directional difference as features efficiently eliminates speckle noise while maintaining finer details and edges in an image [35–37].



Figure 5: Denoised images of various despeckling filters. (a) Standard image (b) Noisy lena picture with standard deviation 0.75. Despeckled picture using (c) GenLike [11] (d) SNIG [12] (e) ABF [13] (f) ATMAV [17] (g) Morphological operator on NSCT [19] (h) Proposed adaptive Fuzzy on NSCT

The difference between speckled and despeckled images is obtained from the existing methods to validate the proposed method qualitatively to preserve fine details and edges. We depict the results in Fig. 6. It clearly shows that the GenLike procedure smoothens more points and edges while SNIG despeckling is very poor. In the ATMAV method, achieve smoothening in the denoised image. The morphological operator on the NSCT method filters more noise but has low contrast [38–42]. While comparing visually with other methods, the proposed denoising filter with a directional difference as a feature achieves better retention of fine details in the denoised picture.



Figure 6: Level of noise eliminated from standard picture (a) GenLike, (b) SNIG, (c) ABF (d) ATMAV (e) Morphological operator on NSCT (f) Proposed adaptive Fuzzy on NSCT

The performance of the proposed technique analyzes quantitatively by a standard edge preservation index (β) metric. We use this metric to investigate the ability of the method to preserve sharp and weak edges. We list the values of β for various despeckling methods in Tab. 3. The table list that the β value of the suggested speckle reduction scheme is more significant than other existing speckle reduction filters. It shows proposed method has good edge preservation. The edge preservation index defines as,

$$\beta = \frac{\sum (\Delta Z - \overline{\Delta Z}) \times (\Delta \hat{Z} - \overline{\Delta \hat{Z}})}{\sqrt{\sum (\Delta Z - \overline{\Delta Z})^2 \sum (\Delta \hat{Z} - \overline{\Delta \hat{Z}})^2}}$$
(25)

Accordingly, using the 3 × 3 typical Laplacian function, ΔZ and $\Delta \hat{Z}$ are the highpass filtration outputs of $\overline{\Delta Z}$ and $\overline{\Delta \hat{Z}}$, accordingly. ΔZ and $\Delta \hat{Z}$ are the average intensities of Z and \hat{Z} , accordingly. The range of β value is [0–1].

We use Signal to Noise Ratio (SNR) to analyze quantitatively for various despeckling methods, and it is defined by,

$$SNR = 10\log_{10}\left(\frac{\sigma_I}{\sigma_D}\right) \tag{26}$$

where A denotes noise-free image variance I(x, y) and σ_D , the difference in noise-free and denoised image variance, i.e., $D = I(x, y) - \hat{F}'(x, y)$, where $\hat{F}'(x, y)$, represents filtered images. Finally, we list SNR values of the various despeckling method used in this study for comparison in Tab. 4. It is observed from the table that the developed despeckling algorithm on the directional difference on NSCT outperforms well in all other methods.

Image	GenLike	SNIG	Adaptive bilateral	ATMAV	Morphological operator on NSCT	Proposed method
Lena	0.644	0.756	0.656	0.483	0.820	0.824
House	0.730	0.700	0.747	0.644	0.808	0.828

Table 3: β values for various filtering methods

Picture type	Technique for analysis	Noise standard deviation (σ_n)				
		0.60	0.70	0.80	0.90	1.00
Grayscale 8-bit 256 × 256	GenLike	14.39	13.29	12.38	11.47	10.61
Lena picture	SNIG	14.60	13.66	12.77	12.01	11.44
	ABF	14.77	13.99	12.93	12.48	11.82
	ATMAV	15.36	14.93	14.39	13.83	13.34
	Morphological operator on NSCT	18.45	17.37	16.42	15.60	15.03
	Proposed fuzzy filter on NSCT	18.35	17.62	16.60	15.84	15.20

 Table 4: SNR metric for different techniques (db)



Figure 7: Denoised image of various speckle reduction filters (a) noise free ultrasound picture (b) noisy picture (c) GenLike (d) SNIG (e) ATMAV (f) morphological operator on NSCT (g) NSCT method

We evaluated the performance of the suggested despeckling scheme with authentic ultrasound images. First, we removed the natural speckle noise from online ultrasound pictures, http://www.telin.rug.ac.be/sanja/[12]. A comparison of the proposed technique on authentic ultrasound images depict in Fig. 8. The figure shows that an adaptive fuzzy filter with a directional difference as a feature outperforms others in eliminating speckle noise and retains essential elements of an ultrasound picture. On the other side, the ATMAV [17] method smoothens the image more and fails to preserve crucial structures. In the case of [19], based on the parameters chosen, filters with less noise depicts clearly in Fig. 7.



Figure 8: Level of noise eliminated ultrasound picture (a) GenLike, (b) SNIG, (c) ATMAV (d) Morphological operator on NSCT (e) NSCT suggested method

The difference between noisy and denoised images obtained to evaluate the various despeckling techniques to preserve fine details is shown in Fig. 8. The developed despeckling algorithm on the directional difference from the difference image has retained all the essential features in the actual ultrasound image. SNIG [12] method filters noise and crucial details in the image, clearly shown in the figure. The morphological operator on NSCT [17] filters more information in the image than noise.

The case of authentic ultrasound images with the denoised image of different despeckling filtering and Noise level removed ultrasound picture depicted in Figs. 7 and 8. As a consequence, hiding the essential elements of the ultrasound image. On the other side, the suggested methodology benefits from denoising the speckle surrounding the lesions in an ultrasound picture while filtering less in the lesion structure, retaining the information features of the lesions in the ultrasound medical image.

5 Conclusions

We take an adaptive fuzzy logic filter with a directional difference as a feature for defining membership function on NSCT as proposed in this article. In the formulated technique, adaptiveness integrates into two stages. We classify image regions at the first stage by applying the membership function [35,36] to the directional difference obtained from the NSCT noisy images. Then, the system adaptively selects the better-suited filter for the specific image region, resulting in significant speckle reduction and enhanced image structural features. We use the structural similarity measure as a tuning parameter, dependent on the kind of picture and the amount of noise contained in the images. The advanced despeckling method has better edge preservation with two degrees of adaptiveness compared to the existing techniques. A study of different despeckling ways on standard, simulated and actual ultrasound pictures. Investigatory results demonstrated that the suggested scheme outperforms previous approaches in noise isolation on homogeneous regions and can preserve boundaries and tiny features in denoised images. Furthermore, our approach has better retention in textures and sharp edges for the actual ultrasound picture than the existing methods. Experiments were conducted on Field II simulated image and the outcomes achieved are improved than the other approaches. The proposed technique outperforms well than other current techniques quantitatively as well as qualitatively.

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