

Dynamic Sliding Mode Backstepping Control for Vertical Magnetic Bearing System

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Abstract: Electromagnets are commonly used as support for machine components and parts in magnetic bearing systems (MBSs). Compared with conventional mechanical bearings, the magnetic bearings have less noise, friction, and vibration, but the magnetic force has a highly nonlinear relationship with the control current and the air gap. This research presents a dynamic sliding mode backstepping control (DSMBC) designed to track the height position of modeless vertical MBS. Because MBS is nonlinear with model uncertainty, the design of estimator should be able to solve the lumped uncertainty. The proposed DSMBC controller can not only stabilize the nonlinear system under mismatched uncertainties, but also provide smooth control effort. The Lyapunov stability criterion and adaptive laws are derived to guarantee the convergence. The adaptive scheme that may be used to adjust the parameter vector is obtained, so the asymptotic stability of the developed system can be guaranteed. The backstepping algorithm is used to design the control system, and the stability and robustness of the MBS system are evaluated. Two position trajectories are considered to evaluate the proposed method. The experimental results show that the DSMBC method can improve the root mean square error (RMSE) by 29.94% compared with the traditional adaptive backstepping controller method under different position tracking conditions.

Keywords: Magnetic bearing system (MBS); Lyapunov stability; dynamic sliding backstepping control (DSMBC) algorithm; adaptive laws; model uncertainty

1 Introduction

Dating back to 1842, it was first proposed to use permanent magnets or fixed current electromagnets alone. No matter how they were configured, it was impossible to suspend a magnetically guided object stably in midair, so it was necessary to find ways to better stabilize the operation. The active magnetic bearing was first produced in 1937 [1,2]. The MBS have many advantages over mechanical and hydrostatic bearings. These include zero frictional wear and efficient operation at extremely high speeds.



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In addition, they are considered an ideal choice for clean environments as they do not require lubrication. MBS are used in many applications, such as energy storage flywheels, high-speed turbines, compressors, pumps and jet engines. Compared with other bearings, magnetic bearings have many advantages [3], as follows: (1) It has almost no rotation resistance and the rotor speed can be much higher than other bearings; (2) They do not require complex lubrication or pneumatic system and can save space; (3) They have a long service life and low maintenance cost; (4) They can avoid the friction-induced noise; (5) They can be applied to special working environment such as under extremely low temperature or high vacuum; (6) They can provide the required rigidity through active control and effectively restraining the vibration problem caused by high-speed operation. Because of the advantages mentioned above, the magnetic floating bearings have been widely used in many fields.

In recent years, several researches have been devoted to the development of magnetic floating bearings [4]. Although many studies have determined the magnetic circuit structure and mechanical structure design of magnetic floating bearings, few researchers have analyzed and studied the nonlinear dynamic characteristics of the magnetic bearing system (MBS). Besides, two estimator based nonlinear controllers [5,6] have been proposed, which are used to estimate the total uncertainty of parameter variations and external disturbances in real time. The design of backstepping control [6,7] cannot respond to the input signals effectively, so it should be combined with the adaptive estimator [8] to estimate the unknown parameters of the system. In the self-tuning controller, the parameters are adapted and the estimated parameters are provided to the controller to solve the nonlinear problem of the MBS. The adaptive backstepping controller [9] can perform better steady-state response by using an estimation system with adaptive rules.

This research paper promotes the application of dynamic sliding mode backstepping control (DSMBC) for the MBS [10]. The slip line from the sliding mode control is used to estimate the total uncertainty of the system. The slope of the sliding line tends to make the coming speed faster, so that the response is compensated in time. Moreover, the estimated values are more effective to reach the accurate values. In this case, the system produces better results than the backstepping control. The Lyapunov function is used in the backstepping control to guarantee the convergence of the position tracking error. Two height position tracking is considered and tested. The simulation and experimental results demonstrate that the developed controller provides better tracking performance in the respect of model uncertainty.

The rest of this paper is structured as follows. Section II introduces the construction of the MBS and system model. In Section III, the dynamic sliding backstepping control is designed and analyzed. Section IV provides the experimental results. Finally, in Section V, conclusions are drawn.

2 Magnetic Bearing System Architecture

The structure of MBS is illustrated in Fig. 1. The system consists of a permanent magnet part and an electromagnet part. The magnetic bearing can float in the air when the electromagnet is electrified. The output current can reduce the power consumption to better alleviate the power required when the magnetic bearing position moves near the center. After comparing the command signal with the height signal feedback, the error signal is sent to the power amplifier through the controller operation. Furthermore, the voltage of the controller is transformed into electric current by a power amplifier and sent to an electromagnet to produce magnetic force. After the magnetic bearing can be suspended in the air, the height information is measured using an infrared sensor. The servo motor is used as the load platform, through which the load is added to complete the experiment. According to the Newton's laws of motion, the dynamic system model is given by



Figure 1: The structure of MBS

$$m\ddot{x} = F_z - mg + f_d \tag{1}$$

where *m* is the bearing mass with a parameter of 1.6 kg, f_d is external interference, *x* is the position of the magnetic bearing, and F_z is the sum of the magnetic forces produced by the top and bottom of the electromagnet. In Fig. 2, the nonlinear electromagnetic force [11,12] can be expressed as

$$F_z = k \left[\frac{(i_0 + i_c)^2}{(x_0 + x)^2} - \frac{(i_0 - i_c)^2}{(x_0 - x)^2} \right]$$
(2)



Figure 2: The electric currents and the positions of magnetic bearing

where x_0 and i_0 are the initial position of magnetic bearing and the initial electric current respectively, i_c is the control current, and k is the electromagnetic force coefficient. Fig. 2 shows the current of magnetic bearing and the relationship between the positions. The nonlinear electromagnetic force is modeled and linearized by using the curve fitting method [12], and is defined as

$$F_z \cong -C_z x_1 + C_i i_c \tag{3}$$

where C_z is the position parameter, and C_i is the current parameter. Eqs. (3) and (4) are substituted into Eq. (1), and obtain

$$m\ddot{x} = -C_z x_1 + C_i i_c - mg + f_d \tag{4}$$

The dynamic system can be written as

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -C_z & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ C_i \end{bmatrix} \dot{i}_c + \begin{bmatrix} 0 \\ -mg + f_d \end{bmatrix}$$
(5)

where $\mathbf{x} = \begin{bmatrix} x_1 & x_2 \end{bmatrix}^T = \begin{bmatrix} x & \dot{x} \end{bmatrix}^T \in R^2$ is the state vector of system.

3 Proposed Dynamic Sliding Backstepping Control

3.1 Conventional Adaptive Backstepping Control

The MBS can be considered as a general second-order nonlinear system.

$$\dot{\mathbf{x}} = \mathbf{f}(\mathbf{x}) + \mathbf{b}(\mathbf{x})\mathbf{u} \tag{6}$$

$$\mathbf{y} = \mathbf{x} \tag{7}$$

where $f(\mathbf{x})$ and $\mathbf{b}(\mathbf{x})$ are unknown continuous nonlinear functions, $\mathbf{u} \in \mathbf{R}$ is the control input, $\mathbf{y} \in \mathbf{R}$ is the system output, and $\mathbf{x} = \begin{bmatrix} x_1 & x_2 \end{bmatrix}^T = \begin{bmatrix} x & \dot{x} \end{bmatrix}^T \in \mathbf{R}^2$ is the state vector of the system, which is assumed to be available for measurement. In order for the dynamic system to be controllable, the function $\mathbf{b}(\mathbf{x})$ must be nonzero for vector x in certain controllability region. Without losing generality, we assume that $0 < \mathbf{b}(\mathbf{x}) < \infty$. Considering the effect of parameter uncertainty, the dynamic equation is written as

$$\dot{\mathbf{x}} = \mathbf{f}_1(\mathbf{x}) + \mathbf{b}_1(\mathbf{x})\mathbf{u} + \mathbf{E}(\mathbf{x}) \tag{8}$$

where $f(\mathbf{x}) = f_1(\mathbf{x}) + f_2(\mathbf{x})$, $b(\mathbf{x}) = b_1(\mathbf{x}) + b_2(\mathbf{x})$, and $E(\mathbf{x}) = f_2(\mathbf{x}) + b_2(\mathbf{x})u$,

 $f_1(\mathbf{x})$ and $b_1(\mathbf{x})$ are the known real continuous functions. $f_2(\mathbf{x})$ and $b_2(\mathbf{x})$ are the unknown real continuous functions. The tracking error selected is $z_1 = x_d - x_1$. x_d is the desired height. The differential height error defined is as follows

$$\dot{z}_1 = \dot{x}_d - \dot{x}_1 = \dot{x}_d - x_2 \tag{9}$$

The stability function is defined as

$$\alpha = c_1 z_1 + \dot{x}_d \tag{10}$$

where c_1 is a positive constant. The variable z_2 is defined as

$$z_2 = -\dot{x}_1 + \alpha \tag{11}$$

where z_2 is the stability function.

The difference between the actual value of the total uncertainty and the estimated value of the total uncertainty is given as

$$\tilde{E}(\mathbf{x}) = E(\mathbf{x}) - \hat{E}(\mathbf{x})$$
(12)

The continuous Lyapunov function is defined as

$$V_1 = \frac{1}{2}z_1^2 \tag{13}$$

The time derivative of function V_1 can be expressed as

$$\dot{V}_1 = z_1(z_2 - c_1 z_1) \tag{14}$$

The second Lyapunov function is selected as

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$$V_{b2} = V_1 + \frac{1}{2}z_2^2 + \frac{1}{2r}\tilde{E}^2(\mathbf{x})$$
(15)

where r is a positive constant. After differentiation operation, it can be expressed as

$$\dot{V}_{b2} = \dot{V}_1 + z_2 \dot{z}_2 - \frac{1}{r} \tilde{E}(\mathbf{x}) \dot{\tilde{E}}(\mathbf{x})$$

$$= z_1 (z_2 - c_1 z_1) + z_2 (-\ddot{x}_1 + \dot{\alpha}) - \frac{1}{r} \tilde{E}(\mathbf{x}) \dot{\tilde{E}}(\mathbf{x})$$

$$= z_1 (z_2 - c_1 z_1) + z_2 (-f_1(\mathbf{x}) - \mathbf{b}_1(\mathbf{x})u - (\tilde{E}(\mathbf{x}) + \hat{E}(\mathbf{x})) + c_1 \dot{z}_1 + \ddot{x}_d) - \frac{1}{r} \tilde{E}(\mathbf{x}) \dot{\tilde{E}}(\mathbf{x})$$

$$= z_1 (z_2 - c_1 z_1) + z_2 (-f_1(\mathbf{x}) - \mathbf{b}_1(\mathbf{x})u - \hat{E}(\mathbf{x}) + c_1 \dot{z}_1 + \ddot{x}_d) - \tilde{E}(\mathbf{x}) \left(\frac{1}{r} \dot{\tilde{E}}(\mathbf{x}) + z_2\right)$$
(16)

The ideal control input u(t) is defined as

$$u(t) = \frac{1}{b_1(x)} \left(\ddot{x}_d - \mathbf{f}_1 + c_1 \dot{z}_1 + z_1 - \hat{E}(\mathbf{x}) + \beta sign(z_2) \right)$$
(17)

$$\hat{E}(\mathbf{x}) = rz_2 \tag{18}$$

where β is a positive constant.

Substituting Eqs. (16) and (17) into Eq. (15), which can be represented as

$$\dot{V}_{b2} = -c_1 z_1^2 - z_2 \beta sign(z_2) = -c_1 z_1^2 - \beta |z_2| \le 0$$
(19)

By using the control law, the state can always approach the sliding surface and hit it. The asymptotic stability of the system can be guaranteed.

3.2 Proposed Dynamic Sliding Mode Backstepping Control

The DSMBC method is derived and developed in the MBS system. The tracking error is defined as $z_1 = x_d - x_1$. The x_d is the desired height. The error differentiation variable is given as follows \dot{z}_1

$$x_1 = \dot{x}_d - \dot{x}_1 = \dot{x}_d - x_2 \tag{20}$$

The stability function can be given by

$$\alpha = \mathcal{C}_1 z_1 + \dot{x}_d. \tag{21}$$

where C₁ is a positive constant. The sliding surface is selected as

$$S = \dot{z}_1 + C_2 z_1 \tag{22}$$

where C_2 is a positive constant. The difference between the actual value of the total uncertainty and the estimated value of the total uncertainty is given by

$$\tilde{E}(\mathbf{x}) = E(\mathbf{x}) - \hat{E}(\mathbf{x})$$
(23)

where E is the actual value of the total set uncertainty. The error parameter of C_2 is defined as

$$\tilde{C}_2 = C_2 - \hat{C}_2 \tag{24}$$

where C_2 is a constant. The variable z_2 is defined as

$$z_2 = -\dot{x}_1 + \alpha \tag{25}$$

The candidate Lyapunov function is given by

$$V_1 = \frac{1}{2} z_1^2 \tag{26}$$

The time derivative of the Lyapunov function is

$$\dot{V}_1 = z_1 \dot{z}_1 = z_1 (\dot{x}_d - \dot{x}_1)
= z_1 (-\dot{x}_1 + \alpha - C_1 z_1) = z_1 (z_2 - C_1 z_1)$$
(27)

The second Lyapunov function can be written as

$$V_{b3} = V_1 + \frac{1}{2}S^2 + \frac{1}{2n_1}\tilde{E}^2(\mathbf{x}) + \frac{1}{2n_2}\tilde{C}_2^2$$
(28)

where n_1 and n_2 are positive constants. The differential operator is used and it becomes

$$\dot{V}_{b3} = \dot{V}_1 + S\dot{S} - \frac{1}{n_1}\tilde{E}(\mathbf{x})\dot{\dot{E}}(\mathbf{x}) - \frac{1}{n_2}\tilde{C}_2\dot{\dot{C}}_2$$

$$= z_1(z_2 - C_1z_1) + S[-f_1(\mathbf{x}) - b_1(\mathbf{x})u - (\hat{E}(\mathbf{x}) + \tilde{E}(\mathbf{x})) + \dot{z}_1(\tilde{C}_2 + \hat{C}_2) + \ddot{x}_d] - \frac{1}{n_1}\tilde{E}(\mathbf{x})\dot{\dot{E}}(\mathbf{x}) - \frac{1}{n_2}\tilde{C}_2\dot{\dot{C}}_2$$

$$= z_1(z_2 - C_1z_1) + S[-f_1(\mathbf{x}) - b_1(\mathbf{x})u - \hat{E}(\mathbf{x}) + \dot{z}_1\dot{C}_2 + \ddot{x}_d] - \tilde{E}(\mathbf{x})\left(\frac{1}{n_1}\dot{\dot{E}}(\mathbf{x}) + S\right) - \tilde{C}_2\left(\frac{1}{n_2}\dot{\dot{C}}_2 - \dot{z}_1S\right)$$
(29)

The ideal control law is defined as

$$u(t) = \frac{1}{b_1(\mathbf{x})} \left(\ddot{x}_d - f_1(\mathbf{x}) + \dot{z}_1 \hat{C}_2 - \hat{E}(\mathbf{x}) + \beta_1 sign(S) + \frac{1}{S+\lambda} z_1 z_2 \right)$$
(30)

$$\dot{\hat{C}}_2 = n_2 S \dot{z}_1 \tag{31}$$

$$\dot{\hat{E}} = -n_1 S \tag{32}$$

where β_1 is a positive constant, and λ is the limited coefficient.

Substituting Eqs. (29), (30) and (31) into Eq. (28), we obtain

$$\dot{V}_{b3} = -C_1 z_1^2 - S \beta_1 sign(S) = -C_1 z_1^2 - \beta_1 |S| \le 0$$
(33)

If $\eta_d > 0$, it can be expressed as

$$\begin{aligned} \dot{V}_{b3} &= -K - \eta |S| \\ &\leq -\eta_d |S| \end{aligned} \tag{34}$$

with
$$C_1 z_1^2 = K > 0, \, \eta_d > \eta_d$$

Integrating the above equation with respect to time, resulting in

$$\int_{0}^{\tau} |S(\tau)| d\tau \le \frac{1}{\eta_d} [V_{b3}(0) - V_{b3}(t)]$$
(35)

Because $V_{b3}(0)$ is bounded, and $V_{b3}(t)$ is nonincreasing and bounded. We obtain that S is bounded, which implies $S \in L_{\infty}$ [13,14]. By using Barbalat's lemma [5,13,14], S will converge to zero as $t \to \infty$. And the lemma implies that $\lim_{t\to\infty} |e(t)| = 0$. Thus, the designed system is stable and the error converges to zero asymptotically. The stability of the DSMBC scheme is guaranteed.

4 Experimental Results

The experimental results show the control capability of the developed algorithm for MBS. In this study, two types of control methods are compared. They are (a) the adaptive backstepping control method, (b) the proposed DSMBC method. Fig. 3 illustrates the experimental setup of the MBS equipment.



Figure 3: A photograph of the MBS system

Fig. 4 describes a block diagram of an adaptive backstepping control system. The MBS system with uncertainties is considered and analyzed. An error estimator is designed to estimate the system with unknown parameters. The estimator can modify the parameters according to the signal fed back to the system. It can also provide the estimated parameters to the controller on-line and calculate the estimated values of the parameters. The adaptive estimation scheme and backstepping control are used to solve the nonlinear problem of MBS. The adaptive backstepping control can keep the robustness of the system when the parameters of the system change or external disturbance occurs.



Figure 4: The system structure of adaptive backstepping controller

The system block diagram of the proposed DSMBC of the magnetic bearing is shown in Fig. 5. After the height command is obtained from the system, the controller can send the control command, and know the bearing system's height and the calculation error subtracted by command. Then, the output of the bearing system enters the control card to calculate the error adjustment sliding mode control to estimate the uncertainty. After adjustment, it enters the control card operation until the command is chased. The controller tends to be based on step-return control and cooperates with the sliding. The model can estimate the uncertainty, where we adjust the parameter C_2 to achieve faster compensation when the bearing encounters external disturbance.



Figure 5: The system structure of dynamic sliding mode backstepping controller

Tab. 1 lists the controller and MBS parameters in this research. The parameters were determined according to the rule of thumb to achieve better transient and steady-state responses under simulated and experimental conditions, considering the requirements of stability.

	1	
Control Methods	MBS Parameters	Controller Parameters
Adaptive backstepping controller	$C_z = 21, m = 1.6, g = 9.8,$ $C_z = 2641.6$	$c_1 = 0.03, r = 50, K = 0.1651$
controller		$K = 0.651, n_1 = 1, n_2 = 1.4, \epsilon = 1.23$

 Table 1: Controller and MBS parameters

4.1 Simulation Results

The simulation results using adaptive backstepping control method and the proposed DSMBC method were obtained and compared to verify the control performance.



Figure 6: The simulation response of 2.5 mm command height. An additional external load of 0.3 A is added at $t \ge 5$ s. (a) Comparison of the height output responses, (b) comparison of the height error responses, (c) comparison of the control inputs, (d) comparison of the estimated uncertainty responses



Figure 7: The simulation response of 2.5 mm height command during $0 \le t < 5$ s. The height command changes to 2.3 mm at $t \ge 5$ s, and an additional external load of 0.3 A is added at $t \ge 10$ s. (a) Comparison of the height output responses, (b) comparison of the height error responses, (c) comparison of the control responses, (d) comparison of the estimated uncertainty responses

In Fig. 6, the output response of command height is 2.5 mm, and an additional external load of 0.3 A is added at $t \ge 5$ s. In addition, it is clear from Fig. 6a that the overshoot response of adaptive backstepping control method is bigger and faster. The DSMBC method has a slower transient response, but a height response can be rendered smoother and more accurate. Compared with the tracking response depicted in Figs. 6b–6d, the conventional sliding mode backstepping control has larger tracking error and estimation error. Therefore, the DSMBC approach can have better error convergence than backstepping control scheme.

As shown in Fig. 7, the adaptive backstepping control has a faster transient response, as illustrated in Fig. 7a. However, the DSMBC method achieves the robustness performance under difference inputs and load conditions. The amount of control increases immediately after the height command changes, see Fig. 7c. Meanwhile, in Fig. 7d, the DSMBC also outperforms the adaptive backstepping control for estimation comparison. It can be seen that the DSMBC method performs better in real-time compensation and robustness tracking regardless of the height command and load disturbance.

4.2 Experimental Results

To verify the practicality of the proposed DSMBC system, the experimental tests were performed and demonstrated. Fig. 8 depicts that the height command is set as 2.5 mm during $0 \le t < 5$ s and an additional external load of 0.3 A is added during $t \ge 5$ s. The two adaptive controllers are employed, and the adaptive laws are also developed to estimate the uncertainty of the model. The parameters of DSMBC are adjusted adaptively, so that the adaptation gain can improve the tracking accuracy effectively. Figs. 8a–8d show that the DSMBC method has a faster response time and less overshoot than the traditional adaptive method. The DSMBC method can quickly track the height command in the transient state and has a smooth response in the steady state.



Figure 8: The experimental responses of 2.5 mm height command. An additional external load of 0.3 A is added at $t \ge 5$ s. (a) Comparison of the height output responses, (b) comparison of the height error responses, (c) comparison of the control responses, (d) comparison of the estimated uncertainty responses

Fig. 9a illustrates the height position response, and the error responses are shown in Fig. 9b. Fig. 9c presents the control input signals, and Fig. 9d depicts the estimated uncertainty responses. During the development of the proposed control method, the height error can be effectively reduced to within 1.1 s. The proposed DSMBC controller guarantees the asymptotic stability and exhibits better tracking capability.



Figure 9: The experimental responses of height command of 2.5 mm during $0 \le t < 5$ s. The height command changes to 2.3 mm at $t \ge 5$ s, and an additional external load of 0.3 A is added at $t \ge 10$ s. (a) Comparison of the height output responses, (b) comparison of the height error responses, (c) comparison of the control responses, (d) comparison of the estimated uncertainty responses

Tabs. 2 and 3 give the calculation results of root mean square error (RMSE). The RMSE performance index is defined as follows

	Height position tracking(mm)	
Control Methods	2.5 mm	2.5 mm to 2.3 mm
Adaptive backstepping controller	0.2153	0.2336
Dynamic sliding mode backstepping controller	0.1776	0.1778

 Table 2: Comparisons of RMSE in simulations

	Height position tracking(mm)	
Control Methods	2.5 mm	2.5 mm to 2.3 mm
Adaptive backstepping controller	0.3171	0.3204
Dynamic sliding mode backstepping controller	0.2118	0.2287

Table 3: Comparisons of RMSE in experiments

$$\text{RMSE} = \sqrt{\frac{\sum_{i=1}^{\alpha} e^2[i]}{\alpha}}$$

(36)

where α is the number of the sampled points, and e[i] is the position error.

Tabs. 2 and 3 clearly demonstrate that the DSMBC method is superior to the dynamic sliding backstepping schemes under all operational conditions because its energy control input is considered in our design. Thus, the experimental results can conclusively establish the regulation ability, dynamic tracking capability and robustness of the proposed adaptive method in a wide speed range.

5 Conclusion

The DSMBC method was successfully developed and used for vertical MBS in height tracking applications. The dynamic model of the MBS system was built by referring to the nonlinear characteristics, and the estimate functions of these nonlinear factors were proposed and applied to the equivalent control law of sliding mode control. The control system was designed, using the backstepping algorithm, and the stability of the MBS system was analyzed. Based on the Lyapunov theorem, the adaptive control law can be obtained and utilized for height position control application. The proposed DSMBC method achieves better tracking capability in real-time compensation and robustness tracking, and is not affected by height command and load disturbance. Two height trajectories are simulated and experimented to illustrate the robustness of the proposed system. Compared with the conventional adaptive backstepping method, the proposed DSMBC control system demonstrates more accurate performance, showing 20.70% improvement of RMSE in simulations and 29.94% improvement of RMSE in experiments. In the future, our goal is to establish a microcontroller or DSP platform, so that the proposed DSMBC method can be better implemented and widely used in industrial applications.

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