## ARTICLE

# Analysis of Friction and Heat Transfer Characteristics of Tubes with Trapezoidal Cut Twisted Tape Inserts 

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#### Abstract

The thermo-hydraulic properties of circular tubes with a twisted tape inside (used accordingly to induce turbulence and enhance heat transfer through the tube wall) are described for Reynolds Numbers ranging from 830 to 1990. Tapes twisted with the three distinct twist ratios are considered, namely, 6, 4.4 and 3. Air is used as the working fluid in several tests. For the sake of comparison, the standard tube with no insert is also examined. It is shown that in the presence of the twisted tape, the 'frictional factor', 'Nusselt Number' and the 'thermal performance factor' are much higher than those obtained for the plain tube. Moreover, the tapes having the lowest twist ratio, i.e., 3 , are more effective than the others in terms of heat transfer augmentation. The 'thermal performance factor' is greater than one for all the twisted tapes used in the experiments, which confirms the enhanced performances of the heat exchanger and the related savings in terms of total energy.


## KEYWORDS

Friction factor; nusselt number; performance ratio; trapezoidal cut twisted tape insert

## Nomenclature

| Nu | Nusselt number |
| :--- | :--- |
| Re | Reynolds number |
| Pr | Prandtl number |
| f | Friction factor |
| $\mathrm{Nu}_{\mathrm{p}}$ | Nusselt number of plane tube |
| $\mathrm{f}_{\mathrm{p}}$ | Friction factor of plane tube |
| d | Diameter of the tube in mm (Internal) |
| L | Length of the tube in mm |
| $\eta$ | Performance ratio |

## 1 Introduction

The process of exchange of heat is widely used in engineering and in the industry. A heat exchanger is difficult to design as it requires a precise study of pressure drop, along with the rate of heat transfer estimates
and cost and performance considerations [1]. A successful heat exchanger will have a small body while achieving a high rate of heat transfer with low pumping power [2]. With the increasing price of materials and power it is imperative that an efficient heat exchange should be developed [3]. Additionally, heat exchanger reduction is sometimes required in specialized applications, such as space applications, where heat transmission must be enhanced. Advances in technology and specialized applications need more accurate and efficient equipment to produce accurate and useful results. For example the OTEC facility (Ocean Thermal Energy Conversion) requires a heat exchanger with the surface area of heat transfer of $10,000 \mathrm{sq} . \mathrm{m} / \mathrm{MW}$ [4]. The wear and tear of the heat exchanger results in fouling or scaling, which further increases the barrier to heat transmission [5]. Similar problems are encountered when heat exchangers are used in other sectors for different applications. Some application require heat exchangers to work with oil and gases, which are known to be poor fluids of thermal conductivity, some are even employed at desalination facilities [6]. One of the approaches for increasing the rate of heat transfer is to generate disturbance on the flow of the fluid (boundary layers of thermal and breaking of the viscosity). The desired effect is accompanied with an increase in pumping power and hence it increases cost [7]. As a result, in recent years, while utilizing the power of pumping, in the existing heat exchanger; several new methods for achieving the desired rate of transferring of heat are devised.

Out of many like these, the passive enhancement of heat transfer techniques is becoming popular. It is utilized widely to increase the performance of a wide range of heat carrying equipment. The method to bring this about is by fully utilizing some inserts, which are in the passage in which the fluid flows, thereby inducing turbulence flow which improves the convective rate of transferring heat [8]. These passive enhancement methods are more advantageous than active transfer enhancement methods. The added advantage is that they may be used directly in heat exchanger with or without extra pumping power. Several types of research on the passive transfer of heat improvement methods are published in the current decade. For the improvement of the performance of the circular thermal tube, researchers $[7,8]$ have employed circularly perforated rings and solid hollow circular discs. Using numerous tapes that are twisted and inserts with solid rings, some [9] studied the heat transfer enhancement experimentally. The 'Thermal Enhancement Factor' (TEF) was seen between 1.46 and 1.61 .

The transfer of heat occurs in the flow of the laminar domain in a variety of applications of engineering and because of the transfer of heat coefficients which are often lower, the augmentations methods of the passive transfer of the heat are usually used [10]. Several devices employ a way of increasing the fluid's residence time staying in the system by creating the motion that is swirling and thus the improvement of the coefficient while there is a transfer of heat, the consequences related to the rise of the pressure drop [11]. Erfanian Nakhchi et al. [12] investigated the effects of the intensity of the holes on the velocity and temperature contours and found that the thermal performance is highly considered with the perforated turbulators than with the VRW inserts and it also augments the mixing of the fluid and transfers the heat from the pipe walls to the core of the tube due to the flow generated by the PVRW. By reducing the DR from 0.4 to 0.13 the enhancement of heat transfer occurs by $25.2 \%$ and also for the heat exchangers with vortex generators with $\mathrm{N}=14$ and $\mathrm{DR}=0.26$, the highest $\eta=2.25$ (thermal efficiency) obtained at $\mathrm{Re}=$ 5000. The output of rotated inclined elliptical (RIE) inserts on heat exchanger pipes for heat transfer and the thermal performance factor of double-pipe were investigated [13]. RIE turbulators improve heat transfer by up to 30.7 percent when compared to non-rotated elliptic (NRIE) turbulators, and for the RIE turbulators with $\beta=90, \mathrm{~d}_{\mathrm{p}} / \mathrm{b}=0.250$, and $\alpha=25^{\circ}$ the highest thermal performance factor of 2.23 was achieved. When NRIE vortex generators with $\mathrm{d}_{\mathrm{p}}=1.5 \mathrm{~mm}$ are used, the heat transfer coefficient is improved by 59.95 percent when compared to typical non-rotated louvered strips. It was discovered that using DPIE turbulators increased the Nusselt number by 217.4 percent when compared to the tube without vortex generators. The maximum thermal efficiency parameter of 1.849 was obtained for the DPIE vortex generators with $\mathrm{d} / \mathrm{b}=0.25$ and $\alpha=25$. A 14.0 percent increase in friction factor was also
observed for the DPIE insert with $\mathrm{d} / \mathrm{b}(0.25)$, and the heat transfer increased by 39.4 percent for the DPIE insert with $\mathrm{d} / \mathrm{b}(0.25)$ [14]. The separation of the thermal boundary layer is the primary cause of heat transfer enhancement [15].

## 2 Tape Inserts

Apart from the insert designs, the thermo-hydraulic behavior of an insert is mostly determined by the conditions of the flow (turbulent or laminar). The following are the main findings of all researchers in connection to various inserts and flow [16].

### 2.1 Tape Twisted in the Laminar Flow

The laminar flow of the thermal resistance is not restricted to any tiny region, the tape that is twisted mixes and efficiently inserts in the bulk flow and performs better in the laminar flow than the other inserts. Twisted tape performance, on the other hand, is influenced by fluid characteristics such as the 'Prandtl number'. If the 'Prandtl number' is large, such as $\operatorname{Pr}=30$, the twisted tape will not perform whereas the other inserts such as the coil of a wire increases in terms of thermo-hydraulic performance. Short-length tape that is twisted outperforms twisted tape which is full length in terms of continuous pumping power. Twisted tape can be utilized successfully to increase heat transfer by the construction of the laminar flow of the heat exchanger [17].

### 2.2 Tape Twisted in the Turbulent Flow

Inside the turbulent flow, the twisted tape effectively upgrades to the particular range of the Reynolds number, but not beyond that. The tape that is twisted is ineffective in turbulent flow as compared to the wire coil as it causes a high-pressure drop and it stops the flow. As a result, in turbulent flow, the twisted tape has a 'thermo-hydraulic performance' that is inferior to that of a wire coil. As a result, it can be stated that the coil of the wire is a favorable option in the turbulent flow for compact heat exchanger construction. The turbulent flow, which has a short length of tape that is twisted, produces good behavior of thermo-hydraulic performance when it is compared to a twisted tape that has the full length [18].

### 2.3 Laminar Flow in the Wire Coil

The transmission heat rate of the coil in the wire, in the laminar flow is considerably increased. The performance, however, is determined by the 'Prandtl number'. If the 'Prandtl number' is large, the performance coil in the wire is favorable because the thick layer of the thermal boundary is modest as compared to the boundary layer of hydrodynamic for a high Prandtl number, and the coil readily breaks this thick boundary layer. As a result, both the pressure and the heat transmission decrease are significant [19].

### 2.4 Turbulent Flow in the Wire Coil

The wire coil in the turbulent flow has effectively improved the transmission of heat. The turbulent flow performs better than the laminar flow. The wire coil outperforms twisted tape in the turbulent flow, in terms of thermo-hydraulic performance [20].

### 2.5 Other Passive Methods

Other than the tape that is twisted and the coil of the wire, passive techniques such as the fins, dimples, and ribs can be used to improve heat transmission in a flow. In turbulent flow, these approaches are typically more effective than in laminar flow.

In heat exchangers, inserts play an essential function as turbulence promoters. In a heat exchanger, there are a variety of ways for producing turbulence in the flow. A large number of studies have been conducted by several researchers that are creating the turbulence inside the flow field of a heat exchanger. Heat exchangers
are also more compact with inserts. The following are some examples of twisted tapes: 1. Tapes with twist ratio 2. Perforated Tapes 3. Cut Tapes 4. Double twist tapes 5. Dimple tapes 6. Coupling 7. V-cut tapes 8. Vfinned 9. Tapered 10. Clockwise twisted 11. Non-Uniform tapes 12. Continuous spaced 13. Trapezoidal 14. Quadruple cut 15 . U cut 16. Multiple quadruple 17. Double v-ribbed 18. Perforated and helical, etc. The description of a few tapes along with the Reynolds range is given in Table 1 below [6,21-23].

Table 1: Various types of tapes and their Reynolds number range [6,21-23]

| Type of tape | Range of Re | Figure |
| :--- | :--- | :--- |
| Perforated | $5000-20000$ |  |
| Alternate clockwise and counter clockwise | $830-1900$ |  |
| Trapezoidal cut | $2000-12000$ |  |
| Trapezoidal cut plain | $2000-12000$ |  |
|  |  |  |

## 3 Set-Up of the Experiment



|  | 1. HOT AIR METER | 8. SWITCHES | 15. COLD AIR CONTROL VALVE | 22. HOT AIR TANK |
| :---: | :---: | :---: | :---: | :---: |
|  | 2. HOT AIR METER | 9. AMMETER | 16. COLD WATER BYPASS VALVE | 23. HOT AIR PUMP |
| - hot Air line | 3. COLD AIR METER | 10. VOLTMETER | 17. COLD AIR SUMP |  |
| - COLD AIR LINE | 4. TEMP. INDICATOR | 11. RTD HOT AIR IN | 18. COLD AIR PUMP |  |
|  | 5. TEMP. CONTROLLER | 12. RTD COLD AIR OUT | 19. HOT AIR CONTROL VALVE |  |
|  | 6. HEAT INDICATOR | 13. RTD COLD AIR IN | 20. HOT AIR BYPASS VALVE |  |
|  | 7. U TUBE METER | 14. RTD HOT AIR OUT | 21. HEATER |  |

Figure 1: Setup of the experiment

Two concentric tubes are placed one within the other in this setup as shown in Fig. 2. The tube made of copper with an internal diameter of 28.5 mm and a length of 2000 mm allows hot air to travel through the tube while cold air flows in the opposite direction through the annulus. The experimental setup includes two rota-meters for measuring cold and hot air flow rates, as well as temperature readings at the input and exit. As shown in Fig. 1, 04 temperature sensors ( 02 on each side) detect the temperature of hot air at the inlet and outlet, whereas 02 ( 01 on each side) measures the temperature of cold air at the inlet and outflow. As the conditions of steady-state are attained in the case of the plain tube, a $U$ tube manometer detects the reduction in pressure, while RTDs (Resistance Temperature Detector) measure the temperatures of hot and cold air at the intake and exit.


Figure 2: Dimensions of pipe
The tests were carried out using twisted tapes displayed in Fig. 3 with twist ratios of 3, 4.4, and 6 ( $\mathrm{y}=54$, 79.2 and 108 mm , and $\mathrm{w}=18 \mathrm{~mm}$ ), with Reynolds numbers ranging from 830 to 1990, and air as the working fluid. For the laminar regime, the reference 'Nusselt number $\left(N u_{p}\right)$ ' and 'friction factor ( $\mathrm{f}_{\mathrm{p}}$ )' taken are ' $\mathrm{Nu}_{\mathrm{p}}=48 / 11$ and $\mathrm{f}_{\mathrm{p}}=64 / \mathrm{Re}^{\prime}$, respectively. Eqs. (1)-(3) [24] are used to determine Nu , f , and $\eta$ with a twisted tape insert.

$$
\begin{align*}
& N u=0.005 \operatorname{Re}^{1.139} \mathrm{Pr}^{0.4}(y / w)^{-0.521}  \tag{1}\\
& f=6.559 \mathrm{Re}^{-0.303}(y / w)^{-0.674}  \tag{2}\\
& \eta=0.005 R e^{0.907}(y / w)^{-0.296} \tag{3}
\end{align*}
$$



Figure 3: (a) Twisted tape insert (b) Dimensions of the trapezoidal-section

## 4 Results and Discussion

### 4.1 Effect of an Insert on Heat Transfer

Nusselt Number $(\mathrm{Nu})$ is defined as the ratio of convective heat transfer to the conductive heat transfer in a fluid subjected to boundary conditions. From Table 2, we notice that the value of 'Nusselt number (Nu)' appears to grow significantly as Reynolds Number rises, indicating an increase in convective heat transfer.

Nusselt number rises as Reynolds number rises across the range studied (laminar regime). It is also discovered that greater $\mathrm{y} / \mathrm{w}$ ratios are associated with lower Nu levels, as shown in Fig. 4.

Table 2: Nusselt number ( Nu ) as a function of Reynold's number

| Re | Plain tube | Nu for $(\mathrm{y} / \mathrm{w})=3$ | Nu for $(\mathrm{y} / \mathrm{w})=4.4$ | Nu for $(\mathrm{y} / \mathrm{w})=6$ |
| :--- | :--- | :--- | :--- | :--- |
| 800 | 4.36 | 8.8686 | 7.26439 | 6.180466 |
| 900 | 4.36 | 10.1419 | 8.307338 | 7.067795 |
| 1000 | 4.36 | 11.435 | 9.36655 | 7.968961 |
| 1100 | 4.36 | 12.7463 | 10.44061 | 8.882761 |
| 1200 | 4.36 | 14.0742 | 11.52835 | 9.808196 |
| 1300 | 4.36 | 15.4177 | 12.62877 | 10.74443 |
| 1400 | 4.36 | 16.7756 | 13.74104 | 11.69073 |
| 1500 | 4.36 | 18.147 | 14.86441 | 12.64648 |
| 1600 | 4.36 | 19.5313 | 15.99824 | 13.61114 |
| 1700 | 4.36 | 20.9276 | 17.14198 | 14.58421 |
| 1800 | 4.36 | 22.3353 | 18.29511 | 15.56529 |
| 1900 | 4.36 | 23.7541 | 19.45719 | 16.55397 |
| 2000 | 4.36 | 25.1832 | 20.6278 | 17.54991 |



Figure 4: Validation of Nusselt number vs. Reynolds number for plain tube with an insert
Fig. 4 also indicates that the Nusselt Number for an insert is greater than the plain tube, because insert causes the flow to spiral along the tube length and disturbs the entire flow which tends to increase the rate of heat transfer. Also, it was deduced that a higher rate of heat transfer given by the lower twist ratio than the higher twist ratio was because of the intensity of turbulence and the length of flow obtained which were higher for the lower twist ratio than the higher twist ratio.

The 'Nusselt number ratio $\left(\mathrm{Nu} / \mathrm{Nu}_{\mathrm{p}}\right)$ ' increases with the increase in 'Reynolds Number', as illustrated in Fig. 5, across the range examined (laminar regime) and the values are tabulated in Table 3 for the different twist ratio.

Table 3: Nusselt number ratio $\left(\mathrm{Nu} / \mathrm{Nu}_{\mathrm{p}}\right)$ as a function of Reynold's number

| Re | Nu/Nup for $(\mathrm{y} / \mathrm{w})=3$ | $\mathrm{Nu} / \mathrm{Nup}$ for $(\mathrm{y} / \mathrm{w})=4.4$ | $\mathrm{Nu} /$ Nup for $(\mathrm{y} / \mathrm{w})=6$ |
| :--- | :--- | :--- | :--- |
| 800 | 2.034083 | 1.666145 | 1.417538 |
| 900 | 2.326124 | 1.905353 | 1.621054 |
| 1000 | 2.622706 | 2.148291 | 1.827743 |
| 1100 | 2.923463 | 2.394636 | 2.037331 |
| 1200 | 3.228028 | 2.644117 | 2.249586 |
| 1300 | 3.536170 | 2.896508 | 2.464318 |
| 1400 | 3.847615 | 3.151614 | 2.68136 |
| 1500 | 4.162156 | 3.409268 | 2.900569 |
| 1600 | 4.479656 | 3.669322 | 3.12182 |
| 1700 | 4.799908 | 3.931647 | 3.345003 |
| 1800 | 5.122775 | 4.196126 | 3.57002 |
| 1900 | 5.448188 | 4.462657 | 3.796781 |
| 2000 | 5.775963 | 4.731146 | 4.025209 |



Figure 5: Variation of $\mathrm{Nu} / \mathrm{Nu}_{\mathrm{p}}$ with Re

### 4.2 Effect of an Insert on Friction Factor

The friction factor is defined as a function of Reynold's number and relative roughness. There is the change of friction factor with the 'Reynolds Number' for the tube with tape insert as shown in Fig. 6. From Table 4 it can be seen that the friction factors of the tube with $y / w=3$ appears to be higher than the one of a simple tube.


Figure 6: Validation of friction factor vs. Reynolds number for plain tube with an insert
Table 4: Friction factor (f) as a function of Re

| Re | Plain tube | f for $(\mathrm{y} / \mathrm{w})=3$ | f for $(\mathrm{y} / \mathrm{w})=4.4$ | f for $(\mathrm{y} / \mathrm{w})=6$ |
| :--- | :--- | :--- | :--- | :--- |
| 800 | 0.085 | 0.4126 | 0.3183596 | 0.258304 |
| 900 | 0.075556 | 0.3982 | 0.3071982 | 0.249248 |
| 1000 | 0.068 | 0.3857 | 0.2975461 | 0.241417 |
| 1100 | 0.061818 | 0.3747 | 0.2890761 | 0.234545 |
| 1200 | 0.056667 | 0.3649 | 0.2815544 | 0.228442 |
| 1300 | 0.052308 | 0.3562 | 0.274808 | 0.222968 |
| 1400 | 0.048571 | 0.3483 | 0.268706 | 0.218017 |
| 1500 | 0.045333 | 0.3411 | 0.2631471 | 0.213507 |
| 1600 | 0.0425 | 0.3345 | 0.2580512 | 0.209372 |
| 1700 | 0.04 | 0.3284 | 0.2533542 | 0.205561 |
| 1800 | 0.037778 | 0.3227 | 0.2490042 | 0.202032 |
| 1900 | 0.035789 | 0.3175 | 0.2449581 | 0.198749 |
| 2000 | 0.034 | 0.3126 | 0.2411805 | 0.195684 |

Fig. 6 also depicts the decrease of friction factor with an increase in Reynold's Number. For every insert, the friction factor is higher than that found in the plain tube. For the lowest twist ratio; it tends to get higher friction factor as there is decrease in twist ratio, with an increase in swirl flow which thus provides the maximum tangential contact between the tube wall surface and secondary flow.

As demonstrated in Fig. 7, the "friction factor ratio ( $\mathrm{f} / \mathrm{f}_{\mathrm{p}}$ )" increases with the "Reynolds number". We tabulated the friction factor ratio for the different twist ratio in Table 5.


Figure 7: Variation of f/fp with Re
Table 5: Friction factor ratio $\left(\mathrm{f} / \mathrm{f}_{\mathrm{p}}\right)$ as a function of Re

| $\operatorname{Re}$ | $\mathrm{f} / \mathrm{fp}$ for $(\mathrm{y} / \mathrm{w})=3$ | $\mathrm{f} / \mathrm{fp}$ for $(\mathrm{y} / \mathrm{w})=4.4$ | $\mathrm{f} / \mathrm{fp}$ for $(\mathrm{y} / \mathrm{w})=6$ |
| :--- | :--- | :--- | :--- |
| 800 | 4.854118 | 3.745407 | 3.0388703 |
| 900 | 5.270263 | 4.065859 | 3.2988721 |
| 1000 | 5.672059 | 4.375677 | 3.550246 |
| 1100 | 6.061341 | 4.676231 | 3.7941033 |
| 1200 | 6.439374 | 4.968607 | 4.0313246 |
| 1300 | 6.809666 | 5.253682 | 4.2626234 |
| 1400 | 7.170946 | 5.532183 | 4.4885874 |
| 1500 | 7.524320 | 5.804715 | 4.7097088 |
| 1600 | 7.870588 | 6.071792 | 4.9264045 |
| 1700 | 8.210000 | 6.333856 | 5.1390322 |
| 1800 | 8.542009 | 6.591287 | 5.3479013 |
| 1900 | 8.871441 | 6.844418 | 5.5532817 |
| 2000 | 9.194118 | 7.093543 | 5.7554111 |

### 4.3 Analysis of the Performance of Heat Exchanger

The thermal performance/enhancement factor is defined as the ratio of the heat transfer coefficient of an augmented surface to that of a smooth surface. The final criteria for evaluating the practical usage of twisted tapes is the thermal performance factor $(\eta)$. Fig. 8 depicts the change in the performance factor of thermal with the 'Reynolds number' of the tubes with the twist ratios $3,4.4$, and 6 falling under the variation of 1.5518-3.5626, 1.385513-3.180843 and 1.263979-2.9018265 for an insert observed in Table 6 and it indicates that performance ratio for all the cases are higher than one (unity), it means that the use of enhancement is valuable towards the point of saving of total energy.


Figure 8: $\eta \mathrm{V} / \mathrm{s}$ Re for tape with an insert of twist ratios 3, 4.4, and 6
Table 6: Thermal performance factor $(\eta)$ as a function of $\operatorname{Re}$

| Re | $\eta$ for $(\mathrm{y} / \mathrm{w})=3$ | $\eta$ for $(\mathrm{y} / \mathrm{w})=4.4$ | $\eta$ for $(\mathrm{y} / \mathrm{w})=6$ |
| :--- | :--- | :--- | :--- |
| 800 | 1.5518 | 1.385513 | 1.263979 |
| 900 | 1.7268 | 1.541722 | 1.4064853 |
| 1000 | 1.8999 | 1.696321 | 1.5475234 |
| 1100 | 2.0715 | 1.849487 | 1.6872537 |
| 1200 | 2.2416 | 2.001361 | 1.825806 |
| 1300 | 2.4103 | 2.152061 | 1.9632873 |
| 1400 | 2.5778 | 2.301686 | 2.0997876 |
| 1500 | 2.7444 | 2.45032 | 2.2353833 |
| 1600 | 2.9099 | 2.598034 | 2.3701403 |
| 1700 | 3.0743 | 2.744892 | 2.5041158 |
| 1800 | 3.2379 | 2.890947 | 2.6373599 |
| 1900 | 3.4005 | 3.03625 | 2.769917 |
| 2000 | 3.5626 | 3.180843 | 2.9018265 |

## 5 Conclusion

In the laminar flow regime, the effects of twisted tape on 'heat transfer (Nu)', 'friction factor (f)' and 'thermal performance $(\eta)$ ' are discussed. The following are the key findings:

1. The Nusselt number $(\mathrm{Nu})$ associated with the tape insert is substantially greater than that associated with the normal tube under comparable conditions- $(\mathrm{y} / \mathrm{w}=3)$ gives a greater $N u$ than $(\mathrm{y} / \mathrm{w}=6)$ in the range studied.
2. Twisted tapes provide a significantly higher thermal efficiency factor, which improves as the twist ratio decreases. For the insert, the heat transfer rate for the twist ratios 3, 4.4, and 6 are higher than the plain tube without the insert. It means that the intensification is valuable for energy saving.
3. The friction factor produced by a tape insert is larger than that induced by a plain tube, and it rises as the twist ratio decreases.

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