

Optimized Gated Recurrent Unit for Mid-Term Electricity Price Forecasting

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Abstract: Electricity price forecasting (EPF) is important for energy system operations and management which include strategic bidding, generation scheduling, optimum storage reserves scheduling and systems analysis. Moreover, accurate EPF is crucial for the purpose of bidding strategies and minimizing the risk for market participants in the competitive electricity market. Nevertheless, accurate time-series prediction of electricity price is very challenging due to complex nonlinearity in the trend of electricity price. This work proposes a mid-term forecasting model based on the demand and price data, renewable and non-renewable energy supplies, the seasonality and peak and off-peak hours of working and non-working days. An optimized Gated Recurrent Unit (GRU) which incorporates Bagged Regression Tree (BTE) is developed in the Recurrent Neural Network (RNN) architecture for the mid-term EPF. Tanh layer is employed to optimize the hyperparameters of the heterogeneous GRU with the aim to improve the model's performance, error reduction and predict the spikes. In this work, the proposed framework is assessed using electricity market data of five major economical states in Australia by using electricity market data from August 2020 to May 2021. The results showed significant improvement when adopting the proposed prediction framework compared to previous works in forecasting the electricity price.

Keywords: Deep learning; energy management; machine learning; prediction

1 Introduction

The forecast of electricity price projection is an important element of expectations for policy makers, governments, and financial market participants. Electricity price forecasting (EPF) has become an important information to manage the deregulated electricity market, complex renewable energy and emission policy objectives. This is because, accurate and consistent price forecasting will minimize risk, maximize profit for the day-to-day market, improve bidding and production measures [1]. In several countries, deregulations of the electricity sector have been developed to enhance congestion control, facilitate renewable energy, and maximize the resource allocation of the power system. In addition, EPF provides vital information to all stakeholders in the power sector marketplace since the accuracy of EPF



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influenced the performance and rational analysis of energy resource optimization. Besides, accurate EPF can improve wholesale electricity price bidding strategy and production which can increase the profits in day-ahead trading and energy management. Usually, power portfolio managers are interested with short-term and mid-term price forecasts. The short-term forecasts (intra-day) are the key elements in day-to-day market operations, especially for bidding at a power exchange or for executing effective demand response. Meanwhile, the mid-term forecasting which can range from several weeks to several months ahead are used for planning purposes such as the tuning of mid-term plans and resources allocation, risk management and the valuation of exchange traded futures and bilateral contracts. This is due to high saturation of intermittent technologies and the evolving concerns related to resource adequacy in the longer-term. These forecasting operations will affect the baseload electricity price, such as the peakload price, the average price for the 24 h of the day or the baseload price [2].

In general, time series forecasting is analyzing time series data via modelling and statistics approach to aid strategic decision-making process. Time series forecasting incorporates information related to historical values and associated patterns to foresee future activity [3,4]. Nowadays, researchers are capable of employing and extracting complex information from time series data to solve various problems such as wind speed prediction [4], stock market prediction [3,5–7], and forecasting electricity prices [8,9]. Time series models have been widely used to forecast electricity prices, although they can be challenging due to large variations [10–19]. Existing statistical techniques tried to reveal the specific pattern of historic power price utilizing curve fitting. For instance, German electricity market has tested a k-factor Guégan Introduced Generalized Autoregressive Conditionally Heteroskedastic (GIGARCH) for forecasting electricity price [10,11]. An iterative neural network methodology is also adopted along with this combinatorial neural network-based prediction technique to forecast upcoming electricity price. The advantages of this method include good precision, model functionality, and reliability. Meanwhile, Autoregressive Integrated Moving Average (ARIMA) was proposed for electricity and power load forecasting [13,14,16,18]. However, application of statistical models had shown to be challenging when predicting multi-dimensional nonlinear price of electricity since they are mainly based on linear equations. Moreover, statistical methods are inadequate for solving nonlinear multi-dimensional data for prediction purpose, as its more suitable in handling linear data [20].

In time series analysis, machine learning models have shown to perform better than statistical methods. Support Vector Machine (SVM) was adopted in [17,20,21] for load and electricity forecasting. The other common machine learning models applied in EPF are support vector regression (SVR) [22–24] and artificial neural network (ANN) [19,25,26]. Hybrid models of ANN are used to predict electricity load and price such as adaptive network-based fuzzy inference system (ANFIS) and Backtracking Search algorithm (BSA) [27]. However, the abovementioned conventional machine learning models are inadequate for complex and nonlinear problems. Recurrent neural network (RNN) which is a deep learning technique with a recurrent feedback network has shown to perform better when dealing with time series data compared to conventional machine learning algorithm [28]. The work in [18] proposed a Deep Belief Network (DBN) for electricity price forecasting. On the other hand, the work in [15], proposed LSTM network for electricity price forecasting. Nevertheless, the performance of the proposed models from previous methods can still be improved to achieve more accurate results when dealing with complex and nonlinear electricity market fluctuations.

Therefore, this paper proposes an optimized GRU consisting of RNN with Bagged Regression Tree forecasting model for electricity price prediction. The bagged trees regression is applied to predict nonlinear data which is further optimized by using GRU RNN network. Then the tanh layer is utilized to optimize the hyperparameters of the heterogeneous GRU to improve the model's performance, error reduction and predict the spikes. Contributions of this study include:

- Improvement of the prediction performance by tuning the nonlinear degree of the feature effects of demand, seasons, fuel supply, renewable and non-renewable energy, peak and off-peak hours of forecasting,
- Integration of Bagged Trees and GRU in RNN to handle complex nonlinear features of electricity price.
- Prediction of the unusual price spikes by adopting GRU and Tanh function layers which optimize the hyper parameters of deep neural networks.

This paper is structured as follows. Section 2 explains the proposed methodology; Section 3 presents the results and discussions. Finally, Section 4 provides the conclusion of this work.

2 Methodology

This work proposed a forecasting framework for mid-term EPF for five states in Australia which includes pre-processing module, Bagged Trees Ensemble (BTE) algorithm, Recurrent Neural Network (RNN) and Gated Recurrent Unit (GRU). The electricity market dataset is divided into three components: training set, validation set and test set. The workflow of the proposed framework is shown in Fig. 1.

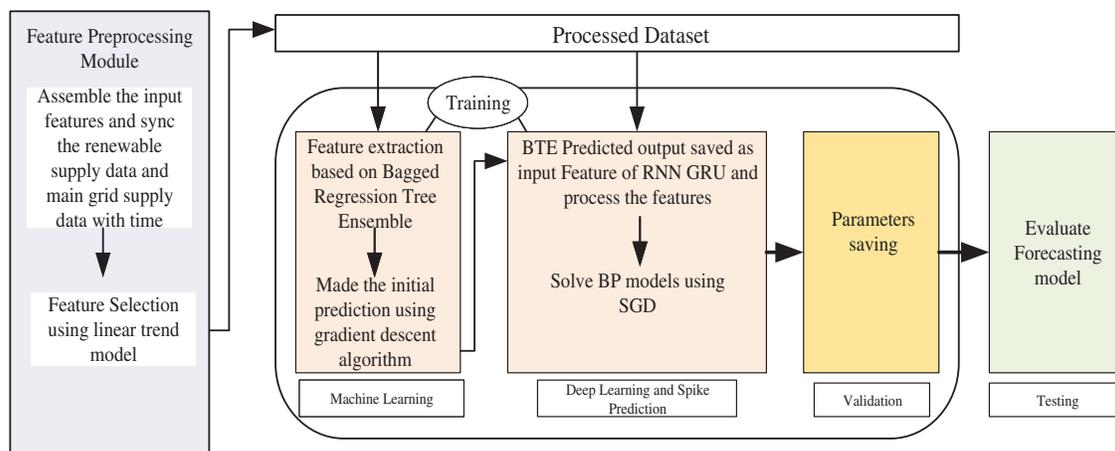


Figure 1: Flow diagram of the proposed framework

2.1 Pre-Processing Module

The proposed forecasting model is developed based on information of the demand and price data in megawatts (MW) and Australian dollar (AUD) from five states in Australia (NSW, QLD, SA, TAS, VIC). Furthermore, we considered renewable and non-renewable energy supplies data in megawatts (MW) which substantially impact pricing electricity. Besides that, the seasonality and peak and off-peak hours of working and non-working days were also considered. Data clusters are usually formed by the input features may present when accumulating unprocessed data due to high dimensions, outliers, and missing values, which contributes to instability in the forecasting performance [29]. Therefore, data clusters need to be pre-processed to aid the prediction process. Hence, in this work, a linear trend model is applied to identify effective pattern of features for the prediction process. Example of dataset adopted in this work is tabulated in Tab. 1.

Table 1: The input features dataset for the proposed model

Peak/off-peak hours	Time (Hour)	Main electricity supply (MWH)	Previous hour price (AUD)	Solar power supply (MWH)	Hydro power Supply (MWH)	Wind power supply (MWH)
1	5	7360.25	40.54	0	992	215.06
1	6	7066.01	43.59	0	992	192.84
1	7	6841.68	34.74	0	645.09	168.44
1	8	6732.33	17.15	0	325.58	146.70
1	9	6980.24	16.61	0	214.92	136.46
0	10	7661.34	31.56	0	125	186.70
0	11	8639.57	40.02	0	60	179.90
0	12	9890.74	49.99	0	2.5	810.19
0	13	9845.55	50.25	0	20	776.65
0	14	9446.45	54.32	0	94.58	819.08
0	15	8992.55	55.51	9.76	380.62	825.95
0	16	8547.70	47.99	189.73	705.43	760.85
0	17	8162.07	39.65	418.42	478.88	746.72

The linear trend method acts with the trend precisely and show the trend without any assumption. The input dataset used in this work are the residual seasonality, peak and off-peak hour and renewable energy trend in time series dataset. Let $p_1 = t_1$ and $q_1 = 0$. The equations for the feature processing are described in Eqs. (1)–(7). Where p_i is the approximation level of the series at time t , q_i is the estimation of the trend (slope) of the series at time t , α is the smoothing parameter of the level $0 < \alpha \leq 1$ and β is the smoothing parameter of the level $0 \leq \beta \leq 1$. i denotes the seasonality and t is the hour of observation.

$$p_i = \alpha t_i + (1 - \alpha)(p_{i-1} + q_{i-1}) \quad (1)$$

$$q_i = \beta(p_i - p_{i-1}) + (1 - \beta)q_{i-1} \quad (2)$$

$$\hat{t}_{i+1} = p_i + q_i \quad (3)$$

Let $p_1 = t_1$ and $q_1 = 0$. An alternative form of these equations are;

$$p_i = p_{i-1} + q_{i-1} + \alpha e_i \quad (4)$$

$$q_i = q_{i-1} + \alpha \beta e_i \quad (5)$$

$$t_{i+1} = p_i + q_i \quad (6)$$

where,

$$e_i = t_i - (p_{i-1} + q_{i-1}) = t_i - \hat{t}_{i-1} \quad (7)$$

Note that if $\beta = 0$, then the linear model can be considered as single exponential smoothing model.

2.2 Bagged Trees Ensemble (BTE)

Bagged Trees Ensemble (BTE) algorithm is adopted to generate several bootstrap samples and trains classifiers on the new learning sets. Then, BTE algorithm computes the mean predictions for a sequential output or performs a plurality for a class outcome. Assuming the training set is defined as $A\{(p_m, q_m), m \in 1, 2, \dots, M\}$ with q_m represents either a class label or numerical response. For an p input q , could be predicted using $\hat{O}(p, A)$, where $\hat{O}(p, A)$ is a single learning set predictor. Assuming there is a series of

learning sets $\{A_R, R = 1, \dots, M\}$ each having M . number of distinct samples chosen from A . The purpose will be to utilize $\{A_R\}$ to obtain more accurate predictor than the single learning set predictor $\mathcal{O}(p, A)$. Replacing $\mathcal{O}(p, A)$ with the average of $\mathcal{O}(p, A_R)$ over R . for a numerical value of q , i.e., $\mathcal{O}_D(p) = E_A \mathcal{O}(p, A)$ is an apparent method of performing the task. The subscript D in \mathcal{O}_D signifies aggregation, and E_A represents the anticipation over A in that equation. Most of the time we have one learning set, however, bootstrap samples can be created from A (A^C) which might be used to replicate a similar procedure leading to \mathcal{O}_D . with replacement, such that $\mathcal{O}_D(p) = \text{average } \mathcal{O}(p, A^C)$ [30]. This technique is called bagging and Tab. 2 pnts the bagging algorithm applied in this work.

Table 2: Bagged regression tree ensemble algorithm

Input	Training dataset = $\{(p_k, q_k), k \in 1, 2, \dots, m\}$ A base learning algorithm using regression trees (RT) and the number of learning cycles, j .	
Process	for $j = 1, \dots, J$ TD _{j} = Bootstrap (TD) with replacement.	Create bootstrapped samples from training dataset
Output	$RT_j(p, q) = GTD_j$ $q^* = \frac{1}{J} \sum_{j=1}^J RT_j(p^*, q)$	Bootstrap sample for training dataset (TD), TD _{j} ; Train regression trees (RT_j). The output of the trained base learners are averaged.

The classifiers are also defined as regression trees (decision trees). In this work, the proposed bagged tress implemented 5 folds cross-dation. Then, the number of RT (chosen N=30) and the minimal leaf size (selected $G_{\min} = 8$) are applied. Each regression tree was built using a bootstrap sample selected uniformly fromhe input data. Further, the bagging method averaged the learners’ outputs to obtain a single forecast. This technique is called bagging and Tab. 2 presents the bagging algorithm applied in this work.

2.3 Gated Recurrent Unit (GRU)

As RNN is recurrent in nature, it wos much the same way for all inputs, while the output of the input data is dependent on the previous calculations. After generating the output data, it is replicated and revert back into the recurrent network unit. RNN count the present input and the output acquired from the last input while it makes logical decision. RNNs can utilize the internal state (memory) to evaluate input variables, which is different from feedforward neural network [31,32]. In recurrent neural network, all of the inputs are connected with one another, which distinguishes it from the other neural networks.

In general, the RNN has an issue with inflating and erasing gradients [33]. The most familiar and used Recurrent Neural Network (RNN) elements are GRU and LSTM. RNNs have a reverse connectivity which has significant detrimental impact on model performance, which can’t see in CNNs, GRU deals with these difficulties. GRU is a more robust RNN framework, designed for long-range dynamic feature dependencies. Besides, a GRU architecture requires less training time, with typically competitive results to an LSTM. The input and forget gates are fused into a single update gate in GRU’s core structure [34,35]. The GRU architecture contains two gates layers: the reset (Y) and an update (Z) gate, whereas LSTM architecture includes three gates [5,15].

In this work, the input and forget gate in GRU are merged to update gate and hidden state reset gate as result it takes less time to process the data. The equations of the GRU cell adopted in this work are shown in Eqs. (8)–(12). A multi-layer GRU is adopted due to faster training process and smaller number of parameters required.

$$p_t = \sigma(W_p \cdot [g_{t-1}, x_t]) \quad (8)$$

$$q_t = \sigma(W_q \cdot [g_{t-1}, x_t]) \quad (9)$$

$$\bar{r}_t = \mathcal{O}(W_r \cdot [p_t \times g_{t-1}, x_t]) \quad (10)$$

$$r_t = (I - q_t) \times g_{t-1} + q_t \cdot \bar{r}_t \quad (11)$$

$$y_t = \sigma(W_o \cdot r_t) \quad (12)$$

where x_t , g_{t-1} , g_t , p_t , q_t , \bar{r}_t and y_t are the input vector, the state memory variable at previous moment, the state memory variable at current moment, the state of reset gate, the state of update gate, the state of the current candidate set and the output vector at current moment respectively. On the other hand, W_p , W_q , W_r , W_o are the weight matrices for the corresponding inputs of the network activation functions while I represent the identity matrix. Then, backpropagation (BP) algorithm is employed to train and adjust the system parameters of the GRU RNN, such as the weights and biases.

The activation function in the neural network is one of the important concerns in the deep training process that works out well in terms of nonlinearity in the learning process. Existing activation functions, such as ReLU [36] and Swish, are unable to use high negative input values and, as a result of zero-hard rectification, may suffer from the dying gradient problem. Therefore, finding a better activation function that doesn't have these limitations is critical. To address the issue this model uses a new nonparametric method called Hyperbolic Tangent for Neural Networks (NNs) [34]. The activation function handles the fading gradient problem by scaling the non-linear Hyperbolic Tangent (Tanh) function through a linear method. A non-parametric hyperbolic tangent activation layer like ReLU, and Swish, the similar unrestricted upper limits property on the right-hand side of the activation curve is shared by Tanh. where $g(x)$ is a hyperbolic tangent function and defined as the Eq. (13).

$$g(x) = \text{Tanh}(x) = \frac{\exp^x - \exp^{-x}}{\exp^x + \exp^{-x}} \quad (13)$$

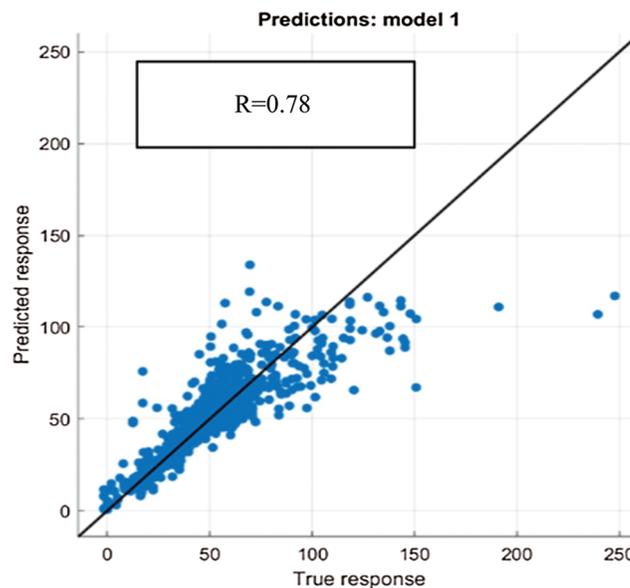
3 Results and Discussions

In this work, electricity demand and price data were obtained from Australian Energy Market Operator (AEMO) from August 2020 to May 2021 to develop the proposed mid-term EPF framework. Test dataset includes the hourly data from January 2021 to May 2021. In the meantime, the training dataset is arranged accordingly where 60% of the data is used as training while the rest 40% is used as validation dataset. The training dataset includes 5 prior months to the forecasting weeks. This work proposed two types of forecasting: 1-week forecasting and 2 weeks forecasting. Tab. 3 briefly shows the sample arrangement of training dataset to forecast electricity price for the month of January and February. The arrangement is modified accordingly to forecast the months of March, April and May 2021.

Table 3: Examples of training data arrangement for the EPF

Training dataset	Testing dataset	
5 months data	1 week forecasting	2 weeks forecasting
Week 1, Aug 2020–Week 4, Dec 2020	Week 1, Jan 2021	Week 1–2, Jan 2021
Week 3, Aug 2020–Week 2, Jan 2021	Week 3, Jan 2021	Week 3–4, Jan 2021

It is argued that the data points used for developing the forecasting model should be strongly correlated with each other. Hence, the correlation coefficient R of the actual and predicted output of the model is computed to assess the feasibility of implementing BTE model. The purpose of analyzing regression model is to extract significant relationships between the forecast variable of interest and the predictor variables. A perfect forecasting modelling will produce a correlation coefficient R value of 1. Figs. 2–6 showed a regression value, R of 0.78, 0.80, 0.88, 0.76, and 0.87 for Australia's five economic states (NSW, QLD, SA, TAS, VIC) respectively when applying BTE model. As can be seen, the regression value obtained when implementing conventional BTE model is in the range between 0.76 to 0.87 which is inadequate in forecasting complex time series data. Hence, in order to improve the accuracy of the forecasting model, the data was further transferred to RNN model and this work proposed to incorporate GRU in the RNN architecture for further optimization.

**Figure 2:** NSW BTE testing model

The two weeks forecasting results are compared in Fig. 7. After applying the proposed BTE and GRU model, the correlation coefficient of R for NSW, QLD, SA, TAS, VIC has improved significantly to 0.9961, 0.9995, 0.9800, 0.9996, 0.9996 respectively (Tab. 4). This shows that the proposed forecasting model achieved a correlation coefficient, R approximately 1 which means that the proposed forecasting model manage to correlate the data points better as compared to BTE model in Figs. 2–6. Thus, high value of R contributed to better performance in mean absolute percentage error (MAPE) and root mean square error (RMSE). In this work, the accuracy of the proposed point forecasting model is evaluated by computing the MAPE and RMSE. RMSE evaluates the forecasting precision and the ability of the point prediction

results while MAPE conveys the absolute average forecasting deviation of trains and targets. As can be seen from Fig. 7, the proposed BTE+GRU produced the smallest value of RMSE and MAPE values compared to other methods such as BiLSTM, LSTM+GRU, and LSTM for all the five states, NSW, QLD, SA, TAS, VIC. It can be concluded that the most effective method in forecasting the electricity price in this work is the proposed BTE+GRU model where BTE and GRU are incorporated in the RNN architecture. Meanwhile, Tab. 5 tabulated the average performance evaluation of the proposed BTE+GRU method for 1 week and 2 weeks forecasting. The results show that the RMSE and MAPE values are about the same for both types of forecasting interval which means that the forecasting model is feasible to solve 1 week and 2 weeks forecasting problem. Eventually, accurate information on the electricity price forecasting will contribute to effective management in the deregulated electricity market, complex renewable energy and emission policy objectives.

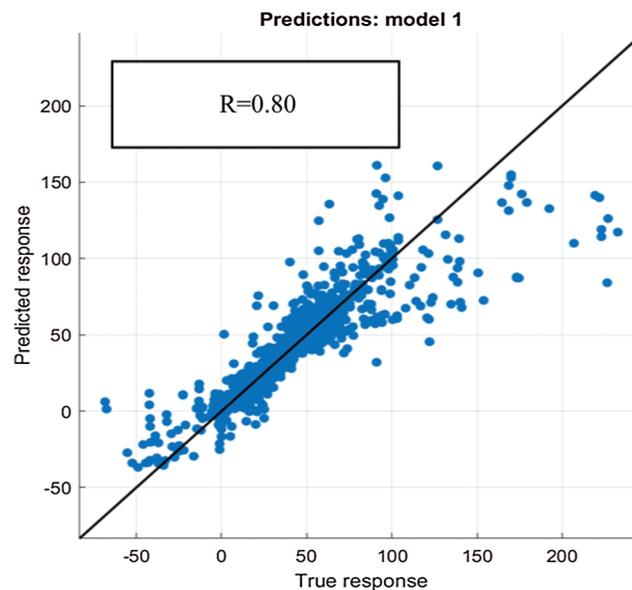


Figure 3: QLD BTE testing model

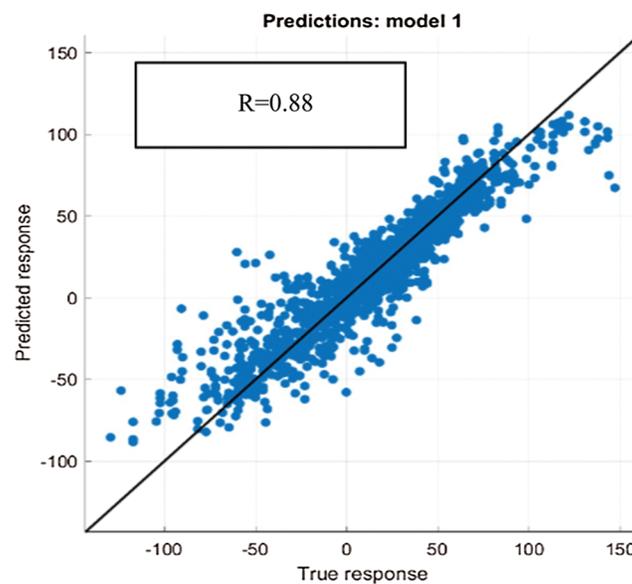


Figure 4: SA BTE testing model

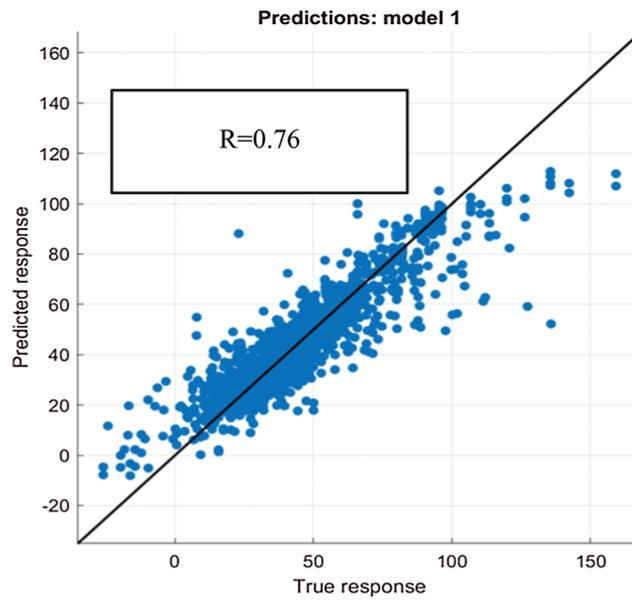


Figure 5: TAS BTE testing model

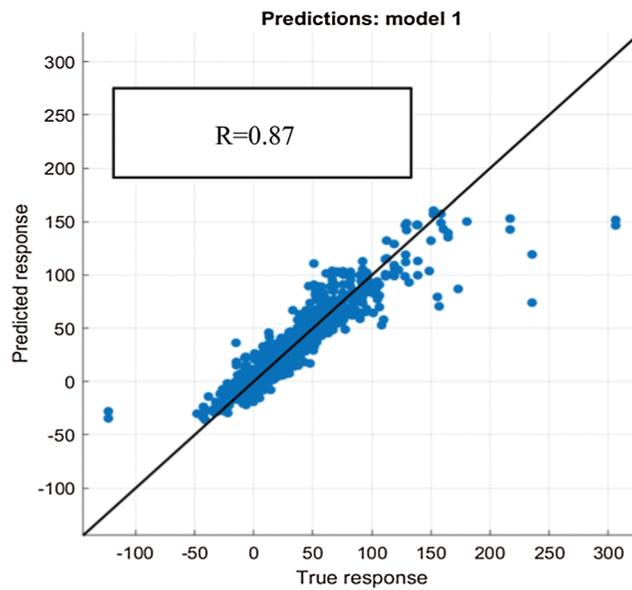


Figure 6: VIC BTE testing model

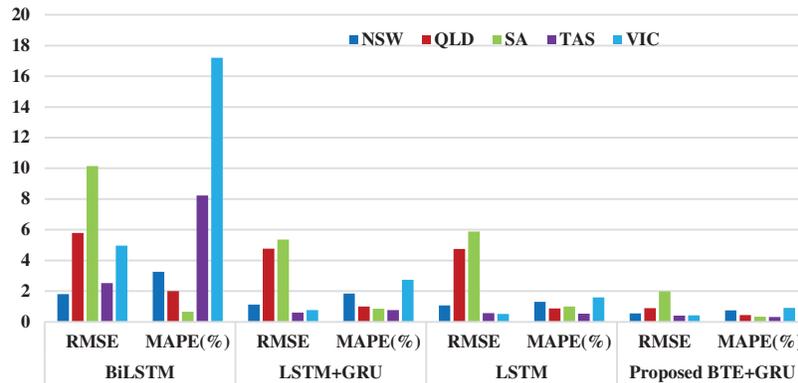


Figure 7: The RMSE and MAPE for EFP using several deep learning methods

Table 4: Comparison of regression correlation coefficient between two different models

States of Australia	R (BTE model)	R (Proposed BTE+GRU model)
NSW	0.78	0.99
QLD	0.80	0.99
SA	0.88	0.98
TAS	0.76	0.99
VIC	0.87	0.99

Table 5: Average performance evaluation of the proposed BTE+GRU method

	1 week forecasting		2 weeks forecasting	
	RMSE	MAPE	RMSE	MAPE
NSW	0.294784	0.671307	0.552075	0.745342
QLD	0.513686	0.428665	0.895746	0.441092
SA	2.263616	0.36288	1.992935	0.326579
TAS	0.404107	0.300019	0.409577	0.318366
VIC	0.308608	0.895352	0.430335	0.905478

As tabulated in [Tab. 6](#), the proposed model is benchmarked with several methods to measure the effectiveness of the proposed BTE and GRU model. As can be seen, the proposed BTE and GRU model produced the lowest mean RMSE and mean MAPE values as compared to other methods which are 0.86 and 0.55 respectively. The work in [\[16\]](#) adopted machine learning approach with Trend and Seasonal Components (TBATS) which adopted trigonometric technique supports forecasting of daily seasonality by applying maximum likelihood estimation. However, TBATS method does not permit the adoption of external regressors. The computation of TBATS+ANN, ANN+ARIMA, TBATS+ARIMA, TBATS+ANN+ARIMA methods were reported in [\[16\]](#) by using Denmark electricity market. It can be seen that the average RMSE for the four methods applied in [\[16\]](#) is significantly high compared to methods applied in this work that adopted deep learning methods such as LSTM, LSTM+GRU, BiLSTM and the proposed model. This justifies the importance of adopting deep learning method in developing an accurate forecasting model.

Table 6: Performance evaluation of the proposed method and other methods

Model	RMSE				MAPE			
	Mean	Min	Max	Std Dev	Mean	Min	Max	Std Dev
The proposed BTE+GRU	0.86	0.12	5.02	1.07	0.55	0.17	1.684	0.39
LSTM	2.55	0.18	18.21	5.09	1.06	1.00	2.81	0.96
LSTM+GRU	2.52	0.33	16.32	5.24	1.43	0.48	5.05	1.28
BiLSTM	5.05	0.84	16.53	4.37	8.27	8.64	59.34	14.57
TBATS+ANN [16]	40.21	8.88	174.2	25.71	33.46	7.53	136.3	21.5
ANN+ARIMA [16]	38.05	8.07	168.8	24.06	31.92	5.90	165.6	21.14
TBATS+ARIMA [16]	37.5	9.94	176.4	26.41	31.11	8.10	162.7	21.86
TBATS+ANN+ARIMA [16]	36.44	8.04	164.2	24.34	30.06	6.63	148.2	20.34

Figs. 8 and 9 show the examples of 1-week forecasting results while Figs. 10 and 11 show the examples of 2-week forecasting results when using the proposed model for two different states in Australia. It can be seen that the electricity price fluctuations for different states of Australia differ due to different demand, supply and energy resources. The results justified that the proposed forecasting model can generate comparatively accurate forecasting results and the deviation between the curve of the proposed BTE+GRU model and the actual load curve is considered the lowest compared to other methods as tabulated in Tab. 6.

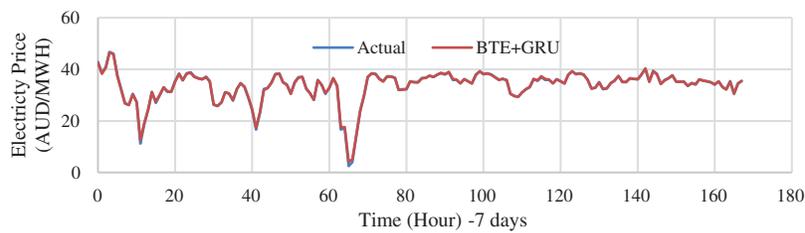


Figure 8: One week forecasting model for NSW

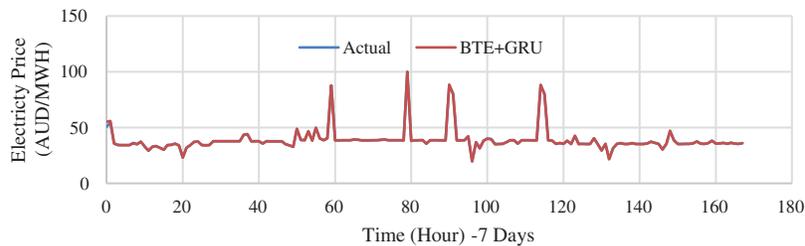


Figure 9: One week forecasting model for TAS

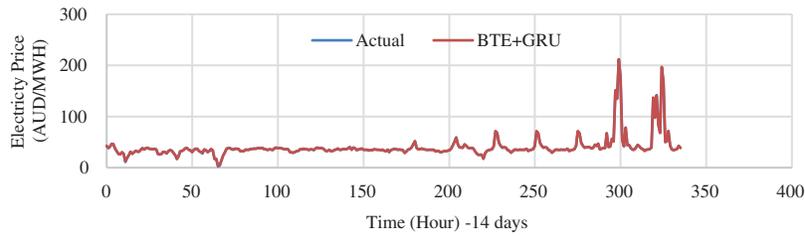


Figure 10: Two weeks forecasting model for NSW

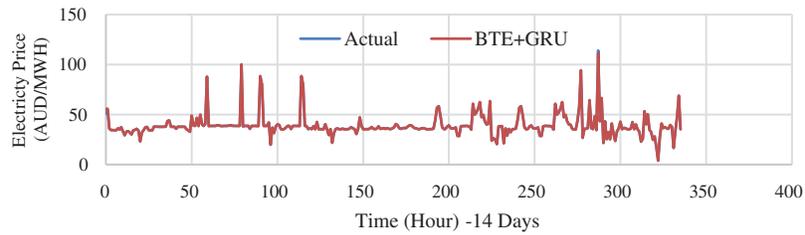


Figure 11: Two weeks forecasting model for TAS

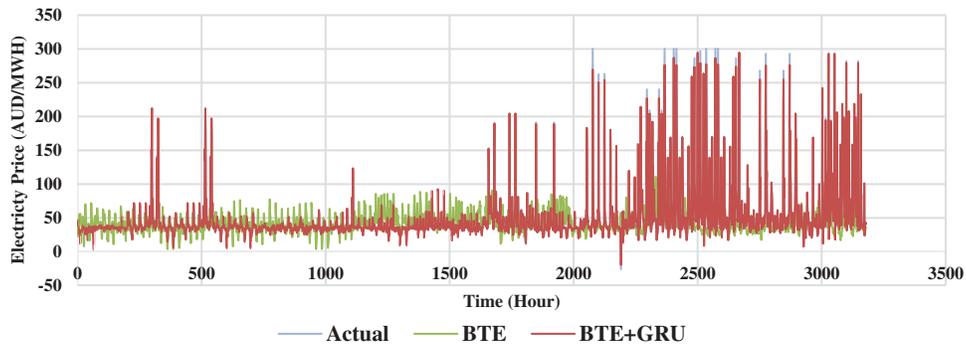


Figure 12: Forecasting model comparison for NSW

Figs. 12–14 presents the 2 weeks forecasting results from the month of January to May 2021 in an hourly basis for three economical states in Australia such as New South Wales, Tasmania and Victoria. At most points, the conventional BTE model was not able to forecast the spikes which justifies the inadequacy of implementing conventional BTE method in EPF. Despite the complex nonlinearity in the trend of electricity price, the proposed model which incorporated BTE and GRU managed to forecast the spikes more accurately and seems to fit the actual data to a satisfactory degree. Hence, this justified the contribution of the proposed model in solving mid-term EPF problem.

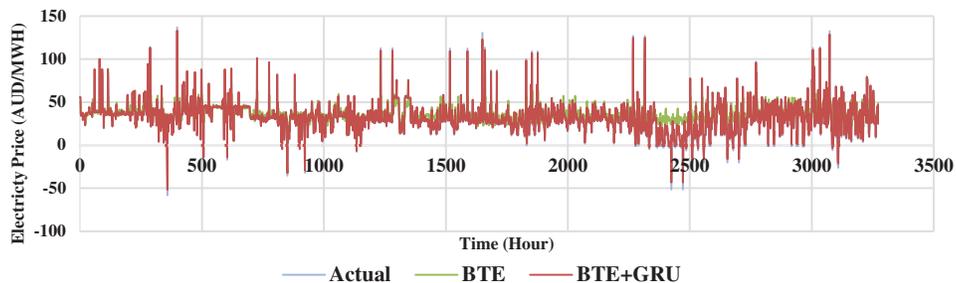


Figure 13: Forecasting model comparison for TAS

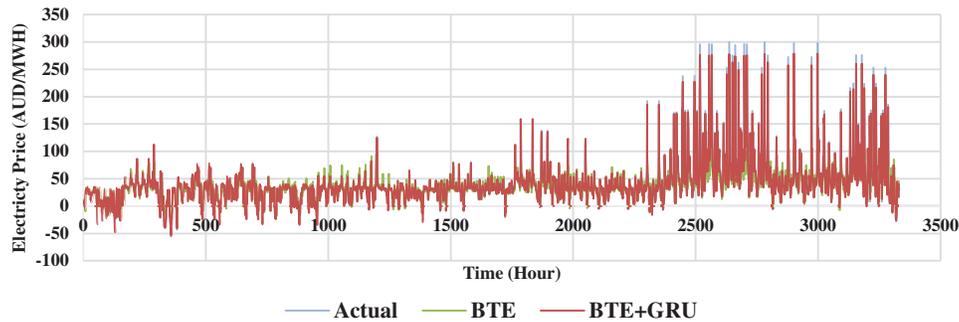


Figure 14: Forecasting model comparison for VIC

Moreover, the MAPE of the proposed forecasting model is benchmarked with previous works that adopted different electricity market as shown in Tab. 7. It can be summarized that the proposed forecasting model for Australian electricity market is feasible with MAPE value in the range of 0.17% to 1.68% as compared to previous works with MAPE values of approximately 11% in [17], 9% in [2], 3% to 5% in [18], 1.9% in [19], 5.85% to 11.8% in [28], and 2.4% to 4.3% in [15]. The MAPE value was computed by averaging the MAPE values for the five states of Australia that are focused in this work. This suggests that the proposed forecasting model is feasible for multi-regional mid-term electricity price forecasting.

Table 7: Benchmarking the proposed method with previous works

Compared model	Electricity market	MAPE (%)	Limitations/challenges
SVM [17] LSSVM [17]	Mid-term PJM electricity market	11.7491% 10.9722%	Accuracy in peak price forecasting considerably low by using the proposed machine learning methods. Optimization of forecasting performance in the peak price area is the main challenge of the study.
Pc4 [2] Auto regressive (AR) [2]	Short-and mid-term electricity market APX. UK	9.01% 8.89%	In summer, the electricity price does not react to the significant decrease in demand. It is challenging to relate the forecasting performance of demand combined with natural gas when applying statistical approach.
ARIMA [18] DBN [18]	Mid-long term electricity consumption wuhan, china	5.140% 3.278%	Data analysis is limited since short-term prediction is challenging.
ANN PSO (Hybrid) [19]	Mid-term load power north american electricity market	1.9%	ANN PSO method is not feasible to handle large data set of nonlinear data.
CNN-KNN [28]	Day-ahead PJM electricity market	5.87%–11.79%	Limited discussion on time series data analysis and statistical reliability.
EEMD-LSTM_SMBO [15]	Day-ahead PJM electricity market	2.47%–4.34%	Uncertain accuracy due to limited variables considered in the prediction model.
Proposed BTE+GRU	Mid-term australian electricity market	0.17%–1.68%	

4 Conclusion

The proposed framework is developed based on information of the demand and price data from various states in Australia (NSW, QLD, SA, TAS, VIC). Furthermore, we also considered renewable and non-renewable energy supplies data, the seasonality, peak and off-peak hours of working and non-

working as the forecasting inputs which substantially impact the electricity pricing. In this work, an optimized GRU consisting of RNN with Bagged Regression Tree forecasting model is proposed for electricity price prediction. Then, the tanh layer is employed to optimize the hyperparameters of the heterogeneous GRU with the aim to improve the model's performance, error reduction and predict the spikes. A machine-learning approach called bagged trees ensemble (BTE) and deep neural network named GRU were successfully integrated in this work to forecast the mid-term electricity price in the current deregulated electricity market. The bagged trees regression is applied to predict nonlinear data which is further optimized by using GRU RNN network. The applied ensemble algorithm managed to enhance the stability of base learners by aggregating the outputs of base learners to generate a single prediction. Finally, a comparative study with conventional time-series models has demonstrated the effectiveness of the proposed methodology. The proposed forecasting model was also compared with previous works and had shown promising results. For future work, the proposed forecasting model can be improved by considering new profit and return-based quality measures. Besides that, the forecasting model can be further modified to solve long-term electricity price forecasting as well. It is worth noting that the methodology presented here can easily be expanded to include a broader scientific domain of time series forecasting applications, such as weather forecasting, earthquake prediction, and heartbeat rate prediction.

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