

Computers, Materials & Continua DOI:10.32604/cmc.2021.014006 Article

# Epidemiological Analysis of the Coronavirus Disease Outbreak with Random Effects

Muhammad Farman<sup>1</sup>, Aqeel Ahmad<sup>1</sup>, Ali Akgül<sup>2,\*</sup>, Muhammad Umer Saleem<sup>3</sup>, Muhammad Naeem<sup>4</sup> and Dumitru Baleanu<sup>5,6,7</sup>

<sup>1</sup>Department of Mathematics and Statistics, University of Lahore, Pakistan
 <sup>2</sup>Department of Mathematics, Faculty of Art and Science, Siirt University, Siirt, 56100, Turkey
 <sup>3</sup>Department of Mathematics, University of Education, Lahore, Pakistan
 <sup>4</sup>Department of Economics and Business Administration, University of Education, Lahore, Pakistan
 <sup>5</sup>Department of Mathematics, Cankaya University, Balgat, 06530, Turkey
 <sup>6</sup>Institute of Space Sciences, Magurele-Bucharest, R76900, Romania
 <sup>7</sup>Department of Medical Research, China Medical University, Taichung,40402, Taiwan
 \*Corresponding Author: Ali Akgül. Email: aliakgul00727@gmail.com
 Received: 30 August 2020; Accepted: 07 January 2021

Abstract: Today, coronavirus appears as a serious challenge to the whole world. Epidemiological data of coronavirus is collected through media and web sources for the purpose of analysis. New data on COVID-19 are available daily, yet information about the biological aspects of SARS-CoV-2 and epidemiological characteristics of COVID-19 remains limited, and uncertainty remains around nearly all its parameters' values. This research provides the scientific and public health communities better resources, knowledge, and tools to improve their ability to control the infectious diseases. Using the publicly available data on the ongoing pandemic, the present study investigates the incubation period and other time intervals that govern the epidemiological dynamics of the COVID-19 infections. Formulation of the testing hypotheses for different countries with a 95% level of confidence, and descriptive statistics have been calculated to analyze in which region will COVID-19 fall according to the tested hypothesized mean of different countries. The results will be helpful in decision making as well as in further mathematical analysis and control strategy. Statistical tools are used to investigate this pandemic, which will be useful for further research. The testing of the hypothesis is done for the differences in various effects including standard errors. Changes in states' variables are observed over time. The rapid outbreak of coronavirus can be stopped by reducing its transmission. Susceptible should maintain safe distance and follow precautionary measures regarding COVID-19 transmission.

**Keywords:** Covid-19; infectious disease; statistical analysis; p-value; epidemiology hypothesis



This work is licensed under a Creative Commons Attribution 4.0 International License, which permits unrestricted use, distribution, and reproduction in any medium, provided the original work is properly cited.

#### 1 Introduction

Severe Acute Respiratory Syndrome (SARS) is also caused by a coronavirus and plays an important role for its investigation [1]. According to the group of investigators, SARS and coronavirus have many similar features [2]. RNA enveloped virus known as coronavirus is spreading particularly among humans, mammals and birds. Many respiratory, enteric, hepatic and neurological diseases are caused by coronavirus [3,4]. Human disease is caused by six different types of coronavirus [5]. The symptom of the common cold in immune-compromised individuals is caused by 229E, OC43, NL63 and HKU1 coronaviruses whereas other 2 coronavirus types are zoonotic in origin. These two are Severe Acute Respiratory Syndrome Coronavirus (SARS-CoV) and Middle East Respiratory Syndrome Coronavirus (MERS-CoV). SARS-CoV and MERS-CoV are fatal in their nature [6]. In 2002 and 2003, Guangdong (the province of China) faced major outbreaks of acute respiratory syndrome which has a caustic agent of SARS-CoV. The Middle East suffered from severe respiratory disease outbreaks which have a caustic agent of MERS-CoV in 2012. Given the high occurrence and wide dispersal of coronaviruses, the large inherent variety and frequent recombination of their genomes, which is increasing interface between human and animal activities, novel coronaviruses are likely to emerge periodically in humans owing to frequent cross-species infections and occasional spillover events [7,8].

In 2019, China faced a major outbreak of Coronavirus disease 2019 (COVID-19) and this outbreak had the potential to become a worldwide pandemic [9]. Interventions and real-time data are needed for the control on this outbreak of coronavirus [10]. In previous studies, the transfer of the virus from one person to another person, its severity and history of the pathogen in the first week of the outbreak has been explained with the help of real-time analysis [11]. In December 2019, a group of people in Wuhan admitted to the hospital that all were suffering from pneumonia and the cause of pneumonia was idiopathic. Most of the people linked the cause of pneumonia with the eating of wet markets and seafood. Investigation on etiology and epidemiology of disease was conducted on the 31st December 2019 by Chinese Center for Disease Control and Prevention (China CDC) with the help of Wuhan city health authorities [8]. Epidemical changings were measured by time-delay distributions including date of admission to hospital and death. According to the clinical study on the COVID-19, symptoms of coronavirus appear after 7 days of onset of illness [12]. The time from hospital admission to death is also critical to the avoidance of underestimation when calculating case fatality risk [13]. COVID-19 epidemiological data and incubation period were measured through public data on known cases [14]. More detail can be found in [15-20].

# 2 Materials and Method

WHO is working closely with clinicians caring for patients with COVID-19, in China and across the globe. International experts on infectious disease can give better understanding, realtime data, the clinical presentation, natural history and treatment interventions for COVID-19. A majority of patients with COVID-19 are adults. Among 44672 patients in China with confirmed infection, 2.1% were of or under the age of 20. The most commonly reported symptoms included fever, dry cough, and shortness of breath, and most patients (80%) experienced mild illness. Approximately 14% experienced severe diseases and 5% were critically ill. Early reports suggested that illness severity is associated with age above sixty (>60 years old) and comorbidity [15]. The latest outbreak of coronavirus 2019 was noted on March 12, 2020 [16] when coronavirus cases were 126,369 with 4,633 deaths and a recovered population of 68,304. Active cases were 53428 out of those 89% were in mild condition and 11% were critical. In closed cases recovered were 94 % and deaths were 6%. Data used for analysis is given in Tabs. 1 and 2.

 Table 1: Worldwide data of COVID-19 combined

Closed cases			Active cases		
Total	Death	Recovered	Mild condition	Critical condition	
114502	4027	64273	32569	7094	

S.No	Country	Total cases	Total death	Total recovered	Active cases
1	China	80757	3136	60096	1725
2	South Korea	7513	54	247	7212
3	Italy	9172	463	724	7985
4	Iran	7161	237	2349	4530
5	Japan	530	9	101	420
6	France	1412	30	12	1370
7	Germany	1224	2	16	1204
8	Spain	1231	30	2	1169
9	Singapore	160		78	67
10	USA	729	27	9	687
11	Hong Kong	100	2	36	62
12	<b>Diamond Princes</b>	706	7	100	599
13	Kuwait	56			56
14	Bahrain	49			49
15	Thailand	43	1	30	12
16	Taiwan	41	1	12	28
17	UK	40		8	32
18	Australia	33	1	15	17
19	Switzerland	30		1	29
20	Malaysia	29		22	7
21	Canada	27		7	20
22	Iraq	26			26
23	Norway	25			15
24	UAE	21		6	16
25	Austria	18			18
26	Netherlands	18			18
27	Vietnam	16		16	
28	Sweden	15			15
29	Lebanon	13			13
30	Israel	12		1	11
31	mACAO	10		6	4

 Table 2: Country-wise of COVID-19

(Continued)

S.No	Country	Total cases	Total death	Total recovered	Active cases
32	Iceland	9			9
33	San Marino	8	1		7
34	Belgium	8		1	7
35	Croatia	8			8
36	Finland	7		1	6
37	Greece	7			7
38	Qatar	7			7
39	Ecuador	6			6
40	India	6		3	3
41	Mexico	6		1	5
42	Oman	6		2	4
43	Algeria	5			5
44	Pakistan	5			5
45	Czeshia	4			4
46	Denmark	4			4
47	Philippines	3	1	2	0
48	Azerbaijan	3			3
49	Georgia	3			3
50	Romania	3		1	2
51	Russia	3		2	1
52	Brazil	2			2
53	Egypt	2		1	1
54	Indonesia	2			2
55	Portugal	2			2
56	Afghanistan	1			1
57	Andorra	1			1
58	Armenia	1			1
59	Belarus	1			1
60	Cambodia	1		1	0
61	Dominican Republic	1			1
62	Estonia	1			1
63	Ireland	1			1
64	Jordan	1			1
65	Latvia	1			1
66	Lithuania	1			1
67	Luxembourg	1			1
68	North Macedonia	1			1
69	Monaco	1			1
70	Morocco	1			1
71	Nepal	1		1	0
72	New Zealand	1			1

Table 2: Continued

(Continued)

S.No	Country	Total cases	Total death	Total recovered	Active cases
73	Nigeria	1			1
74	Saudi Arabia	1			1
75	Senegal	1			1
76	Sri Lanka	1		1	0
77	Tunisia	1			1

 Table 2: Continued

### **3** Formulation for Data Analysis

### 3.1 Case-I

Testing of hypothesis about mean of normal population when  $\sigma$  is unknown and n < 30. Let  $x_1, x_2, \ldots, x_n$  be the observation in a small sample size n, taken from the normally distributed population. Let  $\overline{x}$  be the sample mean and s be the unbiased estimate of  $\sigma$ . So, the procedure of testing hypothesis is given as:

- 1. Formulate null and alternate hypothesis about  $\mu$ , three possibilities occur:
  - (a)  $H_o: \mu = \mu_o$  and  $H_1: \mu \neq \mu_o$  (two tailed)
  - (b)  $H_o: \mu \leq \mu_o$  and  $H_1: \mu > \mu_o$  (one sided)
  - (c)  $H_o: \mu \ge \mu_o$  and  $H_1: \mu < \mu_o$  (one sided)
- 2. Decide upon the significance level  $\alpha$ , as

$$P\left(\overline{x} - t_{\frac{\alpha}{2}(\nu)}\frac{s}{\sqrt{n}} < \mu < \overline{x} + t_{\frac{\alpha}{2}(\nu)}\frac{s}{\sqrt{n}}\right) = 1 - \alpha$$

where v = n - 1 degree of freedom.

3. Computing the t-value from the sample data by using the test statistics as follows

$$t = \frac{\overline{x} - \mu_o}{\frac{s}{\sqrt{n}}}$$

4. Determine the critical region for which  $H_o$  corresponding to different alternative hypothesis is given in Tab. 3.

Alternate hypothesisThe critical region will be $H_1: \mu \neq \mu_o$  $|t| \ge t_{\frac{\alpha}{2}(\nu)}$  $H_1: \mu > \mu_o$  $t \ge t_{\alpha, \nu}$  $H_1: \mu < \mu_o$  $t \le -t_{\alpha, \nu}$ 

Table 3: Alternate hypothesis for case I

### 3.2 Case-II

Suppose that we have two small random sample  $x_{11}, x_{12}, ..., x_{1n_1}$  and  $x_{21}, x_{22}, ..., x_{2n_2}$  from two normally distributed population with a mean  $\mu_1$  and  $\mu_2$  and standard deviation  $\sigma_1$  and  $\sigma_2$ 

respectively. If  $\sigma_1 \neq \sigma_2$ , then we use their sample estimations  $s_1$  and  $s_2$  to compute the standard error of the difference between means as:

$$\sigma_{\overline{x}_1 - \overline{x}_2} = \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$$

As there is no point in combining in  $\sigma_1^2$  and  $\sigma_2^2$  be obtained an estimate of the non-existing common population. Consequently, using to test the hypothesis that difference between mean has a specified value, so

- 1. Formulate null and alternate hypothesis about  $\mu$ , three possibilities are presented as:
  - (a)  $H_o: \mu_1 \mu_2 = \Delta_o$  and  $H_1: \mu_1 \mu_2 \neq \Delta_o$  (two tailed) (b)  $H_o: \mu_1 - \mu_2 \leq \Delta_o$  and  $H_1: \mu_1 - \mu_2 > \Delta_o$  (one sided)
  - (c)  $H_o: \mu_1 \mu_2 \ge \Delta_o$  and  $H_1: \mu_1 \mu_2 < \Delta_o$  (one sided)
- 2. Decide upon the significance level  $\alpha$ . Then, we obtain

$$P\left(\overline{x_1} - \overline{x}_2 - t_{\frac{\alpha}{2}(\nu)}\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}} < \mu_1 - \mu_2 < \overline{x}_1 - \overline{x}_2 + t_{\frac{\alpha}{2}(\nu)}\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}\right),$$

where,

$$v = \frac{\left[\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}\right]^2}{\frac{\left(\frac{s_1^2}{n_1}\right)^2}{n_1 - 1} + \frac{\left(\frac{s_2^2}{n_2}\right)^2}{n_2 - 1}}$$

3. Computing the t-value from the sample data by using the test statistics gives:

$$t = \frac{\overline{x_1 - \overline{x_2} - \Delta_o}}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}, \quad \text{if } \Delta_o = 0, \quad \text{then } t = \frac{\overline{x_1 - \overline{x_2}}}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$$

4. Determine the critical region for which  $H_o$  corresponding to different alternative hypothesis is given in Tab. 4.

Alternate hypothesis	The critical region will be
$\overline{H_1:\mu_1-\mu_2\neq\Delta_o}$	$ t  \ge t_{\frac{\alpha}{2}(v)}$
$H_1: \mu_1 - \mu_2 > \Delta_o$	$t \ge t_{\alpha, v}$
$H_1: \mu_1 - \mu_2 < \Delta_o$	$t \leq -t_{\alpha,v}$

Table 4: Alternate hypothesis for case II

The following Tabs. 5a and 5b are used for the analysis of total country-wise data with a different hypothesis and Tab. 6 is used to check the outbreak of the epidemic disease.

(a)					
Country	Population	Total Cases	Total Death	Total recovered	
China	1408626449	80757	3136	60096	
South Korea	51269185	7513	54	247	
Italy	60461826	9172	463	724	
Iran	83639890	7161	237	2349	
Japan	126601378	530	9	101	
France	65273511	1412	30	12	
Germany	83969900	1224	2	16	
Spain	46754778	1231	30	2	
Singapore	5850342	160		78	
USA	330370141	729	27	9	
Sum	2262817400	109889	3988	63634	
Average	226281740	10988.9	443.1111111	6363.4	
Standard deviation	403010937.5	23477.28628	962.833601	17924.06309	
hypothesized mean	0	0	0	0	
Test statistics	1.776	1.48	1.455	1.123	
DF	9	9	9	9	
significance level(p)	0.1095	0.173	0.1796	0.2906	
95% CI for mean	-62014917.5410	-5805.7389	-245.6586	-6458.7023	
	to	to 27783.5389	to 1131.8808	to 19185.5023	
	514578397.5410				
		(b)			
Active Cases	Critical Condition	Death Rate	Infected Rata	Recovered Rate	
1725	4794	0.038832547	5.73303E-05	0.744158401	
7212	36	0.007187542	0.00014654	0.032876348	
7985	733	0.050479721	0.000151699	0.078935892	
4530		0.033095936	8.5617E-05	0.328026812	
420	33	0.016981132	4.18637E-06	0.190566038	
1370	66	0.021246459	2.16321E-05	0.008498584	
1204	9	0.001633987	1.45767E-05	0.013071895	
1169	11	0.024370431	2.63289E-05	0.001624695	
67	8	0	2.73488E-05	0.4875	
687	7	0.037037037	2.20662E-06	0.012345679	
26369	5697	0.230864791	0.000537466	1.897604344	
2636.9	633	0.023086479	5.37466E-05	0.189760434	
2740.131619	1487.749232	0.016066786	5.32548E-05	0.241446607	
0	0	0	0	0	
3.043	1.345	4.544	3.191	2.485	
9	9	9	9	9	
0.0139	0.2114	0.0014	0.011	0.0347	
676.7279 to 4597.0721	-431.2717	0.0116	0.0000	0.0170	
	to 1697.2717	to 0.0346	to 0.0001	to 0.3625	

Table 5: Total data for statistical analysis

Different cases	Testing of hypothesis of total case and recovered case	Testing of hypothesis of total cases and active cases	Testing of hypothesis of total case and death case	Testing of hypothesis of total case and critical condition
Mean difference standard error	4625.5 9340.53	8352 7474.565	10545.789 7430.411	10355.9 7439.062
DF significance level (p) 95% CI for mean	0.459 18 0.6264 -24249.2253 to 14998.2253	1.117 18 0.2785 -7351.4794 to 24055.4794	1.419 18 0.1729 -5064.9245 to 26156.5023	1.392 18 0.1809 -5272.9884 to 25984.7884

Table 6: Testing of hypothesis for differences of mean

#### 4 Discussion

The mean incubation period was 5.2 days (95% confidence interval, 4.1 to 7.0), with the 95th percentile of the distribution at 12.5 days. In its early stages, the epidemic doubled in size every 7.4 days. With a mean serial interval of 7.5 days (95% CI, 5.3 to 19), the basic reproductive number was estimated to be 2.2 (95% CI, 1.4 to 3.9) [17]. Across the analyzed period, the delay between symptom onset and seeking care at a hospital or clinic were longer in Hubei province than in other provinces in mainland China and internationally. In mainland China, these delays decreased from 5 days before January 18, 2020, to 2 days thereafter until January 31, 2020 (p = 0.0009). Although our sample captures only 507 (5.2%) of 9826 patients with COVID-19 reported by official sources during the analyzed period, our data align with an official report published by Chinese authorities on January 28, 2020 [11].



Figure 1: Outbreak of total cases and recovered cases of corona virus



Figure 2: Outbreak of Active cases, Critical condition and death individual with corona virus

Figs. 1 and 2 represent the actual status of total cases, recovered cases, active cases, critical conditions and death cases of COVID-19 for the major affected countries till March 10, 2020. Fig. 3 represents the comparison of the worldwide effect of coronavirus with time delay which shows how coronavirus spread in a fast way during last week till 17-03-2020. Figs 4–8 represent the behavior of developed hypotheses with zero hypothesized mean of total cases, recovered, death and active cases including critical condition for the p-value respectively. Figs 9–12 represent the behavior of developed hypotheses of differences total cases with other compartments for the p value of zero hypothesized difference mean.



Figure 3: Comparison of coronavirus outbreak with time delay



Figure 4: Testing of hypothesis for average coronavirus cases



Figure 5: Testing of hypothesis for average death cases



Figure 6: Testing of hypothesis for average recovered cases



Figure 7: Testing of hypothesis for average active cases



Figure 8: Testing of hypothesis for average critical cases



Figure 9: Testing of hypothesis for difference between total and recovered cases



Figure 10: Testing of hypothesis for differences of total and death cases



Figure 11: Testing of hypothesis for differences of total and active cases



Figure 12: Testing of hypothesis for differences of total and critical condition

# 5 Conclusion

Investigation of developed hypotheses for different countries with 95% confidence and the average effects were calculated country-wise including p-value which shows how much significance is increased in COVID 19. Also, the hypothesis was developed for the differences of different effects with total cases including standard error with zero hypothesized difference mean. Ultimately a decision was made for the developed hypothesis to accept or reject our null hypothesis. Graphical representation of spread virus with developed hypotheses can be easily analyzed to show the actual behavior and effect of diseases. Comparison was made to check the increasing effects worldwide over the time.

Acknowledgement: We certify that the information that we have presented here is accurate and complete to the best of our knowledge.

Funding Statement: The authors received no specific funding for this study.

**Conflicts of Interest:** The authors declare that they have no conflicts of interest to report regarding the present study.

# References

- R. S. Baric, K. Fu, W. Chen and B. Yount, "High recombination and mutation rates in mouse hepatitis virus suggest that coronaviruses may be potentially important emerging viruses," *Advances in Experimental Medicine and Biology*, vol. 380, pp. 571–576, 1995.
- R. Mark and M. D. Denison, Coronavirus Research: Keys to Diagnosis, Treatment and Prevention of SARS. Bookshelf ID, NBK92477: ncbi, National Academy of Sciences, 2004.
- [3] S. R. Weiss and J. L. Leibowitz, "Coronavirus pathogenesis," *Advances in Virus Research*, vol. 81, pp. 85–164, 2011.
- [4] P. S. Masters, S. Perlman and S. Coronaviridae, In: D. M. Knipe, P. M. Howley (Eds.), *Fields Virology*, 6<sup>th</sup> ed., vol. 2. Philadelphia: Lippincott Williams & Wilkins, pp. 825–858, 2013.
- [5] S. Su, G. Wong, W. Shi, J. Lue, A. C. K. Lai *et al.*, "Epidemiology, genetic recombination, and pathogenesis of coronaviruses," *Trends Microbiology*, vol. 24, no. 6, pp. 490–502, 2016.
- [6] N. S. Zhong, B. J. Zheng and Y. M. Li, "Epidemiology and cause of severe acute respiratory syndrome (SARS) in Guangdong," *Lancet*, vol. 362, pp. 1353–1358, 2003.
- [7] G. Wong, W. Liu, Y. Liu, B. Zhou, Y. Bi et al., "SARS, and Ebola: The role of super-spreaders in infectious disease," Cell Host & Microbe, vol. 18, no. 4, pp. 398–401, 2015.
- [8] N. Zhu, D. Zhang and W. Wang, "A Novel Coronavirus from Patients with Pneumonia in China," *The new England journal of medicine*, vol. 727, pp. 1–7, 2019.
- [9] WHO, "Statement on the second meeting of the International Health Regulations, Emergency Committee regarding the outbreak of novel coronavirus (2019-nCoV)," 2005. https://www.who.int/news/item/.
- [10] C. Rivers, J. P. Chretien, S. Riley, J. A. Pavlin, A. Woodward et al., "Using outbreak science to strengthen the use of models during epidemics," *Nature Communication*, vol. 10, no. 1, pp. 3102, 2019.
- [11] K. Sun, J. Chen and C. Viboud, "Early epidemiological analysis of the coronavirus disease 2019 outbreak based on crowd sourced data: A population-level observational study," *Lancet Digital Health*, vol. 7500, no. 20, pp. 30026–30021, 2020.
- [12] M. Natalie, T. Kobayashi Linton and Y. Yang, "Incubation period and other epidemiological characteristics of 2019 novel coronavirus infections with right truncation: A statistical analysis of publicly available case data," *Journal of Clinical Medicine*, vol. 9, no. 2, pp. 538, 2020.
- [13] C. Huang, Y. Wang, X. Li, L. Ren and J. Zhao et al., "Clinical features of patients infected with 2019 novel coronavirus in Wuhan," *Lancet*, vol. 395, pp. 497–506, 2020.
- [14] C. A. Donnelly, A. C. Ghani, G. M. Leung, A. J. Hedley, C. Farser *et al.*, "Epidemiological determinants of spread of causal agent of severe acute respiratory syndrome in Hong Kong," *Lancet*, vol. 361, no. 9371, pp. 1761–1766, 2003.
- [15] World meter Caronavirus, https://www.worldometers.info/coronavirus/.
- [16] L. Qun, X. Guan and P. Wu, "A novel coronavirus from patients with pneumonia in china," 2019 The New England Journal of Medicine, vol. 2001316, pp. 727–733, 2019.
- [17] M. Naveed, D. Baleanu, M. Rafiq, A. Raza, A. H. Soori *et al.*, "Dynamical behavior and sensitivity analysis of a delayed coronavirus epidemic model," *Computers Materials & Continua*, vol. 65, no. 1, pp. 225–241, 2020.
- [18] D. Baleanu, H. Mohammadi and S. Rezapour, "A fractional differential equation model for the COVID-19 transmission by using the Caputo-Fabrizio derivative," *Advances in Difference Equations*, vol. 20, no. 1, pp. 299, 2020.

- [19] A. Raza, M. Farman, A. Akgül, M. S. Iqbal, A. Ahmad *et al.*, "Simulation and numerical solution of fractional order Ebola virus model with novel technique," *AIMS Bioengineering*, vol. 7, no. 4, pp. 194–207, 2020.
- [20] A. Ahmed, B. Salam, M. Mohammad, A. Akgül and S. H. A. Khoshnaw, "Analysis coronavirus disease (COVID-19) model using numerical approaches and logistic model," *AIMS Bioengineering*, vol. 7, no. 3, pp. 130–146, 2020.