

**ARTICLE**

Identification Method for Users-Transformer Relationship in Station Area Based on Local Selective Combination in Parallel Outlier Ensembles Algorithm

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ABSTRACT

In the power distribution system, the missing or incorrect file of users-transformer relationship (UTR) in low-voltage station area (LVSA) will affect the lean management of the LVSA, and the operation and maintenance of the distribution network. To effectively improve the lean management of LVSA, the paper proposes an identification method for the UTR based on Local Selective Combination in Parallel Outlier Ensembles algorithm (LSCP). Firstly, the voltage data is reconstructed based on the information entropy to highlight the differences in between. Then, the LSCP algorithm combines four base outlier detection algorithms, namely Isolation Forest (I-Forest), One-Class Support Vector Machine (OC-SVM), Copula-Based Outlier Detection (COPOD) and Local Outlier Factor (LOF), to construct the identification model of UTR. This model can accurately detect users' differences in voltage data, and identify users with wrong UTR. Meanwhile, the key input parameter of the LSCP algorithm is determined automatically through the line loss rate, and the influence of artificial settings on recognition accuracy can be reduced. Finally, this method is verified in the actual LVSA where the recall and precision rates are 100% compared with other methods. Furthermore, the applicability to the LVSA with difficult data acquisition and the voltage data error in transmission are analyzed. The proposed method adopts the ensemble learning framework and does not need to set the detection threshold manually. And it is applicable to the LVSA with difficult data acquisition and high voltage similarity, which improves the stability and accuracy of UTR identification in LVSA.

KEYWORDS

Low-voltage station area; users-transformer relationship identification; line loss; ensemble learning; LSCP algorithm

Nomenclature

UTR	Users-transformer relationship
LVSA	Low-voltage station area
LSCP	Local Selective Combination in Parallel Outlier Ensembles algorithm
I-Forest	Isolation Forest
OC-SVM	One-Class Support Vector Machine
COPOD	Copula-Based Outlier Detection



LOF	Local Outlier Factor
DTW	Dynamic time warping distance
MILP	Mixed integer linear programming
LVDN	Low-voltage distributed network
KNN	K-Nearest Neighbor

1 Introduction

The users-transformer relationship (UTR) refers to the subordinate relationship between the end user's electricity meter and the transformer in the low-voltage station area (LVSA). The UTR of LVSA in China is shown in Fig. 1. The correct UTR is the guarantee for outage management [1], LVSA line loss calculation [2], line transformation, and other services [3]. The transformation and upgrading of low-voltage distribution lines make the relationship between users and transformer change frequently [4]. Delay or manual omission in the information update of power distribution system will lead to wrong UTR files in LVSA. The incorrect UTR affects the operation and maintenance of the distribution network [5], and causes the inconsistent measurement data of the marketing measurement system between users and the transformer, which will lead to the abnormal line loss of the LVSA and affect the lean management of the LVSA [6].

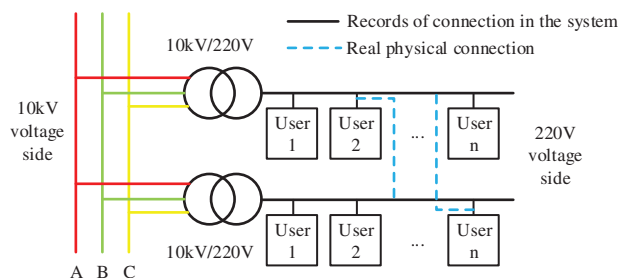


Figure 1: The UTR of LVSA in China

To solve the problems, such as abnormal line loss caused by the wrong UTR, it is necessary to identify the UTR in LVSA. Traditional engineering methods, including instantaneous power outage method [7] and pulse current method [8,9], etc., require manual on-site verification and have low accuracy and efficiency, which are not in line with the intelligent development goal of the distribution network. Therefore, it is urgent to put forward a new method of the UTR identification, which can meet the requirements of accuracy and intelligence and facilitate the digital transformation of the distribution network [10].

In recent years, with the popularity of smart meters, the acquisition system has accumulated massive electrical data of users, providing a basis for the UTR identification in the LVSA [11,12]. At present, the existing data-driven identification methods for UTR can be roughly divided into four categories, which are based on the similarity of electrical data, conservation of electrical data, multi-source data, and others.

1. Similarity of electrical data: the similarity of all customer voltage data was measured based on the Pearson correlation coefficient [13–16] and discrete Frechet distance [17]. UTR was identified according to the level of similarity. But the boundary between actual LVSA's voltage data is fuzzy, resulting in the similarity threshold difficult to determine. So, users with high similarity of voltage data cannot be distinguished. In [18], the voltage zero-crossing sequences were

- constructed from raw voltage data. Accordingly, an improved spectral clustering algorithm was proposed for UTR identification. In [19], the adaptive piecewise aggregate approximation algorithm was used to extract the features of voltage data, and the improved density-based spatial clustering of application with noise algorithm was used to get the users with wrong UTR. In [20–22], the dynamic time warping distance (DTW) algorithm was used to analyze the voltage data difference between users and transformer in LVSA, and the UTR was obtained by clustering algorithm according to the DTW distance. The clustering method needs to obtain the number and voltage data of adjacent LVSA in advance, which is not suitable for the identification of UTR without the boundary of a single station, and is susceptible to the influence of noise data. In [23], an outlier detection algorithm was adopted to rectify the UTR, but this algorithm relies on the selection of the number of neighborhood data points, and is difficult to determine the parameter.
2. Conservation of electrical data: In [24,25], the objective function was constructed according to the power conservation and solved with an optimization algorithm to obtain the membership relationship of users in LVSA. In [26,27], a UTR identification model was constructed based on Kirchhoff's law of current, and the mixed integer linear programming (MILP) algorithm was used to get the results. However, this method has complicated calculation and high requirements for data integrity. It is not applicable to the LVSA where data collection is difficult.
 3. Multi-source data: In [28], principal component analysis and independent component analysis were used to extract features from voltage data. Then, the K-means clustering method is used to classify the voltage data into corresponding groups due to the users in the same LVSA have the same voltage characteristics. Finally, the Pearson correlation coefficient between the different groups of users' total current and transformer's current was compared to realize UTR identification. In [11], a multiple linear regression model using voltage and power data of users meters was established to estimate topology, line parameters, and user and line phasing connections in LVSA.
 4. Other methods: In [29], a UTR identification algorithm that combines the data preprocessing with multi-dimensional prior knowledge based on voltage characteristics in low-voltage distributed network (LVDN) was proposed to get users with wrong UTR and their real UTR. Each LVDN has its own special structure. The prior knowledge of voltage characteristics extracted from a single LVDN may not be applicable to the identification of the UTR of massive LVSA. In [30], the knowledge graph of LVDN topology was constructed by integrating data in multiple LVDN information systems, and UTR in LVDN information system was verified based on the knowledge graph. However, the formation rules of the knowledge graph of the LVDN topology are complex, which require the fusion of multiple data. The disadvantage of the method lies in the difficulty of obtaining GIS data and the high requirements for the accuracy of data. [Table 1](#) provides a brief summary of the literature on UTR identification.

Table 1: Brief summary of the literature on UTR identification

UTR identification	Key words	References
Similarity of electrical data	Pearson correlation coefficient	[13–16]
	Discrete Frechet distance	[17]
	Clustering	[18–22]
	Outlier detection	[23]
Conservation of electrical data	Power conservation	[24,25]
	Current conservation	[26,27]
Multi-source data	Voltage data and current data	[28]
	Voltage data and power data	[11]
Other methods	Prior knowledge	[29]
	Knowledge graph	[30]

Based on the voltage distribution characteristics in LVDN, the similarity of voltage data changes is low due to the fact that users in different LVSA belong to different outgoing lines and have a long electrical distance [31]. Based on the voltage data difference of users in different LVSA, an outlier detection algorithm can be used to identify users with wrong UTR. Zimek et al. [32,33] have studied the ensemble method of outlier detection. Compared with a single outlier detection model, the ensemble method combines multiple outlier detection models to achieve better performance and reliability. The ensemble learning is also widely used in electricity theft detection [34], power dispatching data anomaly detection [35], and time series anomaly detection [36]. Therefore, to enhance the stability and accuracy of identification results, the outlier detection method with an ensemble framework is applied to the UTR identification.

Different electrical characteristics of different LVSA, high similarity between individual LVSA voltage data, and limited data, lead to low accuracy, weak applicability and low reliability of UTR identification in the existing methods. To solve these problems, this paper proposes a UTR identification method based on Local Selective Combination in Parallel Outlier Ensembles (LSCP) algorithm. The main contributions of the paper are listed as follows:

1. Information entropy is used to reconstruct the original voltage data to highlight the difference between data and reduce the impact of data noise.
2. Based on the voltage characteristics of the LVDN, an identification method of UTR based on the ensemble framework LSCP algorithm is proposed, which increases the accuracy and stability of identification results of UTR in the LVSA.
3. Based on the historical line loss rate data in LVSA, the key input parameter of the proposed model is determined automatically, which increases the accuracy of the identification result, avoids the artificial parameter setting, and is more suitable for the implementation of the UTR identification in the massive LVSA.

The rest of this paper is organized as follows. Section 2 describes the mathematical model of the proposed ensemble learning outlier detection algorithm. Section 3 deduces the realization process of UTR identification based on the proposed model. The tests and results are illustrated in Section 4. Lastly, the conclusion of the study and the future work are drawn in Section 5.

2 Ensemble Learning Outlier Detection Model

The core function of the outlier detection method is to identify the data with different regularity from most data in the input dataset. Compared with the outlier detection algorithm of the general ensemble framework, the LSCP algorithm is a completely unsupervised outlier detection algorithm integrated with multiple outlier detection algorithms in parallel [37].

2.1 Introduction of LSCP Algorithm

To strengthen the stability and robustness of the identification result of the UTR in LVSA, we adopt the LSCP algorithm to identify the UTR. Fig. 2 is the overall framework of the LSCP algorithm, The characteristics of the LSCP algorithm are as follows: (1) Multiple base outlier detection models are calculated independently and executed in parallel; (2) According to the performance of the base outlier detection model, the combined base model is dynamically selected; (3) Feature sample subspaces are constructed from subsequences of different dimensions of randomly sampled data to emphasize local anomalies; (4) Support the base outlier detection model of heterogeneous or isomorphic.

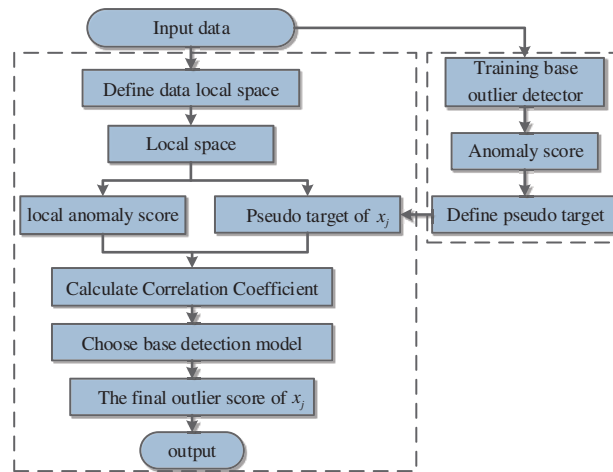


Figure 2: The framework of the LSCP algorithm

The specific flow of outlier data detection by the LSCP algorithm is as follows:

1) Train base outlier detector

Enter the voltage dataset $X \in R^{n \times d}$ to be detected. The base outlier detector is $C = \{C_1, C_2, \dots, C_R\}$. The basic outlier detectors are trained, then the abnormal score matrix $O(X) \in R^{n \times R}$ is obtained in Eq. (1).

$$O(X) = [C_1(X), C_2(X), \dots, C_R(X)] \tag{1}$$

2) Define data local space

For each piece of voltage data $x_i \in X$, $x_i \in R^{1 \times d}$, construct the feature subsequence x'_i of the dimension $[Min_dimension, Max_dimension]$ by random sampling, and get a set of feature subspace of dataset X . In feature subspace, calculate the Euclidean distance with x'_i , using the method of K-Nearest Neighbor (KNN), and get the nearest K neighbor samples.

T group random sampling is carried out to obtain T group feature subspace. In the adjacent samples of the feature subspace of data x_i , the samples that exceeds the threshold of sample number (Threshold) are taken as the local space ψ_i of x_i in Eq. (2).

$$\psi_i = \{x_i | x_i \in X, x_i \in KNN_{ens}^{(i)}\} \quad (2)$$

The cardinality b of the local space of each data x_i is different, that is, the number of samples it contains is different.

3) Calculate the local anomaly score of data

After the local region of voltage data x_i is obtained, the base detection model is used to obtain the local anomaly score matrix $O(\psi_i) \in R^{b \times R}$ from $O(X) \in R^{n \times R}$. Assuming that the local region of x_i contains 10 data samples, and the anomaly scores of the data local region are calculated by the R base detection model, finally, a $10 \times R$ dimensional anomaly score matrix $O(\psi_i)$ is obtained.

4) Pseudo target

The maximum score of R base anomaly detector is taken as the pseudo target of the data sample in Eq. (3). The pseudo target of the data x_i is **target** (x_i) $\in R^{b \times 1}$.

$$\mathbf{target}(x_i) = f_{\max}(O(\psi_i)) \quad (3)$$

5) Choose base detection model

The Pearson Correlation Coefficient is calculated between the local anomaly score matrix $O(\psi_i)$ and the pseudo target, and we select the x base detection models that are most similar to the pseudo target through the correlation coefficient.

6) Anomaly score of data

According to the selected x base detection models, the anomaly score matrix $O(x_i)$ of the data x_i is calculated, and the average value of the x anomaly scores is used as the final anomaly score of the data x_i in Eq. (4).

$$s = f_{\text{avg}}(O(x_i)) \quad (4)$$

7) Judge outlier data

After obtaining the anomaly scores matrix $S \in R^{n \times 1}$ of all the data in the test dataset, the parameter of outlier data contamination (c) is used to control the number of outlier data in the test dataset in Eq. (5). The first Y data with high score in S is regarded as outlier data, and the user with voltage outlier data is considered as the user with the wrong UTR.

$$n \times c = Y \quad (5)$$

where n is the number of samples in the test dataset, Y is the number of outlier data in the test dataset.

Table 2 summarizes the adjustable parameters when the LSCP algorithm is used to identify the UTR.

Table 2: LSCP algorithm parameter description

Parameter symbol	Parameter description
c	Proportion of outlier data
K	Number of KNN nearest neighbor samples
T	Random sampling times
$Min_dimension$	A random sampling of the lowest dimension
$Max_dimension$	A random sampling of the highest dimension
$Threshold$	Threshold of sample number in feature subspace

The proportion of outlier data c is a key input parameter, which controls the number of users with wrong UTR. Other parameters are mainly related to the local space construction of the dataset, such as the number of KNN nearest neighbor samples (K), random sampling times (T), random sampling of the lowest dimension ($Min_dimension$), random sampling of the highest dimension ($Max_dimension$), and threshold of sample number in feature subspace ($Threshold$).

2.2 Selection of Base Outlier Detection Model for LSCP Algorithm

In this paper, the ensemble learning LSCP algorithm is combined with heterogeneous base outlier detection model, and four classical outlier detection algorithms are used as the base model. The choice of the base detection is Isolation Forest (I-Forest), One-Class Support Vector Machine (OC-SVM), Copula-Based Outlier Detection (COPOD), and Local Outlier Factor (LOF). The four base outlier data detection algorithms are used to detect different angles of data anomalies, promote the learning of different characteristics of the data, and improve the reliability and stability of the detection model.

The Isolation Forest algorithm realizes outlier detection of a dataset based on the idea of partition. The less the sample is divided, the more easily it is isolated, and the higher the anomaly degree of the sample is. The anomaly score of each data is shown in Eq. (6) [38].

$$s(x, n) = 2^{-\frac{E(h(x))}{c(n)}} \quad (6)$$

where $h(x)$ is the length of the path through which data x is divided; $E(h(x))$ is the expected path length of data x in a batch of isolated trees; and $c(n)$ is the average value of path length when the given data sample number is n .

OC-SVM is an outlier detection algorithm proposed for unbalanced samples. By mapping original data to high-dimensional space through kernel function, there are significant differences between normal data and abnormal data. A hyperplane is constructed to separate the two accordingly. The decision function to judge whether the data is abnormal is shown in Eq. (7) [39].

$$f(x) = \text{sgn}(\omega^T \phi(x) - \rho) \quad (7)$$

where ω is the normal vector of hyperplane; $\phi(\cdot)$ is the nonlinear mapping function; and ρ is the hyperplane intercept. If the output is 1, the data is normal; if the output is -1 , the data is abnormal.

COPOD realizes anomaly detection based on statistical methods. Aiming at the diversity of data distribution and the multidimensional data, it calculates the tail probability of each data point and calculates the skewness of distribution to correct the tail probability of data, so as to estimate the anomaly degree of data. The anomaly score of data x is shown in Eq. (8) [40].

$$s(x) = \max \{p_l, p_r, p_s\} \quad (8)$$

$$p_l = -\sum_{j=1}^d \log(\hat{U}_{j,i}) \quad (9)$$

$$p_r = -\sum_{j=1}^d \log(\hat{V}_{j,i}) \quad (10)$$

$$p_s = -\sum_{j=1}^d \log(\hat{W}_{j,i}) \quad (11)$$

where p_l, p_s is the left tail probabilities; p_r is the right tail probabilities; and $\hat{U}_{j,i}, \hat{V}_{j,i}, \hat{W}_{j,i}$ is the empirical copula observations.

LOF is based on the idea of density. It detects anomalies by comparing the density of each point with its neighboring points. Moreover, the LOF algorithm calculates the density through the k^{th} neighborhood of the point, without causing abnormal misjudgment due to different data density dispersion. The local outlier factor of x_i is shown in Eq. (12) [41].

$$LOF_k(x_i) = \frac{\sum \frac{Ird_k(x_j)}{Ird_k(x_i)}}{|N_k(x_i)|} \quad (12)$$

where $Ird_k(x)$ is the locally accessible density of data x ; and $N_k(x)$ is the k -distance neighborhood of data x .

3 Identification of Users-Transformer Relationship in the Station Area

The voltage data of users in different LVSA are different, showing different trends and characteristics, and the proportion of users with the wrong UTR is very small. Therefore, the problem of UTR identification can be defined as outlier data detection of unbalanced samples. To ensure the accuracy and reliability of the results, this paper adopts the LSCP algorithm with an ensemble framework to identify the relationship between users and the transformer in LVSA.

3.1 Selection and Processing of Algorithm Input Data

At present, the data in the user information collection system of the LVSA includes voltage, current, electricity consumption, and power. In this paper, voltage data is selected as the input of the LSCP algorithm, because the variation patterns of voltage data are not similar for users in different LVSA due to electrical distances and different outgoing lines [31]. The voltage curves of normal users (users with right UTR) and abnormal users (users with wrong UTR) in the LVSA are shown in Fig. 3.

As can be seen from Fig. 3, there are different trends between them. To highlight the difference, two-day voltage data of all users in the LVSA are selected as input dataset.

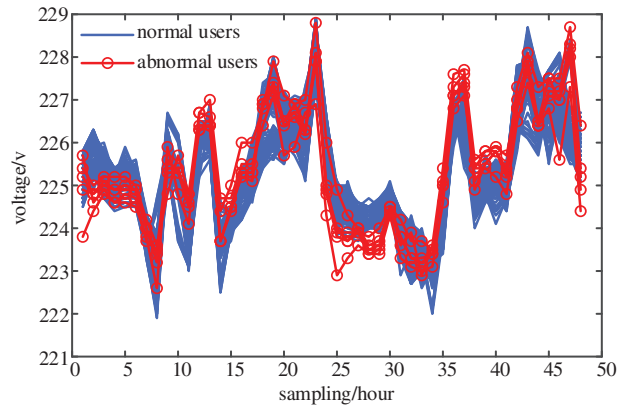


Figure 3: Voltage curve of users in the station area

Meanwhile, to highlight the difference in users' voltage data, this paper reconstructed voltage data based on the information entropy. Information entropy refers to the degree of ordering or complexity of voltage data at different times. When the information entropy of voltage data at a certain time is large, it indicates that the voltage data of the user at that time is greatly different from that of other users. The user's voltage data Y can be expressed as:

$$Y = \begin{bmatrix} y_{11} & y_{12} & \cdots & y_{1N} \\ y_{21} & y_{22} & \cdots & y_{2N} \\ \vdots & \vdots & \cdots & \vdots \\ y_{M1} & y_{M1} & \cdots & y_{MN} \end{bmatrix} \quad (13)$$

where, M is the number of users; N is the number of voltage data samples; and y_{mn} is the voltage of the m^{th} user at time n^{th} .

Voltage information entropy at different moments can be defined as follows [42]:

$$\Delta y_{mm} = \frac{y_{mm} - \max(y_n)}{\min(y_n) - \max(y_n)} \quad i = 1, 2, \dots, m \quad (14)$$

$$H_n = -\lg \left(M \sum_{m=1}^M \Delta y_{mm} \lg(\Delta y_{mm}) \right) \quad (15)$$

where the column vector y_n represents the voltage vectors of all users at the n^{th} moment; Δy_{mm} is the voltage at the n^{th} moment of the m^{th} user after normalization; and H_n is the voltage information entropy at the n^{th} moment.

Based on the information entropy of voltage data, the voltage data reconstruction coefficient is calculated, as shown in Eq. (16). And the original voltage data Y is reconstructed to obtain the matrix Y' , as shown in Eq. (17).

$$\alpha_m = \frac{H_m}{\sum_{m=1}^M H_m} \quad (16)$$

$$Y' = [\alpha_1 y_1, \alpha_2 y_2, \dots, \alpha_N y_N] \quad (17)$$

where α_j is the reconstruction coefficient obtained according to information entropy.

3.2 Determine the Key Input Parameter of the LSCP Algorithm

Based on the LSCP algorithm, the principle of the identification method of the UTR is as follows: input the voltage data reconstructed by information entropy of all users in the LVSA, use the LSCP algorithm to accurately detect the abnormal trend of the voltage data, judge the abnormal degree of the voltage data, and get the abnormal score of the voltage data of each user. The individual user with the highest data anomaly score is regarded as the user with wrong UTR, and the output is 1. Other users are regarded as normal users, and the output is 0. Among the input parameters of the LSCP algorithm, the proportion of outlier data is a key input parameter, which controls the number of users with the wrong UTR. In the UTR identification, the proportion of users with the wrong UTR is unknown. If the proportion of outlier data is set to a fixed value, the accuracy and efficiency of calculation results will be affected. This paper tries to optimize the key input parameters selection of the LSCP algorithm from the perspective of line loss rate, to avoid artificially setting parameters affecting the identification results and improve the practicability of the proposed method. The procedure for determining the key input parameter is as follows:

1. Input different proportions of outlier data values. The LSCP algorithm is used to get the serial number of users with wrong UTR. In this paper, the proportion of outlier data is in the interval $[0, 0.10]$, and the value is traversed every 0.01. This is because the number of users in LVSA in this paper is about 100. When the interval is 0.01, the number of users with wrong UTR output each time increases by about 1. If 0.005 is selected, the amount of calculation will increase; if 0.02 is used, the parameter changes are too large, and it is difficult to find the optimal parameter.
2. The sum of electricity consumption of users with the right UTR is selected to calculate the line loss rate of the LVSA.
3. Considering the LVSA existing line loss, the minimum line loss rate threshold should be set according to the historical line loss record of the system or the actual LVSA characteristics.
4. If the line loss rate calculated according to different input parameters is lower than the minimum line loss threshold, it is considered that an error occurs in the UTR. When the outlier data proportion of input data is increased, the number of users with wrong UTR in output will increase. The users with right UTR may be misjudged as abnormal users, which will further reduce the total power consumption of users in the LVSA and increase the line loss rate. Therefore, on the basis of the minimum line loss threshold, the input value corresponding to the minimum line loss rate is selected as the optimal parameter with flowchart shown in [Fig. 4](#).

3.3 The Realization Process of Users-Transformer Relationship Identification

The specific implementation steps of the UTR identification method based on the proposed method are as follows:

- 1) Data processing

Filter out and collect complete data from the user information collection system, including 2 days' voltage data and 10 days' daily electricity consumption data. Meanwhile, voltage data is reconstructed based on information entropy.

2) Determine the outlier data proportion c

The input parameter outlier data contamination c is traversed every 0.01 in the interval $[0, 0.10]$. The LSCP algorithm is used to obtain the users with wrong UTR. The line loss rate of the LVSA is calculated and the best input parameter is determined.

3) Users-transformer relationship identification

Input the best parameter, use the LSCP algorithm to identify the UTR, and obtain users with wrong UTR in the LVSA.

4) On-site verification

The staff verifies the users with abnormal UTR on-site and updates the system's UTR files on time.

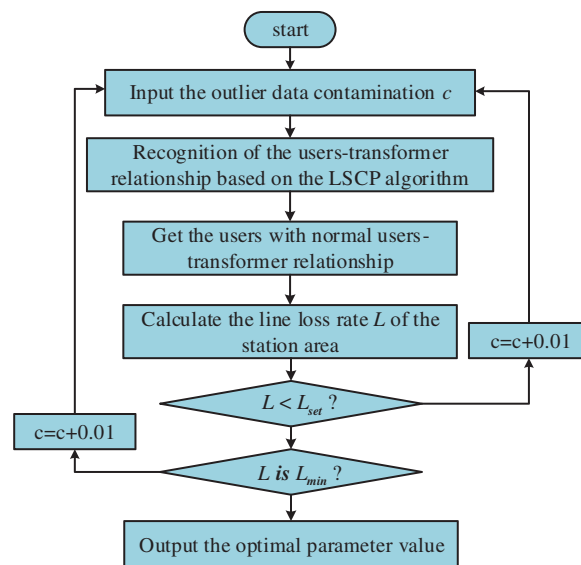


Figure 4: Flowchart of determining the key input parameter

4 Experiment

The electricity consumption and voltage data of Nanjing, Jiangsu Province in April 2020 is selected as the dataset. The voltage data is used to identify the relationship between transformer and user, and the electricity consumption data is used to determine the optimal input parameter of the algorithm. Experiments are carried out in the actual LVSA to verify the effectiveness and applicability of the proposed method. The structure diagram of the LVSA is shown in Fig. 5. The LVSA 1 has 107 single-phase residential users. The LVSA 2 has 89 single-phase residential users. The LVSA 3 has 143 single-phase residential users.

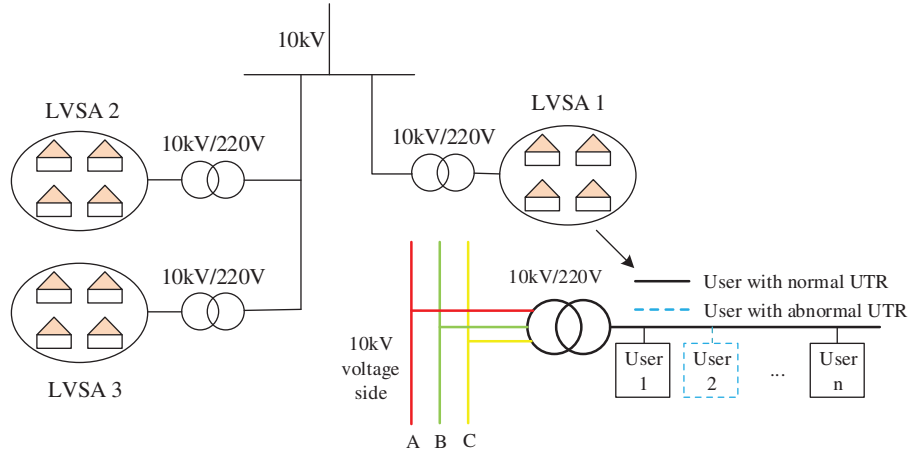


Figure 5: Structure diagram of the LVSA

Three simulation scenarios are set to verify the proposed UTR identification method. Simulation scenario 1: There are 107 users in LVSA 1. 5 users are randomly selected from LVSA 2 and placed in LVSA 1 as users with wrong UTR. Simulation scenario 2: There are 89 users in LVSA 2, and 3 users are randomly selected from LVSA 1 and LVSA 3 respectively as users with wrong UTR. Simulation scenario 3: There are 7 LVSA in total. 5 users from one LVSA are randomly selected and assigned to the other 6 LVSA as users with wrong UTR. In this paper, recall and precision are used to evaluate the effect of the method. The calculation of the two indexes is shown in Eqs. (18) and (19).

$$\text{Recall}\% = \frac{A_u - M_u}{A_u} \times 100\% \quad (18)$$

$$\text{Precision}\% = \frac{N - W_u}{N} \times 100\% \quad (19)$$

where A_u is the actual number of users with abnormal UTR; M_u is the number of missed users with abnormal UTR; N is total number of users in the LVSA; W_u is the number of users whose UTR is incorrectly identified.

4.1 Determine the Key Input Parameter of the Algorithm

The State Grid Corporation of China defines the abnormal line loss LVSA as that lasts over 10 days. In Simulation scenario 1, the average power consumption of users in the LVSA in 10 days is used to calculate the line loss rate and determine the proportion of outlier data. Input parameters are taken at 0.01 intervals in $[0, 0.10]$, and traversal calculation is carried out to obtain the UTR membership and LVSA line loss rate of each calculation. The LVSA line loss rate is shown in Table 3.

Due to limited space, only the calculation results of parameters in the interval $[0.02, 0.06]$ are listed in Table 3. In this paper, the minimum threshold of line loss rate is set as 2%. In practical application, the minimum threshold can be modified according to the historical line loss value and the actual LVSA characteristics. As can be seen from Table 3, based on the specified minimum line loss rate, when the input parameter value is 0.04, the calculated line loss rate is the smallest. Therefore, 0.04 is selected as the best input parameter.

Table 3: Process of determining key parameters

Proportion of outlier data/ c	ID of abnormal user	Line loss rate/%	Optimum parameter
0.02	108,109,112	1.05%	no
0.03	108,109,110,112	1.39%	no
0.04	108,109,110,111,112	2.25%	yes
0.05	56,108,109,110,111,112	2.45%	no
0.06	56,98,108,109,110,111,112	5.02%	no

4.2 Example Analysis of Users-Transformer Relationship Identification Based on the LSCP Algorithm

Simulation scenarios 1 and 2 are used to verify the applicability and effectiveness of the identification method of the users-transformer relationship in the station area based on the LSCP algorithm. According to the calculation rules in Section 4.1, the optimal input parameter of the algorithm in simulated scenarios 1 and 2 are 0.04 and 0.06, respectively. The LSCP algorithm selects I-Forest, OC-SVM, COPOD, and LOF as its base outlier detection models, and sets the number of nearest neighbors of the LOF algorithm as 10, 14, 18, and 22 to form a group of heterogeneous base models. Parameter Settings of the LSCP algorithm are shown in Table 4. Input dataset is two-day reconstructed voltage data based on information entropy with the collection frequency 1 h/time and a total of 48 points.

Table 4: Parameter settings of LSCP algorithm in simulation scenario

Parameter symbol	Parameter value
K	30
T	20
$Min_features$	24
$Max_features$	48
$Threshold$	15

In practice, due to the close electrical distance between LVSA, the voltage similarity of users in different LVSA is very high. In simulated scenarios 1 and 2, the Pearson correlation coefficient method is used to measure the voltage data similarity index between the users with normal UTR and users with abnormal UTR in the LVSA. The mean value of the correlation coefficient is shown in Fig. 6.

As is seen from Fig. 6, in simulated scenario 2, the voltage data similarity between users in LVSA 2 and LVSA 3 is the highest, reaching above 0.9 because their electrical distance is relatively close. In the simulation scenario with high voltage similarity, the method presented in the paper is used to identify the UTR. The calculation results are shown in Table 5, and the anomaly scores of users' voltage data in the LVSA is shown in Fig. 7.

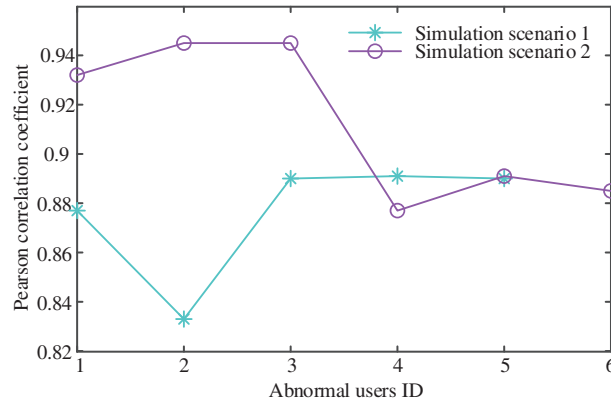


Figure 6: Voltage data correlation coefficient average value

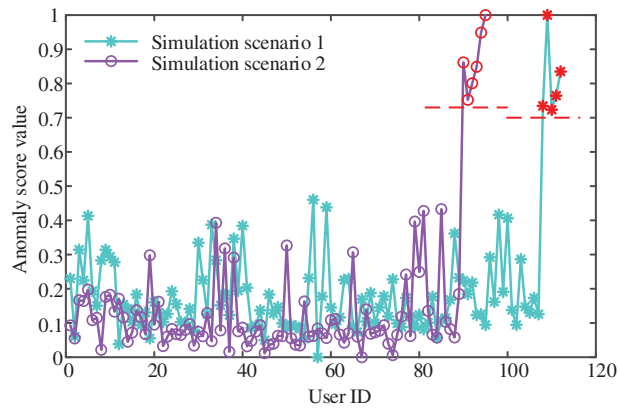


Figure 7: Anomaly scores of users' voltage data in LVSA

Table 5: Identification results of the proposed method in the paper

Simulation scenario	ID of abnormal user	Recall ratio/%	Precision/%
Simulation scenario 1	108, 109, 110, 111, 112	100%	100%
Simulation scenario 2	90, 91, 92, 93, 94, 95	100%	100%

In [Table 5](#), both recall and precision rates in the simulated scenario are 100%. In [Fig. 7](#), the anomaly scores of voltage data of users in the LVSA are very different, which is conducive to the identification of users with wrong UTR. In view of the high similarity of voltage data, the method based on the LSCP algorithm is more sensitive to the local difference of voltage curves between normal and abnormal users by constructing the local feature space of data samples. Meanwhile, different outlier detection algorithms based on different principles are used as the base detector, which further ensures the high accuracy and reliability of the identification result.

To further illustrate the superiority of the method proposed in this paper in solving the UTR identification problem in LVSA, it is compared with the single outlier detection algorithm. The comparison results are shown in [Table 6](#).

Table 6: Comparison of results of various methods

Method	Recall ratio/%	Precision%	ID of abnormal users
Isolation Forest	100%	93.75%	8,34,56,59,96,98,100, 108,109,110,111,112
One-Class Support Vector Machine	100%	93.75%	5,9,34,56,59,98,100, 108,109,110,111,112
Copula-Based Outlier Detection	100%	93.75%	3,8,10,34,56,96,100, 108,109,110,111,112
Local Outlier Factor	100%	93.75%	30,33,38,40,88,98,103, 108,109,110,111,112
The proposed method	100%	100%	108,109,110,111,112

According to the test results in [Table 6](#), general identification methods can cause misjudgment of UTR with the accuracy rate of 93.75% and varied users of wrong UTR. It is also noted that general identification methods detect outlier data from a single angle and do not optimize the input parameter of the algorithm, resulting in poor accuracy and stability. The recall and precision of the proposed method are both 100%, and the input parameter of the algorithm can adapt to the characteristics of the actual station area.

At the same time, to verify the universality and reliability of the proposed method, under simulated scenario 3, the voltage data of two days is used to identify the UTR of six LVSA. The test results are shown in [Table 7](#).

Table 7: Test results under simulation scenario 3

LVSA	Number of actual users	Recall ratio/%	Precision/%
LVSA 1	143	100%	100%
LVSA 2	116	100%	100%
LVSA 3	124	100%	100%
LVSA 4	156	80%	98.71%
LVSA 5	87	100%	100%
LVSA 6	134	100%	100%

In [Table 7](#), the recall rate of the LVSA 4 is 80% and the precision rate is 98.71%, missing one user with wrong UTR. The recall rate and precision rate of the other five LVSA are 100%. However, for the LVSA 4, the recall rate and precision rate can still reach 100% if voltage data of more than 2 days is used for calculation. In practical application, for higher accuracy and reliability, voltage data of more than 2 days can be used for calculation when the voltage data of the station area is sufficient. Therefore, the method proposed in this paper has high accuracy and applicability in the identification of the UTR in LVSA.

4.3 The Practical Analysis of this Method in Application

The influence of the voltage data of different days and the error of voltage data in transmission on the identification result are considered to verify the method in the practical application.

4.3.1 The Influence of Voltage Data in Different Days on the Result

In simulated scenario 1, voltage data of different days are taken as input data to identify the relationship between users and the transformer and to verify the influence of voltage data of different days on the identification result, as shown in [Table 8](#).

Table 8: Influence of voltage data of different days on identification of the users-transformer relationship

Number of days to enter the voltage data/day	Recall ratio/%	Precision/%
1	60%	98%
2	100%	100%
3	100%	100%
4	100%	100%
5	100%	100%

It can be seen from [Table 8](#) that the proposed method can accurately identify the UTR by using two-day voltage data. It is also applicable to the LVSA with poor collection function and difficulties in obtaining multi-day complete voltage data, which shows that the proposed algorithm is not too dependent on data. It improves the applicability and reduces the calculation cost.

4.3.2 The Influence of Random Error of Voltage Data Measurement on the Result

Considering the existence of random errors in the measurement and transmission of electricity data, the influence of the errors on the identification results of the proposed method is verified. In simulation scenario 1, the measured voltage data for 30 days in April in the LVSA (the actual measured voltage data contains random measurement errors) is selected, and the two-day data was divided into 1 group. The average test results of 15 groups of data are shown in [Table 9](#).

Table 9: Average test results of 15 groups of data

Simulation scenario	Number of total users	Number of abnormal users	Average recall ratio/%	Average precision/%
Simulation scenario 1	112	5	98.66%	99.88%

When testing 15 groups of data, only the third group has a recall rate of 80% and a precision rate of 98.21%, while the other groups have a recall rate and precision rate of 100%. The average recall rate is 98.66% and the average precision rate is 99.88%. Therefore, the random error in voltage measurement has no influence on the accuracy of the algorithm identification results, which further demonstrates the practicability and anti-interference of the proposed method.

5 Conclusions

This paper proposes an ensemble learning LSCP algorithm to identify the relationship between users and the transformer, which provides a new idea for solving the UTR correction. The proposed method contributes to the lean management of the LVSA, which is of great significance to the economic operation of the LVDN. The effectiveness of the proposed method is verified in the three

designed simulation scenarios. It is concluded that the LSCP algorithm of the ensemble framework is used to build an identification model for the UTR, which improves the accuracy and reliability of identification results. The recall and precision rate of this method can reach 100%. The proposed method can make use of two-day voltage data to identify the UTR accurately and avoid the dependence on data, which is applicable to the LVSA where data acquisition is difficult while reducing the cost of calculation. In the case of high voltage similarity of users in different LVSA, the method presented in this paper can still achieve accurate identification and meet the requirements of practical application. In this paper, the optimal key input parameter of the algorithm is determined automatically by the line loss rate index, which can adapt to the characteristics of different LVSA actively and improve the practicability. The shortcoming of the proposed method is that it can merely find there are users with wrong UTR in LVSA, without automatically determining which LVSA the user belongs to. In the future, we can study how to achieve UTR identification based on voltage characteristics when photovoltaic and other renewable power generation are connected to the LVSA.

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References

1. Jiang, Y. C., Liu, C. C., Diedesch, M., Lee, E., Srivastava, A. K. (2016). Outage management of distribution systems incorporating information from smart meters. *IEEE Transactions on Power Systems*, 31(5), 4144–4154. DOI 10.1109/TPWRS.2015.2503341.
2. Li, P., Yan, Y. H., Xu, M. Z., Liu, F., Wang, J. R. et al. (2019). The research of users-transformer relationship verification method based on data-driven. *2019 IEEE Innovative Smart Grid Technologies—Asia (ISGT Asia)*, pp. 2550–2554. Chengdu, China. DOI 10.1109/ISGT-Asia.2019.8881160.
3. Luan, W. P., Peng, J., Maras, M., Lo, J., Harapnuk, B. (2015). Smart meter data analytics for distribution network connectivity verification. *IEEE Transactions on Smart Grid*, 6(4), 1964–1971. DOI 10.1109/TSG.2015.2421304.
4. Yu, J. F., Weng, Y., Rajagopal, R. (2019). PaToPaEM: A data-driven parameter and topology joint estimation framework for time-varying system in distribution grids. *IEEE Transactions on Power Systems*, 34(3), 1682–1692. DOI 10.1109/TPWRS.2018.2888619.
5. Shi, C. K., Zhang, B., Sheng, W. X., Zhou, M., Gao, Y. et al. (2016). Discussion on functional architecture for distribution network operation and maintenance management platform. *Power System Technology*, 40(7), 2206–2211.
6. Pappu, S. J., Bhatt, N., Pasumarthy, R., Rajeswaran, A. (2018). Identifying topology of low voltage distribution networks based on smart meter data. *IEEE Transactions on Smart Grid*, 9(5), 5113–5122. DOI 10.1109/TSG.2017.2680542.
7. Zheng, M. C. (2014). Application of instantaneous power failure method in the investigation of household relationship change in area. *Guide to Business*, 23, 193.

8. Ying, J., Chen, Y. L., Ji, W. L., Liu, M. X., You, Y. et al. (2019). Topology modeling method for distribution network via power line communication. *2019 IEEE Innovative Smart Grid Technologies—Asia (ISGT Asia)*, pp. 323–327. Chengdu, China. DOI 10.1109/ISGT-Asia.2019.888174.
9. Lisowski, M., Masnicki, R., Mindykowski, J. (2019). PLC-enabled low voltage distribution network topology monitoring. *IEEE Transactions on Smart Grid*, *10(6)*, 6436–6448. DOI 10.1109/TSG.2019.2904681.
10. Matthew, L., Matthew, J. R., Jouni, P. (2019). Distribution system parameter and topology estimation applied to resolve low-voltage circuits on three real distribution feeders. *IEEE Transactions on Sustainable Energy*, *10(3)*, 1585–1592. DOI 10.1109/TSTE.2019.2917679.
11. Cunha, V. C., Freitas, W., Trindade, F. C. L., Santoso, S. (2020). Automated determination of topology and line parameters in low voltage systems using smart meters measurements. *IEEE Transactions on Smart Grid*, *11(6)*, 5028–5038. DOI 10.1109/TSG.2020.3004096.
12. Ma, L., Wang, L. F., Liu, Z. X. (2022). Topology identification of distribution networks using a split-EM based data-driven approach. *IEEE Transactions on Power Systems*, *37(3)*, 2019–2031. DOI 10.1109/TPWRS.2021.3119649.
13. Zhao, J. M., Cai, Y. Z., Guo, W. C., Li, J. (2021). User-transformer relationship verification method of low voltage distribution network based on voltage correlation analysis. *2021 IEEE International Conference on Electronic Technology, Communication and Information (ICETCI)*, pp. 163–166. Changchun, China. DOI 10.1109/ICETCI53161.2021.9563352.
14. Blakely, L., Reno, M. J. (2021). Identification and correction of errors in pairing AMI meters and transformers. *2021 IEEE Power and Energy Conference at Illinois (PECI)*, pp. 1–8. Urbana, United States. DOI 10.1109/PECI51586.2021.9435274.
15. Xiao, Y., Zhao, Y., Tu, Z. D., Dian, B., Chang, R. M. (2019). Topology checking method for low voltage distribution network based on improved pearson correlation coefficient. *Power System Protection and Control*, *47(11)*, 37–43.
16. Zhang, M. Z., Luan, W. P., Guo, S., Wang, P. (2018). Topology identification method of distribution network based on smart meter measurements. *2018 China International Conference on Electricity Distribution*, pp. 372–376. Tianjin, China. DOI 10.1109/CICED.2018.8592228.
17. Tang, D. L., Ni, P. B., Zhang, J., Liu, Y. B., Li, Y. et al. (2021). Identification method for relationship between household transformers based on Discrete Frechet Distance. *Automation of Electric Power Systems*, *45(6)*, 223–230.
18. Liu, L. N., Li, F. S., Zhou, Y. F., Cheng, Z. J., Qu, M. et al. (2021). An identification algorithm of low voltage user-transformer relationship based on improved spectral clustering. *2021 IEEE 2nd China International Youth Conference on Electrical Engineering (CIYCEE)*, pp. 1–5. Chengdu, China. DOI 10.1109/CIYCEE53554.2021.9676868.
19. Cui, X. Y., Liu, S. Y., Jin, W. C., Lin, Z. Z., Xuan, Y. H. et al. (2021). Consumer-transformer relationship and phase identification based on APAA and improved DBSCAN algorithm. *Power System Technology*, *45(8)*, 3034–3043.
20. Hu, W., Guo, Q. H., Wang, W., Wang, W. H., Song, S. H. (2021). Research on user–transformer relationship based on improved dynamic time warping algorithm. *2021 IEEE 5th Conference on Energy Internet and Energy System Integration (EI2)*, pp. 485–489. Taiyuan, China. DOI 10.1109/EI252483.2021.9713261.
21. Liu, S., Huang, C., Li, K. M., Hou, S. S. (2022). Identification method for household-transformer relationship based on derivative dynamic time warping distance and density-based spatial clustering of application with noise algorithm. *Automation of Electric Power Systems*, *45(18)*, 71–77.
22. Li, K. M., Jiang, Y. Q., Huang, S. F., Li, J. Q., Yang, M. S. (2021). Topology identification method of a low-voltage distribution station area based on DTW distance and cluster analysis. *Power System Protection and Control*, *49(14)*, 29–36.

23. Guo, S., Lin, J. Y., Wang, P., Zhang, J. C., Chen, L. et al. (2020). Topology verification of low voltage distribution network based on ROF outliers detection algorithm. *Control Engineering of China*, 27(1), 201–206.
24. Feng, Z. Y., Shen, J., Wang, D. Y., Liu, Y., Wen, G. P. (2020). Transformer area topology verification method based on sparse adaptive learning. *Electrical Measurement & Instrumentation*, 57(7), 29–34.
25. Li, P., Wu, W. J., Yan, Y. H., Xu, B., Liu, F. et al. (2020). Research on the method of transformer-meter relationship verification based on data-driven. *Power Demand Side Management*, 22(1), 64–68.
26. Deng, W., Zhu, J. R., Tang, H. G., Hu, W., Liu, Y. et al. (2021). Users-transformer relationship identification based on smart meter data. *2021 China International Conference on Electricity Distribution (CICED)*, pp. 1040–1044. Shanghai, China. DOI 10.1109/CICED50259.2021.9556773.
27. Farajollahi, M., Shahsavari, A., Mohsenian-Rad, H. (2020). Topology identification in distribution systems using line current sensors: An MILP approach. *IEEE Transactions on Smart Grid*, 11(2), 1159–1170. DOI 10.1109/TSG.2019.2933006.
28. Hu, W., Liu, Y., Guo, Q. T., Wang, J., Wang, Y. L. et al. (2020). Detection of users-transformer relationship in the secondary power distribution system with smart meter data. *2020 15th IEEE Conference on Industrial Electronics and Applications (ICIEA)*, pp. 449–454. Kristiansand, Norway. DOI 10.1109/ICIEA48937.2020.9248159.
29. Zhou, L., Wen, F. J., Yang, X. F., Zhong, Y. M. (2022). User-transformer connectivity relationship identification based on knowledge-driven approaches. *IEEE Access*, 10, 54358–54371. DOI 10.1109/ACCESS.2022.3175841.
30. Gao, Z. P., Zhao, Y., Yu, Y. L., Luo, Y. J., Xu, Z. W. et al. (2020). Low-voltage distribution network topology identification method based on knowledge graph. *Power System Protection and Control*, 48(2), 34–43.
31. Tang, J., Cai, Y. Z., Zhou, L., Yi, Y. Q., Chen, G. P. et al. (2020). Data-driven based identification method of feeder-consumer connectivity in low-voltage distribution network. *Automation of Electric Power Systems*, 44(1), 127–134.
32. Zimek, A., Campello, R., Sander, J. (2014). Ensembles for unsupervised outlier detection: Challenges and research questions a position paper. *ACM SIGKDD Explorations Newsletter*, 15(1), 11–22. DOI 10.1145/2594473.2594476.
33. Yao, R., Li, J., Hui, M., Bai, L. (2022). Pattern recognition for partial discharge using adaptive boost classification model based on ensemble method. *Power System Technology*, 46(6), 2410–2420.
34. Khan, I. U., Javeid, N., Taylor, C. J., Gamage, K. A. A., Ma, X. D. (2022). A stacked machine and deep learning-based approach for analysing electricity theft in smart grids. *IEEE Transactions on Smart Grid*, 13(2), 1633–1644. DOI 10.1109/TSG.2021.3134018.
35. Wang, F., Gao, X., Jia, X., Ren, B., Zha, S. (2021). An anomaly detection ensemble algorithm for power dispatching data based on log-interval isolation. *Power System Technology*, 45(12), 4818–4827.
36. Xu, X., Zhao, H. B., Liu, H. Q., Sun, H. (2020). LSTM-GAN-XGBOOST based anomaly detection algorithm for time series data. *2020 11th International Conference on Prognostics and System Health Management (PHM-2020 Jinan)*, pp. 334–339. Jinan, China. DOI 10.1109/PHM-Jinan48558.2020.00066.
37. Zhao, Y., Nasrullah, Z., Hryniewicki, M. K., Li, Z. (2019). LSCP: Locally selective combination in parallel outlier ensembles. *Proceedings of the 2019 SIAM International Conference on Data Mining*, pp. 585–593. Calgary, Alberta, Canada. DOI 10.1137/1.9781611975673.66.
38. Li, X. P., Gao, X., Yan, B., Chen, C. X., Chen, B. et al. (2019). An approach of data anomaly detection in power dispatching streaming data based on isolation forest algorithm. *Power System Technology*, 43(4), 1447–1456.
39. Scholkopf, B., Platt, J. C., Shawe-Taylor, J., Smola, A. J., Williamson, R. C. (2001). Estimating the support of a high-dimensional distribution. *Neural Computation*, 13(7), 1443–1471. DOI 10.1162/089976601750264965.

40. Li, Z., Zhao, Y., Botta, N., Ionescu, C., Hu, X. et al. (2020). COPOD: Copula-based outlier detection. *The 20th IEEE International Conference on Data Mining*, pp. 1118–1123. Sorrento, Italy. DOI 10.1109/ICDM50108.2020.00135.
41. Zhao, Q. Z., Li, Y., Tian, S. M., Dong, Y. L., Tan, Y. et al. (2016). A state estimation and fault processing method based on big data analysis of smart distribution network. *Power System Technology*, 40(3), 774–780.
42. Yan, Y. L., Li, J., Li, H., Sun, P., Zhang, X. M. (2015). A wind turbine anomaly detection method based on information entropy and combination model. *Power System Technology*, 39(3), 737–743.