

# Intelligent Color Reasoning of IOT Based on P-laws

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**Abstract:** Aiming at the dynamics and uncertainties of natural colors affected by the natural environment, a color  $P$ -law generation model based on the natural environment is proposed to develop algorithms and to provide a theoretical basis for plant dynamic color simulation and color sensor data transmission. Based on the HSL (Hue, Saturation, Lightness) color solid, the proposed method uses the function  $P$ -set to provide a color  $P$ -law generation model and an algorithm of the Dynamic Colors System (DCS), establishing the DCS modeling theory of the natural environment and the color  $P$ -reasoning simulation based on the HSL color solid. The experimental results show that based on the color  $P$ -law, for the DCS of the natural environment, when the external factors change, the color of the plant changes, accordingly, verifying the effectiveness of the color  $P$ -law generation model and the algorithm of the DCS. In the dynamic color intelligent simulation system, when external factors change, the dynamic change of plant color generally conforms to the basic laws of the natural environment. This enables the effective extraction of color data from the Internet of Things (IoT)-based color sensors and provides an effective way to significantly reduce the data transmission bandwidth of the IoT network.

**Keywords:** Natural environment; function  $P$ -sets; color  $P$ -law; intelligent color; reasoning simulation

## 1 Introduction

Color is the outcome of a visual perception of light reflected by objects on the human brain and visual organs. Color comes from nature. Due to the natural factors of color, color has an important influence on people's mental state or mood. The most beautiful and harmonious color matching comes from nature. The color matching information extracted from the natural landscape has its unique vitality and beauty. This information facilitates color sensors based on the Internet of Things (IoT) to understand how to rapidly optimize the settings of color parameters and apply them to products and systems [1–3]. One leaf knows autumn (from the fall of a leaf, we know the arrival of autumn). We can explore the variation law of the natural color of a certain type of plant from the color variation of this type of plant. With the changing of the four seasons, plants will show different colors as the seasons change. Each type of plant



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has its own life. From the birth of plants to vibrant colors, and to gradual decay, plants are telling its story. The color variation of plants shows the color flow of nature in the four seasons.

Currently the most widely used color standards are: 1) Munsell color system established by the National Bureau of Standards (NBS) ; 2) the Natural Color System (NCS) is the Swedish national color standard; 3) German RAL color system; 4) CIE-XYZ (Commission Internationale de L' Eclairage-XYZ); 5) RGB color stereo; 6) Adobe RGB color solid; 6) other color solid: such as HSI (Hue, Saturation, Intensity) cylindrical color solid, HSI spherical color solid, Lab color solid [4]. The basis of color digitization is to create a three-dimensional digital model of color. In this paper, it's called color solid, which is a three-dimensional representation of color space, being an analog the two-dimensional representation of the color wheel. The added spatial dimension allows a color solid to depict an additional dimension of color variation.

This paper sets the color defined by the  $(H, S, L)$  value in the HSL space, where  $0^{\circ} \leq H < 360^{\circ}$ ,  $0 \leq S, L \leq 1$ . While  $(R, G, B)$  in RGB space, where  $0 \leq R, G, B \leq 1$ .

Color digitization is to obtain hue (red, green, blue, etc.), lightness (light and shade), and saturation (or chroma) from the natural color through the color sensor, which makes a color solid can show all possible colors in the three-dimensional structure.

In the natural environment, the color of plants is mostly affected by changes in environmental factors. Genetic factors of plants are the internal cause of plant color formation, whereas plant photosynthesis, water metabolism, mineral metabolism and other processes are often affected by light, temperature, humidity, and other external factors, causing changes in the proportion of various pigments in plants, resulting in the manifestation of different colors [5–7].

In recent years, color digital simulation based on a natural environment has been applied in the IoT devices. The proposed approaches of color digital simulation are mainly divided into 1) the texture model based on optical characteristics and the time-varying model based on physical authenticity [8–13]; 2) Algorithm based on environmental factors [14–19]; 3) the research on simulation algorithms in large scenarios, etc. [20].

The study [14,18] which apply the Markov chain algorithm takes the external environment and seasonal factors of plants into consideration, and the simulation effect has strong physical authenticity. However, the simulation is static, and the color effect is also static color simulation, which cannot be changed in real-time with changes in external environmental factors such as temperature and light. Nevertheless, in practice, the data collected in real scenes is uncertain and large, causing difficulty in smoothly transmitting in the network formed by the IoT devices.

This naturally raises a question. In the natural environment, can we study the regularity of external uncertain factors such as light intensity, temperature, and humidity that affect the color of plants, and obtain the color variation law of plants through reasoning?

This paper analyzes the influence of external uncertain factors on the color of plants and uses the function  $P$ -set [21] to propose a color reasoning algorithm based on the  $P$ -law in a natural environment. When external factors change, the color of plants also changes accordingly. Then, the changed results are recorded by IoT sensors to achieve the optimization of plant color parameter settings through reasoning. To model the dynamic color system of plants based on the natural environment, it aims to develop an algorithm and provide a theoretical basis for the dynamic simulation of natural color of plants for the IoT devices.

## 2 The Color $P$ -law of the Dynamic Color System

If the color variation process is abstracted into a Dynamic Colors System which is called  $D$ . Apparently since the Dynamic Color System  $D$  is affected or interfered by some dynamic and uncertain external factors

in the natural environment. These factors are all in the set  $\alpha$  which includes illuminance, temperature, and humidity etc. The existence of these factors results in the uncertainty of the Dynamic Colors System  $D$ . More specifically, the factors in the natural/environment cause the color variation law of  $D$  to be dynamic and uncertain. This process can be abstracted as follow:

The color variation law set of a Dynamic Colors System  $D$  is  $U(x)$ , which we call the Universe of Color law having  $U(x) = \{u_0(x), u_1(x), \dots, u_{m-1}(x)\}$ . The attribute set of color factors  $\alpha = \{\alpha_0, \alpha_1, \dots, \alpha_{n-1}\}$  is affected by the external factor set  $(F, \bar{F})$ , or  $\alpha$  is interfered by  $(F, \bar{F})$  to become  $\alpha^F \alpha^{\bar{F}}$ , then the color law sets  $S$  becomes  $(S^{\bar{F}}, S^F)$ , that is, the  $(F, \bar{F})$ - interference of the attribute set  $\alpha$  of  $S$  leads to the generation of the color law sets  $(S^{\bar{F}}, S^F)$ .

In fact, if the relationship and characteristics between the distribution law of  $D$ 's external factor change and  $D$ 's color distribution law can be obtained, the color variation law of  $D$  can also be obtained by reasoning.

Function  $P$ -sets (Function Packet Sets) is a new mathematical structure, which has dynamic and uncertainty. It has achieved promising results in the application of dynamic system law mining, dynamic law discovery and Pattern dynamic recognition [14,16–18,20–28]. Function  $P$ -sets have dynamic characteristics and law characteristics, which is suitable for solving the problem of uncertain law with a dynamic system.

This paper utilizes approaches provided by the literature [4,21,29,30] to present the concept of the color  $P$ -law, the generation color  $P$ -law and the color  $P$ -reasoning of Dynamic Colors System  $D$ . We present a Dynamic Color System  $D$  in a natural environment, an intelligent color reasoning algorithm based on the  $P$ -law, aiming to provide a theoretical basis for the dynamic color processing of the IoT sensors in the natural environment.

### 2.1 The Color $P$ -law

**Convention:** Let  $U(x)$  be a color law (function) finite domain and  $V(\alpha)$  is the finite attribute domain of  $U(x)$ .  $S(x) = \{s_0(x), s_1(x), \dots, s_{m-1}(x)\}$  is the finite color law sets of  $U(x)$ .  $U(x), V(\alpha), S(x), s_i(x)$  are abbreviated as  $U, V, S, s_i$ , respectively. The features of law migration family  $F = \{f_0, f_1, \dots, f_{n-1}\}$ ,  $\bar{F} = \{\bar{f}_0, \bar{f}_1, \dots, \bar{f}_{n-1}\}$  is:

$$\exists r_i \in U - S, f \in F \Rightarrow f(r_i) = s'_i \in S \tag{1}$$

$$\exists s_j \in S, \bar{f} \in \bar{F} \Rightarrow f(s_j) = r_j \in U - S. \tag{2}$$

**Definition 1.** Given the color law set  $S = \{s_0, s_1, \dots, s_{k-1}\} \subset U, \alpha = \{\alpha_0, \alpha_1, \dots, \alpha_{n-1}\} \subset V$  is the attribute set of  $S$ , called  $S^{\bar{F}}$ , which is the color  $P$ -internal law set generated by  $S$  and

$$S^{\bar{F}} = S - S^- \tag{3}$$

where  $S^-$  is called the color  $\bar{F}$ - law deleted set of  $S$  and

$$S^- = \{r_i | s_i \in S, \bar{f}(s_i) = r_i \notin S, \bar{f} \in \bar{F}\} \tag{4}$$

if the attribute set of  $S^{\bar{F}}$ , called  $\alpha^{\bar{F}}$ , satisfies

$$\alpha^{\bar{F}} = \alpha \cup \{\alpha'_i | f(\beta_i) = \alpha'_i \in \alpha, \beta_i \in V - \alpha, f \in F\}. \tag{5}$$

**Definition 2.** Given color law set  $S = \{s_0, s_1 \dots, s_{k-1}\} \subset U, \alpha = \{\alpha_0, \alpha_1, \dots, \alpha_{n-1}\} \subset V$  is the attribute set of  $S$ , then  $S^F$  is called the color  $P$ -external law set generated by  $S$  and

$$S^F = S \cup S^+ \quad (6)$$

$S^+$  is called the color  $F$ -law supplemented set of  $S$  and

$$S^+ = \{s'_i | f(r_i) = s'_i \in S, r_i \in U - S, f \in F\} \quad (7)$$

if the attribute set  $\alpha^{\bar{F}}$  of  $S^F$ , satisfies

$$\alpha^{\bar{F}} = \alpha - \{\beta_i | \bar{f}(\alpha_i) = \beta_i \notin \alpha, \alpha_i \in \alpha, \bar{f} \in \bar{F}\}. \quad (8)$$

**Definition 3.** The color-law set pair formed by  $S^{\bar{F}}$  and  $S^F$  is called the color  $P$ -law set generated by the color law set  $S$  and

$$(S^{\bar{F}}, S^F) \quad (9)$$

Based on Definitions 1-3, the color  $P$ -law characteristics based on the natural environment is put forward.

## 2.2 The Characteristics of Color $P$ -law

Based on **Definition 1**, the attribute set  $\alpha$  of the color law set  $S$  is continuously attribute supplemented or deleted to obtain the color  $P$ -law interference chain.

**Theorem 1.** Color law Interference Chain Reasoning Theorem

Given the color law set  $S = \{s_0, s_1, \dots, s_{k-1}\} \subset U$ ,  $\alpha = \{\alpha_0, \alpha_1, \dots, \alpha_{n-1}\} \subset V$  is the attribute set of  $S$ , then

$$\alpha_0^F \subseteq \alpha_1^F \subseteq \dots \subseteq \alpha_{m-1}^F \Rightarrow S_{m-1}^{\bar{F}} \subseteq \dots \subseteq S_1^{\bar{F}} \subseteq S_0^{\bar{F}} \quad (10)$$

$$\alpha_{m-1}^{\bar{F}} \subseteq \dots \subseteq \alpha_1^{\bar{F}} \subseteq \alpha_0^{\bar{F}} \Rightarrow S_0^F \subseteq S_1^F \subseteq \dots \subseteq S_{m-1}^F \quad (11)$$

From Eqs. (10) and (11), corollary 1 can be directly obtained:

**Corollary 1.** If the existence of the color  $P$ -law set depends on the interference (supplement or deletion) of the attribute set of the color-law set  $S$ , then there is

$$\{(S_i^{\bar{F}}, S_j^F) | i, j \in \{0, 1, \dots, m-1\}\} \quad (12)$$

where any  $(S_i^{\bar{F}}, S_j^F)$  is the color  $P$ -law.

Apparently, when  $F = \bar{F} = \phi$  and the color  $P$ -law set  $S$  is not interfered, the color  $P$ -law  $(S_i^{\bar{F}}, S_j^F)$  loses its dynamic characteristics, that is,

**Corollary 2.** Color law  $S$  and color  $P$ -law set  $\{(S_i^{\bar{F}}, S_j^F) | i, j \in \{0, 1, \dots, m-1\}\}$  satisfy

$$\{(S_i^{\bar{F}}, S_j^F) | i, j \in \{0, 1, \dots, m-1\}\}_{F=\bar{F}=\phi} = S. \quad (13)$$

Based on Definitions 1–3, Theorem 1 and Corollary 1, a color  $P$ -law generation model can be given.

## 3 Color $P$ -law Generation Model

Given the color law set  $S = \{s_0, s_1, \dots, s_{k-1}\} \subset U$ ,  $\alpha = \{\alpha_0, \alpha_1, \dots, \alpha_{n-1}\} \subset V$  is the attribute set of  $S$ , the color law generation algorithm can be given as follows:

### 3.1 The Color P-law Generation Algorithm

#### (1) Discretization of the Color Law

Discretized form of color law  $\forall s_i \in S$

$$s_i(x_0), s_i(x_1), \dots, s_i(x_{m-1}), i = 0, 1, \dots, k - 1 \tag{14}$$

#### (2) Discrete Form Generation of the Color Law Set

Based on Eq. (14), the discrete form of the color law set  $S = \{s_0, s_1, \dots, s_{k-1}\}$  is

$$y_0 = \sum_{i=0}^{k-1} s_i(x_0), y_1 = \sum_{i=0}^{k-1} s_i(x_1), \dots, y_{m-1} = \sum_{i=0}^{k-1} s_i(x_{m-1}) \tag{15}$$

#### (3) The Law Generation of the Color Law Set S

$$N(x) = f(x_0) + f[x_0, x_1](x - x_0) + \dots + f[x_0, x_1, \dots, x_m](x - x_0) \dots (x - x_{m-1})f[x_0, x_1, \dots, x_m] \tag{16}$$

$$f[x_0, x_1, \dots, x_{k-1}] = \frac{f[x_0, \dots, x_{k-2}, x_{k-1}] - f[x_0, x_1, \dots, x_{k-2}]}{x_{k-1} - x_{k-2}} \tag{17}$$

Eq. (17) is the  $k$ -th order mean difference of  $f(x)$ , where  $f(x_j) = y_j, j = 0, 1, \dots, m - 1$ , and the form of Eq. (14) is not unique, its form can be derived according to specific questions.

Apparently, the attribute set  $\alpha = \{\alpha_0, \alpha_1, \dots, \alpha_{n-1}\}$  of the color law set  $S = \{s_0, s_1, \dots, s_{k-1}\}$  is interfered by  $(F, \bar{F})$ , inevitably leading to the generation of color  $P$ -law set  $(S^{\bar{F}}, S^F)$  of  $S$ .

**Definition 4.** Let  $(S^{\bar{F}}, S^F)$  be the color  $P$ -law set generated by the color law set  $S$ , we have:

- (1)  $N(x)^F$  is called the  $P$ -external law generation the color of  $S$ , abbreviated as  $S$  the color  $P$ -external law, if  $N(x)^F$  is the color law set generation of  $S^F$ ;
- (2)  $N(x)^{\bar{F}}$  is called the  $P$ -internal law generation the color of  $S$ , abbreviated as  $S$  the color  $P$ -internal law, if  $N(x)^{\bar{F}}$  is the color law set generation of  $S^{\bar{F}}$ ;
- (3)  $(N(x)^F, N(x)^{\bar{F}})$  is called the color  $P$ -law generation of  $S$ , abbreviated as the color  $P$ -law of  $S$ .

The curve of the color  $P$ -external law  $N(x)^F$  generated by  $S$  and the curve of the color  $P$ -internal law  $N(x)^{\bar{F}}$  generated by  $S$  jointly form the color  $P$ -law band of  $S$ .

$$\{N(x)^F, N(x)^{\bar{F}}\} \tag{18}$$

### 3.2 Dynamic Characteristic of Color P-law Generation Algorithm

**Definition 5.** Let  $(S^{\bar{F}}, S^F)$  be the color  $P$ -law set generated by the color law set  $S$ , we have:

- (1)  $\gamma(S^F)$  is called the  $P$ -external law interference degree of  $S^F$  with respect to  $S$ , abbreviated as the  $P$ -external law interference of  $S$ , if

$$\gamma(S^F) = \frac{\|S^F - S\|}{\|S^F\|} \tag{19}$$

- (2)  $\gamma(S^{\bar{F}})$  is called the  $P$ -internal law interference degree of  $S^{\bar{F}}$  with respect to  $S$ , abbreviated as the  $P$ -internal law interference of  $S$ , if

$$\gamma(S^{\bar{F}}) = \frac{\|S - S^{\bar{F}}\|}{\|S\|} \tag{20}$$

where  $\|S\|$  is the color law measure of  $S$ .

(3)  $(\gamma(S^{\bar{F}}), \gamma(S^F))$  is called the  $P$ -law interference degree of  $(S^{\bar{F}}, S^F)$ , if  $\gamma(S^F), \gamma(S^{\bar{F}})$  are the  $P$ -external law interference and the  $P$ -internal law interference degree of  $S$ , respectively.

Obviously, definition 5 reveals the dynamic change degree of the  $P$ -external law set  $S^{\bar{F}}$  and the  $P$ -internal law set  $S^F$  with respect to  $S$  when the attribute set  $\alpha$  of the color law set  $S$  is interfered by  $(F, \bar{F})$ . In other words, the bigger  $\gamma(S^F)$  and  $\gamma(S^{\bar{F}})$  are, the more dynamic the color  $P$ -law  $(S^{\bar{F}}, S^F)$  of  $S$  is.

**Theorem 2.** Given the color law set  $S$  and the attribute set  $\alpha$  of  $S$ , if  $\alpha$  is interfered by  $(F, \bar{F})$ , then the  $P$ -law interference degree of  $(S^{\bar{F}}, S^F)$  is  $(\gamma(S^{\bar{F}}), \gamma(S^F))$ , satisfies,

$$0 \leq \gamma(S^{\bar{F}}) \leq 1, \quad 0 \leq \gamma(S^F) \leq 1; \tag{21}$$

$$F = \phi \Rightarrow \gamma(S^{\bar{F}}) = 0; \tag{22}$$

$$\bar{F} = \phi \Rightarrow \gamma(S^F) = 0. \tag{23}$$

**Proof:** If  $\alpha$  is interfered by  $(F, \bar{F})$ , according to definition 1, there is  $S^{\bar{F}} \subseteq S \subseteq S^F$ , then

$$S^F - S \subseteq S^F \Rightarrow \|S^F - S\| \leq \|S^F\|, \tag{24}$$

$$S - S^{\bar{F}} \subseteq S \Rightarrow \|S - S^{\bar{F}}\| < \|S\|. \tag{25}$$

According to definition 5, (24) and (25), there is  $0 \leq \gamma(S^{\bar{F}}) \leq 1, \quad 0 \leq \gamma(S^F) \leq 1$ .

If  $F = \phi$ , then  $S^{\bar{F}} = S$ , therefore  $\gamma(S^{\bar{F}}) = 0$ ; If  $\bar{F} = \phi$ , then  $S^F = S$ , therefore  $\gamma(S^F) = 0$ .

### 3.3 The Interconversion between Color Spaces

Without loss of generality, only the conversion between RGB space and HSL space is discussed here [31].

#### (1)RGB to HSL Color Conversion

The R, G, B values are divided by 255 to change the range from [0, 255] to [0, 1], respectively. To make our definitions easier to write, we'll define:

$$M = \max\{R, G, B\}, \quad m = \min\{R, G, B\}, \quad D = M - m. \tag{26}$$

And Hue, Saturation and Lightness calculation:

$$H = \begin{cases} 0^0, & \text{if } D = 0 \\ 360^0 \cdot \frac{G - B}{D} \bmod 6, & \text{if } M = R \\ 360^0 \cdot (\frac{B - R}{D} + 2), & \text{if } M = G \\ 360^0 \cdot (\frac{R - G}{D} + 4), & \text{if } M = B \end{cases}, \tag{27}$$

$$S = \begin{cases} 0, & \text{if } D = 0 \\ \frac{D}{1 - |2 \cdot L - 1|}, & \text{if } D \neq 0 \end{cases}, \tag{28}$$

$$L = \frac{M + m}{2} \tag{29}$$

**(2) HSL to RGB Color Conversion**

Given a color with hue  $H \in [0^\circ, 360^\circ)$ , saturation  $S \in [0, 1]$ , and lightness  $L \in [0, 1]$ , Hue, Saturation and Lightness calculation:

$$(R, G, B) = \begin{cases} (0, 0, 0) + K, & \text{if } H \text{ is undefined} \\ (C, X, 0) + K, & \text{if } 0 \leq H/60^0 < 1 \\ (X, C, 0) + K, & \text{if } 1 \leq H/60^0 < 2 \\ (0, C, X) + K, & \text{if } 2 \leq H/60^0 < 3 \\ (0, X, C) + K, & \text{if } 3 \leq H/60^0 < 4 \\ (X, 0, C) + K, & \text{if } 4 \leq H/60^0 < 5 \\ (C, 0, X) + K, & \text{if } 5 \leq H/60^0 < 6 \end{cases} \tag{30}$$

$$X = C \cdot (1 - |H/60^0 \bmod 2 - 1|), \quad C = (1 - |2 \cdot L - 1|) \cdot S, \quad K = L - C/2. \tag{31}$$

In many situations, the central limit theorem (CLT) establishes that the sum of many independent, additive effects is approximately normally distributed, even if the original variables themselves are not normally distributed.

**Theorem 3.** (Central Limit Theorem [31]) If  $X_1, X_2, \dots, X_n$  are  $n$  random samples drawn from a population with overall mean  $E(X_i) = \mu$  and finite variance  $D(X_k) = \sigma^2, k = 1, 2, \dots, n$ , and if  $\bar{X}_n = \frac{1}{n} \sum_{k=1}^n X_k$  is the sample mean, the limiting form of the distribution,

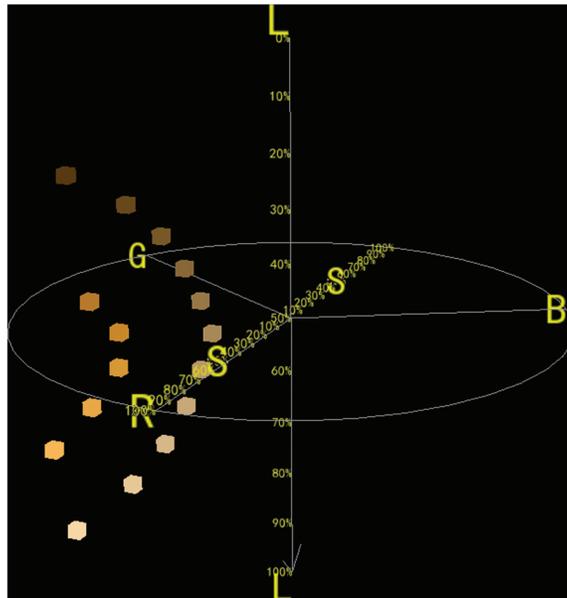
$$\lim_{n \rightarrow +\infty} P\left\{\sqrt{n}\left(\frac{\bar{X}_n - \mu}{\sigma}\right) \leq x\right\} = \int_{-\infty}^x \frac{1}{\sqrt{2\pi}} e^{-t^2/2} dt = \Phi(x) \tag{32}$$

**4 Color P-law Reasoning Simulation**

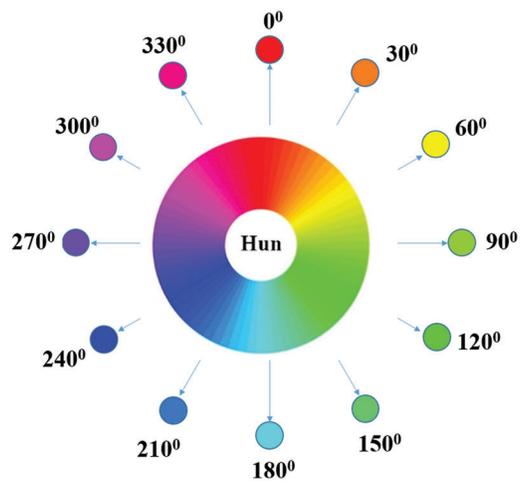
Various colors in nature can be applied to color sensors to obtain  $(H, S, L)$  digital values in the HSL space, which is a one-to-one mapping to the positions in the color three-dimensional space. Each color can be represented by a digital quantity. The digitization of the color enables a more accurate and convenient color management, the order chain in HSL color space is shown in Fig. 1. The value of hue in HSL space, which satisfies  $H \in [0^\circ, 360^\circ)$ , can be calculated counterclockwise from the red spot (as it is shown in Fig. 2) in the color wheel. Red is  $0^\circ$ , green is  $120^\circ$ , and blue is  $240^\circ$ . Their complementary colors are  $60^\circ$  for yellow,  $180^\circ$  for cyan, and magenta for  $300^\circ$ . Saturation indicates how close the color is to the spectral color. A color is a mixture of a certain spectral color and white. The larger the proportion of the spectral color, the closer the color is to the spectral color, and the higher the saturation, the deeper and colorful the color. The white light component of the spectral color is 0, and the saturation is the highest. Usually, the value ranges from 0% to 100%. The larger the value, the more saturated the color. The HSL color solid simulation is shown in Fig. 3 [4].

In simulation experiments, when the external color factors of simulated plants in the natural environment are disturbed, they form a discrete color law family (the corresponding RGB values are omitted), and the color of the corresponding plants changes accordingly.

By simulating and analyzing the factor  $\alpha$  of the color law set of plants when  $(F, \bar{F})$ -interference occurs, according to theorem 3 (Central Limit Theorem) and [25–30], the generation of  $(H, S, L)$  law distribution family of HSL space (as shown in Figs. 4, 6), deduce the generated color P-law of HSL, where  $H$  is represented using  $R, G$  and  $B$ , to achieve the intelligent color P-law reasoning simulation based on the natural environment.



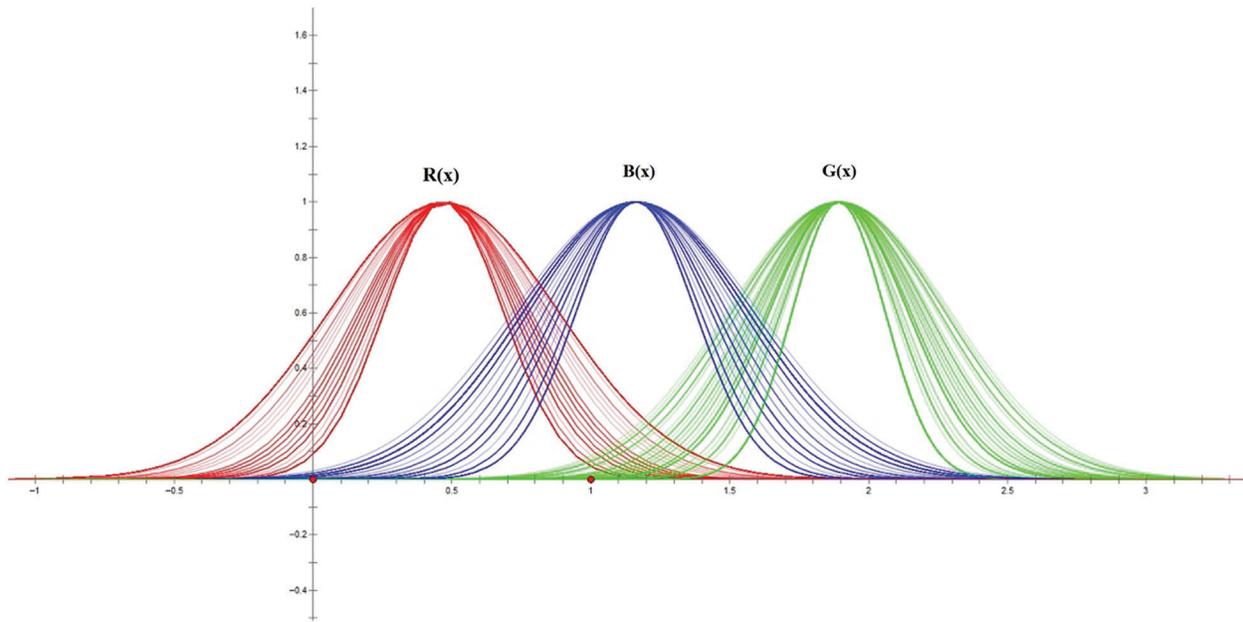
**Figure 1:** Order chain in HSL color space



**Figure 2:** The hun color wheel

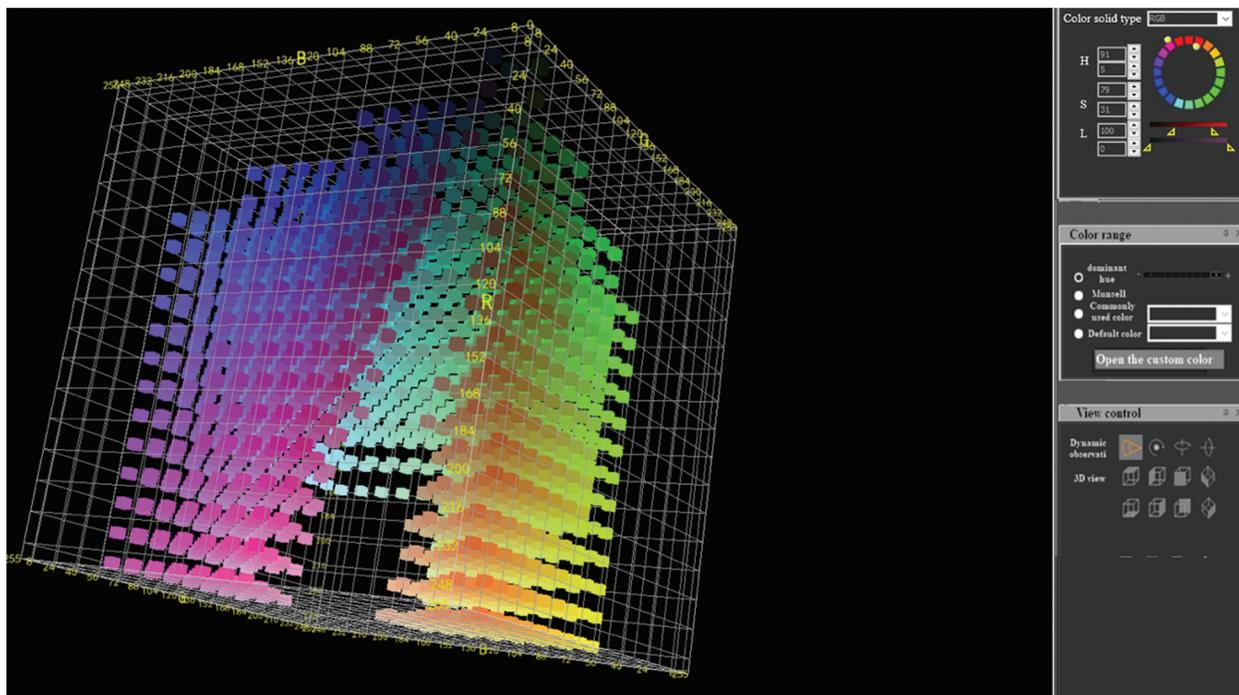


**Figure 3:** The simulation image of the HSL color solid

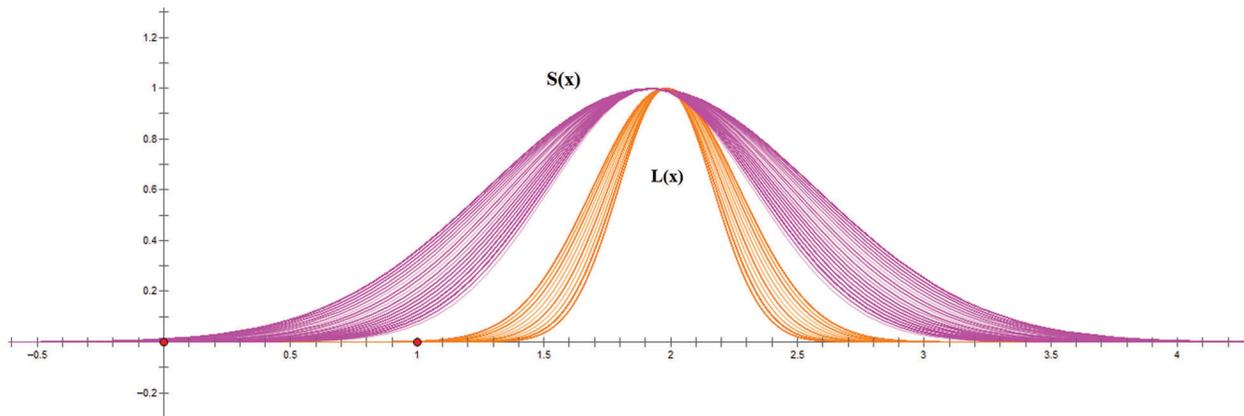


**Figure 4:**  $(F, \bar{F})$ -interference distribution of the  $(R, G, B)$

The simulation of the RGB color solid by  $(F, \bar{F})$ -interfered is shown in Fig. 5, when  $5^{\circ} \leq H < 91^{\circ}$ ,  $31\% \leq S \leq 79\%$ ,  $0 \leq L \leq 100\%$ .



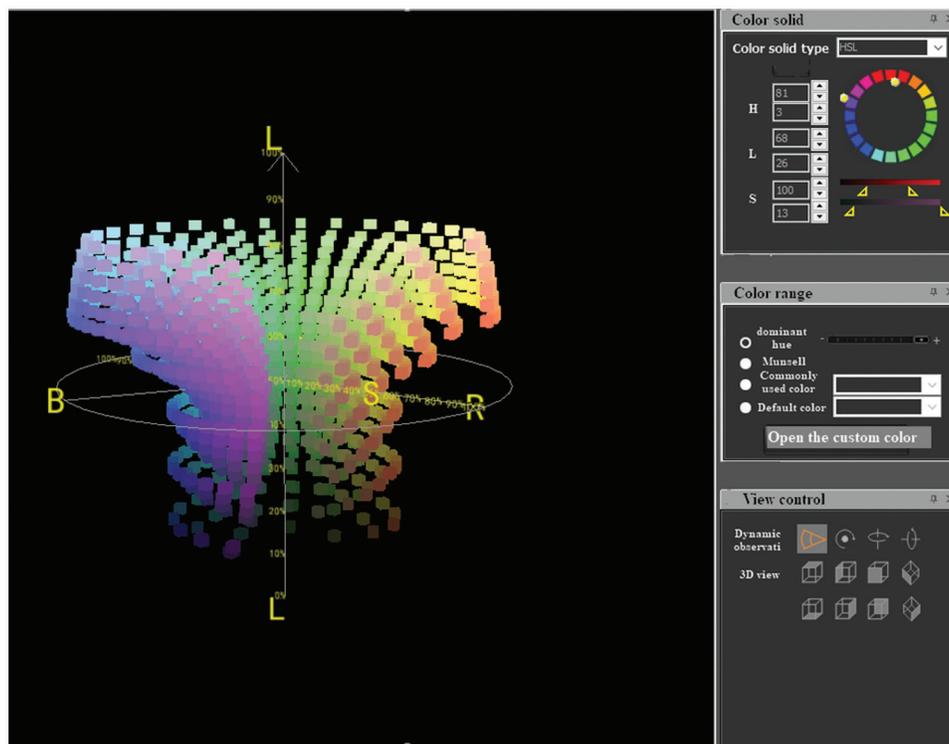
**Figure 5:** The simulation of the RGB color solid by  $(F, \bar{F})$ -interfered



**Figure 6:**  $(F, \bar{F})$ -interference distribution of the saturation and lightness

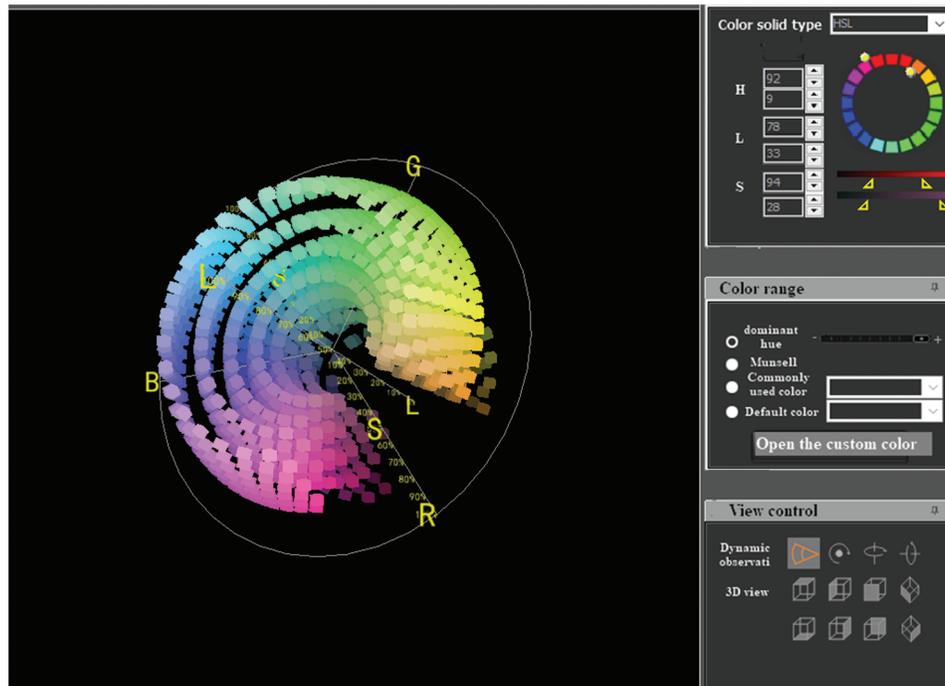
The simulation of the HSL color solid by  $(F, \bar{F})$ -interfered as follows:

When  $3^0 \leq H < 81^0$ ,  $26\% \leq S \leq 100\%$ ,  $26\% \leq L \leq 68\%$ , the simulation of the HSL color solid by  $(F, \bar{F})$ -interfered is shown in Fig. 7.



**Figure 7:** The simulation of the HSL color solid by  $(F, \bar{F})$ -interfered

When  $9^0 \leq H < 92^0$ ,  $28\% \leq S \leq 94\%$ ,  $33\% \leq L \leq 78\%$ , the simulation of the HSL color solid by  $(F, \bar{F})$ -interfered is shown in Fig. 8.



**Figure 8:** The simulation of the HSL color solid by  $(F, \bar{F})$ -interfered

## 5 Conclusion

This paper proposes a dynamic color system theory based on the function  $P$ -set and presents a color reasoning algorithm for the  $P$ -law in a natural environment. The simulation experiment simulates the basic law of color variation when external factors change. The outcome of this paper will be applied in the color simulation of the IoT devices. When the natural conditions in the scene change, the plants will also change autonomously. The proposed algorithm can effectively extract color data, which can significantly reduce the data transmission bandwidth of color sensors in the IoT network.

Since the models and algorithms currently studied only simulate the color factors of plants, there are some points worthy of further study: 1) The time and space complexity of the algorithm can be analyzed; 2) The research and simulation of the color-law relationship between HSL and other standard color stereo, etc. To facilitate the analysis, this paper adopts the calculation method of normal distribution and incorporates the random function into the proposed method to obtain the expected effect, which will be further discussed in the follow-up research.

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