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Evolution Analysis of Network Attack and Defense Situation Based on Game Theory

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ABSTRACT: To address the problem that existing studies lack analysis of the relationship between attack-defense game behaviors and situation evolution from the game perspective after constructing an attack-defense model, this paper proposes a network attack-defense game model (ADGM). Firstly, based on the assumption of incomplete information between the two sides of the game, the ADGM model is established, and methods of payoff quantification, equilibrium solution, and determination of strategy confrontation results are presented. Then, drawing on infectious disease dynamics, the network attack-defense situation is defined based on the density of nodes in various security states, and the transition paths of network node security states are analyzed. Finally, the network zero-day virus attack-defense behaviors are analyzed, and comparative experiments on the attack-defense evolution trends under the scenarios of different strategy combinations, interference methods, and initial numbers are conducted using the NetLogo simulation tool. The experimental results indicate that this model can effectively analyze the evolution of the macro-level network attack-defense situation from the micro-level attack-defense behaviors. For instance, in the strategy selection experiment, when the attack success rate decreases from 0.49 to 0.29, the network destruction rate drops by 11.3%, in the active defense experiment, when the interference coefficient is reduced from 1 to 0.7, the network destruction rate decreases by 7%, and in the initial node number experiment, when the number of initially infected nodes increases from 10 to 30, the network destruction rate rises by 3%.

KEYWORDS: Network attack-defense; situation evolution; zero-day virus; NetLogo

1 Introduction

With the development of 5G networks, the number of Internet of Things (IoT) devices has increased dramatically, leading to more complex, intelligent, and diverse network security threats and attack methods. Traditional passive defense technologies are no longer able to meet the ever-changing network security needs, so there is an urgent need for technologies that can effectively characterize network attack-defense behaviors, accurately predict the evolution trends of network attack-defense situations, and implement active defense. The characteristics of the network attack-defense confrontation process, such as objective opposition, strategy dependence, and non-cooperative relationships, align with the features of game theory [1]. Game theory is considered to be one of the fundamental theories in the discipline of cyberspace security, and can provide an effective way to study network security issues [2]. Therefore, constructing network attack-defense



behavior models based on game theory enables an in-depth analysis of the evolution of network attack-defense situations, effectively enhancing the capability to prevent security threats and improving defense efficiency [3].

In network security research, game theory models provide a systematic framework for analyzing and optimizing the selection of attack-defense strategies. According to the degree of completeness of the behavior and gain information grasped by both attackers and defenders, it can be categorized into complete and incomplete information game models [4]. The degree of completeness of information refers to the fact that the attack and defense parties clearly understand all the strategies that the other side may adopt at each stage, and accurately know the benefits of different behaviors or combinations of strategies. In a complete information game model, all participants have complete knowledge of all information. For example, Sun et al. [5] addressed the issue of selecting defense strategies for multi-path combination attacks in network attack and defense, established a non-zero-sum game model based on complete information, optimized the computation method for the gain, and proposed the selection method of the optimal defense strategy. To assess the security status of large-scale cloud networks, Chowdhary et al. [6] constructed a two-player zero-sum Markov game model, which can enhance network security defense capabilities by identifying the attacker's optimal strategy and forcing the attacker to adopt sub-optimal strategies. Wang et al. [7] addressed the issue of security risk assessment for military information networks and proposed a network security risk assessment method based on complete information game. The method quantified the gains of attack-defense strategies in terms of network security features and provided recommendations for selecting optimal defense strategies on the basis of risk assessment.

In an incomplete information game model, at least one party cannot have certain key information, which can result in information asymmetry. Liu et al. [8] addressed the issue that existing network research focuses on only one of the attack-defense parties, making it difficult to accurately describe and represent the network attack-defense dynamics. They proposed an incomplete information attack-defense game model, and elucidated the temporal evolution of the network attack-defense situations through simulation experiments in various scenarios. However, relying solely on the quantity of a certain type does not intuitively reflect the network attack-defense situation. Yi et al. [9] established an attack-defense tree model for false data injection attacks using economic indicators and attack metrics, calculated the expected gains for both attackers and defenders, and determined the optimal defense strategy through equilibrium analysis. Yan et al. [10] addressed the problem of allocating limited defense resources in complex information-physical power systems to cope with false data injection attacks. They developed an incomplete information zero-sum game model, used the state offset caused by false data injection attacks to quantify the attack-defense gains, and provided the optimal defense resource allocation method through simulation results. However, the unequal gains of both sides were ignored in the gain quantification process. Gao et al. [11] addressed the lack of in-depth analysis of dynamic continuous interactions between multiple attackers and defenders in future wireless networks. They constructed an interaction model based on a differential game, introduced the paralysis threshold, derived the equilibrium strategy using optimal control theory combined with Hamilton's function, and proposed an optimal decision-making algorithm. However, the model relies on numerous fixed parameters, making it suitable only for short-term attack-defense scenarios. To solve the problem that existing deception resource selection methods based on game theory cannot simulate continuous dynamic attack and defense behaviors when modeling, He et al. [12] constructed a deception resource choice method based on differential game and Deep Q-network (DQN). The method constructed the node state evolution process based on the infectious disease susceptible-infected-removed (SIR) model by analyzing the attacks and defense strategies, giving the main function of the attacks and defenses, and solving the optimal deception resource strategy by the DQN algorithm. However, the DQN algorithm has the problem

of overestimation when calculating the Q-value. Aiming at the problem that complex network defense strategies do not fully consider the attack and defense characteristics and the existing algorithms are difficult to adapt to a variety of complex networks, Zhang et al. [13] constructed a potential differential game model for network attack-defense, analyzed node state evolution, quantified attack-defense payoff, and enhanced defense effectiveness, but still faces the challenges of high computational cost and poor scalability. Tang et al. [14] addressed the problem of complex and variable attack behaviors and dynamic changes of the network structure in the network environment. They constructed a Stackelberg hypergame model to describe the conflict in cyberspace, and derived the game evolution by hierarchical multi-intelligence reinforcement learning to form a dynamic and autonomous defense strategy. Their model can effectively respond to the attacks and reasonably allocate resources, but the game model is constructed based on rational assumptions, which makes it fail to fully reflect the real network attack and defense confrontation environment fully. He et al. [15] tackled the problem that existing deception decision models based on game theory ignore the optimal defense timing. They proposed a deception timing method based on the FlipIt game and Proximal Policy Optimization (PPO). By incorporating discount factors and transfer probabilities, the single-stage FlipIt game was extended to a multi-stage version, designed payoff functions, and the optimal deception timing strategy was solved using the PPO algorithm. However, the model is poorly adapted and migrated, and the scope of application is relatively narrow.

In summary, the analysis and optimization of attack-defense strategies based on game theory models demonstrate that each method can provide theoretical guidance for selecting defense strategies. However, existing methods also have certain limitations. Although the complete information game model is simple to construct, easy to reason and analyze, and simple to calculate and solve, in real-world network attack-defense confrontations, both parties find it difficult to fully understand each other's information. The game model based on incomplete information takes into account the incomplete information mastery of both attack-defense parties, making them more aligned with real-world network attack-defense processes, but it cannot effectively analyze the relationship between attack-defense behaviors and situation evolution.

Therefore, this paper considers the decision-making behavior of network attack-defense nodes as logically simultaneous decisions, establishes an incomplete information static attack-defense game model, and defines the network attack-defense situation by drawing on infectious disease dynamics theory. Through network zero-day virus attack-defense game experiments, we study the evolution trend of network attack-defense situations under different scenarios. The main contributions are as follows:

- A network attack-defense model is constructed based on incomplete information static game theory, proposing methods for payoff quantification, game equilibrium solution, and determination of strategy confrontation results, which aligns with the information incompleteness in real-world network attack-defense scenarios better.
- Drawing on the theory of infectious disease dynamics, the network attack-defense situation is defined through the density of network nodes, and the five state transition paths of network nodes are analyzed, which helps to explain the evolution of the network attack-defense situation from the perspective of attack-defense behaviors.
- Using the improved SIR model, a simulation model for a network attack-defense game is constructed. It simulated the temporal evolution of network attack-defense situations under different strategy combinations, interference methods, and initial numbers, and proposes recommendations to enhance network defense effectiveness.

The remainder of this paper is organized as follows. [Section 2](#) provides the method of revenue quantification, game equilibrium solution, and determination of strategy confrontation results. [Section 3](#)

describes the network attack-defense situation definition and evolution analysis. [Section 4](#) presents the setup of the simulation experiments and the analysis of the results. [Section 5](#) concludes this paper.

2 Construction of Network Attack-Defense Game Model

This section describes the construction of the game model used to analyze the evolutionary trend of the network attack-defense situation, which is divided into three main parts: game model definition, game equilibrium solution, and the method for determining attack-defense strategy confrontation results. Before the discussion, in order to facilitate the description, [Table 1](#) lists some of the relevant symbols used in this paper.

Table 1: Symbols explanation

Symbols	Explanation
N	Game player space
S	Strategy space
θ	Type space
$x(t)$	Network attack and defense situation at time t
T	Time
P	Probability space
β	Interference coefficient
U	Payoff function
AC	Attack cost
DC	Defense cost
SLC	System loss cost
SPE	System protection earnings
η	Defense strategy effectiveness
AL	Attack lethality
RI	Resource importance
SAD	Security attribute damage
Q	Strategy strength
p	Attack success rate

2.1 Game Model Definition

In network attack-defense scenarios, the attackers and defenders have completely opposing objectives, resulting in a distinct game structure. This antagonistic relationship makes it difficult for both sides to fully grasp each other's action strategy information, resulting in both attackers and defenders being constrained by limited rationality. In this environment, the attacker's attack strategies, attack revenues, and other key information are not visible to the defender. The defender can only analyze the system's potential vulnerabilities, speculate on the attacker's possible behaviors, and choose the optimal defense strategy on this basis. Therefore, to effectively construct attack-defense game model, it is generally assumed that both the attacker and the defender are constrained by factors such as capabilities, resources, and preferences. The

attack-defense strategies are limited, and both parties aim to maximize their payoffs through appropriate strategy combinations.

Definition 1. The network attack-defense game model (ADGM) can be represented as an eight-tuple, $ADGM = (N, S, \theta, x(t), T, P, \beta, U)$.

- (1) $N = (N_A, N_D)$ is the game player space, where N_A denotes the attacker, and N_D denotes the defender.
- (2) $S = (AS, DS)$ is the game strategy space, where $AS = \{AS_i | i = 1, 2, 3, \dots, m\}$ denotes the optional strategy set of the attacker and $DS = \{DS_j | j = 1, 2, 3, \dots, n\}$ denotes the optional strategy set of the defender, and $1 \leq (m, n) \leq +\infty$.
- (3) $\theta = (\theta_A, \theta_D)$ is the type space, where θ_A denotes the type of the attacker, and θ_D denotes the type of defender.
- (4) $x(t)$ is the network attack-defense situation at time t . This paper uses the density of security state nodes to characterize the network attack-defense situations, please see Definition 8 in Section 3 for detailed analysis.
- (5) T denotes time. The network attack-defense games are dynamic and continuous adversarial processes that require modeling and analysis from a temporal perspective.
- (6) $P = (P_A, P_D)$ is the probability space of the players, where P_A denotes the attacker probability space, and P_D denotes the defender probability space.
- (7) β is the interference coefficient. The defender can adopt an active defense approach to interfere with attacker's actions and reduce their success rates.
- (8) $U = (U_A, U_D)$ is the game payoff function, where U_A represents the attacker payoffs, and U_D represents the defender payoffs.

2.2 Game Equilibrium Solution

The quantification of attack-defense payoffs is the fundamental basis for equilibrium calculation and inference analysis in game models. To more accurately show the advantages and disadvantages of attack-defense strategies, this paper redefines the quantification of attack cost, defense cost, system loss cost, system protection earnings, and defense strategy effectiveness from the perspective of both attackers and defenders on the basis of existing research [16,17].

Definition 2. Attack cost (AC) refers to the expenses incurred by the attacker in carrying out an attack during the attack-defense process. This includes the cost of creating and deploying zero-day viruses, as well as the penalty incurred when the defender detects the attack.

Definition 3. Defense cost (DC) refers to the expenses incurred by the defender to implement defensive actions for resource protection. This includes the cost of implementing zero-day virus defense strategies and the losses caused by increased system overhead due to taking defensive actions.

Definition 4. System loss cost (SLC) is influenced by the combination of attack-defense strategies, denoted as $SLC(AS_i, DS_j)$, which represents the loss incurred by the target system when the defense strategy selection DS_j fails to stop the attack strategy AS_i .

Definition 5. System protection earnings (SPE) are influenced by the combination of attack-defense strategies, denoted as $SPE(AS_i, DS_j)$, which represents the protection of target system resources when the defense strategy selection DS_j effectively blocks the attack strategy AS_i .

Definition 6. Defense strategy effectiveness $\eta(AS_i, DS_j)$ refers to the effectiveness of defense strategy DS_j for countering attack strategy AS_i during the attack and defense process, and it satisfies $\eta(AS_i, DS_j) \in [0, 1]$.

System loss cost $SLC(AS_i, DS_j)$ and system protection earnings $SPE(AS_i, DS_j)$ are usually described by attack lethality (AL), resource importance (RI), security attribute damage (SAD), and defense strategy effectiveness $\eta(AS_i, DS_j)$, the calculation method is given by Eq. (1).

$$\begin{cases} SLC(AS_i, DS_j) = (1 - \eta(AS_i, DS_j)) * AL * RI * SAD \\ SPE(AS_i, DS_j) = \eta(AS_i, DS_j) * AL * RI * SAD \end{cases} \quad (1)$$

Due to the different implementation costs of the attack-defense strategies, the payoff $U_A(AS_i, DS_j)$ and $U_D(AS_i, DS_j)$ under different combinations of attack-defense strategies (AS_i, DS_j) are calculated by Eq. (2).

$$\begin{cases} U_A(AS_i, DS_j) = SLC(AS_i, DS_j) - AC(AS_i) \\ U_D(AS_i, DS_j) = SPE(AS_i, DS_j) - DC(DS_j) \end{cases} \quad (2)$$

ADGM is an incomplete information static game with Bayesian Nash equilibrium, whose existence theorem and proof can be found in the literature [18]. When solving the equilibrium of incomplete information games, the Harsanyi transformation is used to introduce a virtual player, “Nature,” converting the problem into an equilibrium-solving task for a complete but imperfect information game. For the convenience of reasoning and analysis, we assume that the attacker has two types $\theta_A = \{\theta_{A1}, \theta_{A2}\}$, with corresponding probabilities $P_{Ai} = \{P_{A1}, P_{A2}\}$, where $P_{A1} + P_{A2} = 1$, and each type has attack strategies of different strengths, $\theta_{A1} = \{AS_1, AS_2\}$ and $\theta_{A2} = \{AS_3, AS_4\}$. Similarly, we assume that the defender has two types $\theta_D = \{\theta_{D1}, \theta_{D2}\}$, with corresponding probabilities $P_{Dj} = \{P_{D1}, P_{D2}\}$, where $P_{D1} + P_{D2} = 1$, and each type has attack strategies of different strengths, $\theta_{D1} = \{DS_1, DS_2\}$ and $\theta_{D2} = \{DS_3, DS_4\}$. The incomplete information static Bayesian game tree obtained by Harsanyi transformation twice is shown in Fig. 1.

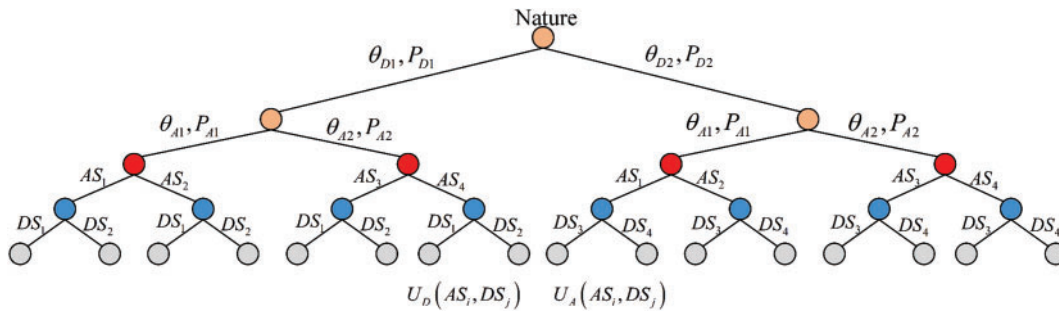


Figure 1: Incomplete information static Bayesian game tree

At time t , the attacker’s payoff is denoted as $U_A(AS(t), DS(t))$ (abbreviated as $U_A(t)$). Due to the incomplete information static game, the attacker does not know the exact type of the defender, so the attacker’s payoff $U_A(t)$ needs to account for the probability P_{Dj} of the defender’s various types, as well as the probability P_{Ai} of the attacker’s various types. For each combination of defense type θ_{Dj} and attack type θ_{Ai} , the payoff is $U_A(AS_i, DS_j)$ (where AS_i is the attack strategy under the attack type θ_{Ai} and DS_j is the defense strategy under the defense type θ_{Dj}). By weighting the payoffs of all possible combinations according to their

probabilities, the attacker’s payoff can be represented by Eq. (3).

$$\begin{aligned}
 U_A(t) &= \sum_{i=1}^m \sum_{j=1}^n P_{Ai} * P_{Dj} * U_A(AS_i, DS_j) \\
 &= \sum_{\theta_A} P_{Ai} * P_{Dj} * U_A(AS_i, DS_j)
 \end{aligned} \tag{3}$$

Similarly, at time t , the defender’s payoff is denoted as $U_D(AS(t), DS(t))$ (abbreviated as $U_D(t)$) as shown in Eq. (4).

$$\begin{aligned}
 U_D(t) &= \sum_{i=1}^m \sum_{j=1}^n P_{Ai} * P_{Dj} * U_D(AS_i, DS_j) \\
 &= \sum_{\theta_D} P_{Ai} * P_{Dj} * U_D(AS_i, DS_j)
 \end{aligned} \tag{4}$$

Let $U_A^*(t)$ and $U_D^*(t)$ be the Bayesian Nash equilibrium solutions of the ADGM, which satisfy Eq. (5).

$$\begin{cases}
 U_A^*(t) = \max \sum \{P(DS_j|AS_i) U_A[(AS(t), DS^*(t)); AS_i, DS_j]\} \\
 U_D^*(t) = \max \sum \{P(AS_i|DS_j) U_D[(DS(t), AS^*(t)); DS_j, AS_i]\}
 \end{cases} \tag{5}$$

where $U_A^*(t)$ denotes the maximum payoff for the attacker when choosing the optimal strategy $AS^*(t)$ under the given defense strategy $DS(t)$. $P(DS_j|AS_i)$ denotes the conditional probability that the defender chooses strategy DS_j when the attacker chooses strategy AS_i . $U_A[(AS(t), DS^*(t)); AS_i, DS_j]$ denotes the attacker’s payoff when the attacker chooses strategy $AS(t)$ and the defender chooses the optimal strategy $DS^*(t)$. $U_D^*(t)$ denotes the maximum payoff for the defender when choosing the optimal strategy $DS^*(t)$ under the given attack strategy $AS(t)$. $P(AS_i|DS_j)$ denotes the conditional probability that the attacker chooses strategy AS_i when the defender chooses strategy DS_j . $U_D[(DS(t), AS^*(t)); DS_j, AS_i]$ denotes the defender’s payoff when the defender chooses strategy $DS(t)$ and the attacker chooses the optimal strategy $AS^*(t)$.

Eqs. (3)–(5) are combined to form a system of equations, and the Bayesian Nash equilibrium of the ADGM can be solved using the linear programming method. The equilibrium solution represents the optimal strategy for each party, where no unilateral change in strategy by either party will increase their payoff.

2.3 Determination of Network Attack-Defense Strategy Confrontation Results

Definition 7. The strategy strength $Q = (Q_A, Q_D)$ indicates the magnitude of a strategy’s capability, where Q_A represents the attacker’s strategy strength and Q_D represents the defender’s strategy strength, which is mainly used to determine the results of attack-defense game.

Referring to the common vulnerability scoring system [19], strategy types are categorized based on the strength of attack-defense strategies. According to the attacker’s strategy strength, they are classified into two categories, i.e., strong attack and weak attack, denoted as $\theta_A = \{\theta_{AH}, \theta_{AL}\}$, where Q_{AH} and Q_{AL} denote the strategy strength values of the strong and weak attacks, respectively. If the attacker adopts a mixed strategy at time t , with the selection probabilities P_{AH} and P_{AL} of strong and weak attacks, respectively, the probability

of choosing the mixed strategy is denoted as $P_A(t) = \{P_{AH}, P_{AL}\}$. The expected value method is used to calculate the strategy strength $Q_A(t)$ of the attacker, as shown in Eq. (6).

$$\begin{cases} Q_A(t) = P_{AH} * Q_{AH} + P_{AL} * Q_{AL} \\ P_{AH} + P_{AL} = 1 \\ Q_{AH}, Q_{AL} \in [0, 1] \end{cases} \quad (6)$$

Considering that the defender typically use active defense strategies to disrupt attackers' actions and reduce their success rates. When the interference coefficient β is introduced, the attacker's strategy strength is shown in Eq. (7).

$$Q_A^*(t) = \beta * Q_A(t) \quad (7)$$

Based on the defender's strategy strength, their strategy type are classified into two categories, i.e., strong defense and weak defense, denoted as $\theta_D = \{\theta_{DH}, \theta_{DL}\}$, where Q_{DH} and Q_{DL} denote the strategy strength values of the strong and weak defense, respectively. If the defender adopts mixed strategy at time t , with the selection probabilities P_{DH} and P_{DL} of strong and weak defenses respectively, the probability of choosing the mixed strategy is denoted as $P_D(t) = \{P_{DH}, P_{DL}\}$. The expected value method is used to calculate the strategy strength $Q_D(t)$ of the defender, as shown in Eq. (8).

$$\begin{cases} Q_D(t) = P_{DH} * Q_{DH} + P_{DL} * Q_{DL} \\ P_{DH} + P_{DL} = 1 \\ Q_{DH}, Q_{DL} \in [0, 1] \end{cases} \quad (8)$$

Definition 8. The attack success rate p denotes the value where the attacker's strategy strength is higher than the defender's strategy strength, as shown in Eq. (9).

$$p = \begin{cases} Q_A^*(t) - Q_D(t), Q_A^*(t) > Q_D(t) \\ 0, Q_A^*(t) < Q_D(t) \end{cases} \quad (9)$$

3 Network Attack-Defense Situation Definition and Evolution Analysis

Emergence is a natural attribute of network security. Qu et al. [20] pointed out that epidemic models and agent-based simulations are effective methods for studying the emergence of network security. The SIR model is a classic infectious disease model, which is mainly used to analyze the propagation patterns of infectious diseases within a population. The main reason why the infectious disease model is suitable for modeling network attacks is the similarities between the two in terms of propagation characteristics and state transitions. (1) In terms of propagation characteristics, infectious diseases spread through inter-individual contact or other means, whereas network attacks spread through the network via connections between nodes, and infected nodes can become new sources of propagation and continue to trigger spread. (2) In terms of state transitions, infectious individuals undergo a process from susceptibility to infection to recovery, while network nodes undergo a process from susceptibility (vulnerable nodes) to infection to immunity. These similarities enable the infectious disease model to effectively simulate network attack-defense behaviors, predict the spread of attacks, and provide an important reference for the development of network attack prevention and control strategies. While Markov chains and stochastic processes can describe the state transfer of a system, they often fail to reflect the complexity and diversity behind the transfer. In contrast, the susceptible-infected-removal-damaged (SIRD) model portrays the security state evolution of network nodes

more comprehensively by introducing multiple security state nodes (e.g., susceptible, infected, removal, and damaged states) and their transfer paths. For example, in a case of an attack on an enterprise network, some employees initially clicked on a malicious link in a phishing email (corresponding to a susceptible state node contacting the source of the infection), which resulted in some of the computers within the enterprise entering the infected state. As the attack continued, the enterprise security team deployed firewalls and intrusion detection systems (corresponding to the defense policy), and some of the infected nodes were quarantined or repaired and transferred to the immune state. However, some new attacks (e.g., zero-day vulnerability attacks) cause repaired nodes to be infected again (similar to removal state nodes changing back to susceptible state due to virus mutation), and some nodes with failed defense suffer data leakage or system corruption (enter the damaged state). The above modeling approach not only better fits the complex dynamics of actual network attack and defense scenarios, but also more accurately predicts the scope and trend of attack propagation. The SIR model, Markov chains, and stochastic process comparison are presented in [Table 2](#).

Table 2: Model comparison

Model	SIR model	Markov chains	Stochastic process
State change portrayal	Graphical depiction of state transfers for better intuition	Describing state transfers in terms of a probability matrix is less intuitive	Describing state transfers in terms of random variables is not intuitive
Attack propagation path representation	Clearly show the path of attack proliferation	Difficulty in presenting clear details of the attack path	Difficulty in accurately representing attack propagation paths
Accuracy of long-term trend forecasts	Relatively high	Ordinary	Relatively low

The SIR model has been used to some extent in the area of cybersecurity research. For example, Wang et al. [21] constructed a “Two-go and One-live” type virus propagation model based on the susceptible-infected-removed-susceptible (SIRS) information diffusion model, analyzed the stability of equilibrium points by applying the Routh-Hurwitz stability criterion, and provided countermeasure suggestions to enhance network defense capabilities. Liu et al. [22] established a susceptible-exposed-infected-removal (SEIR) propagation model with mutant viruses based on the infectious disease model. By determining the optimal control variable pair for the repair rates of infected and mutant nodes, the optimal control strategy was proposed. Tang et al. [23] proposed a susceptible-latent-breaking-recovered-susceptible (SLBRS) virus propagation model for scale-free network topology features based on the infectious disease model and gave the optimal control strategy by analyzing the global stability under virus-free equilibrium.

During the confrontation process, the attacker attempts to expand the attack range by deploying the attack strategy to more nodes, and the defender attempts to protect the normal service of network nodes by deploying defense strategies to more nodes. From the emergence perspective, micro-level network attack-defense game behaviors cause changes in network node states, thereby influencing the evolution of network attack-defense situations at the macro-level. In a network system composed of numerous nodes, attack-defense confrontations primarily cause two changes. (1) The security state of individual network nodes changes continuously. (2) The number of network nodes in different security states undergoes ongoing dynamic changes. According to the mechanism of action of network viruses, the zero-day virus propagation

process consists of four stages, i.e., susceptibility, virus propagation, virus repair, and damage. Therefore, based on the SIR model, the damaged state is introduced to propose the SIRD model, which defines four types of network node states, i.e., susceptible state S , infected state I , removal state R , and damaged state D .

S : The network node has not deployed any attack-defense strategies, and normal users have control over the node. $S(t)$ denotes the count of susceptible state nodes at time t .

I : The attacker has deployed an attack strategy at this node and has control over it, which corresponds to N_A in the ADGM. $I(t)$ denotes the count of infected state nodes at time t .

R : The defender has deployed a defense strategy at this node and has control over it, which corresponds to N_D in the ADGM. $R(t)$ denotes the count of removal state nodes at time t .

D : All defense strategies fail, and the infected nodes lose their normal service function. $D(t)$ denotes the count of damaged state nodes at time t .

In network attack-defense research, it is generally assumed that the studied network system is fixed, with a constant number of nodes denoted as N . The network attack and defense games can cause node security state transitions and dynamic changes in the number of different types of nodes, but regardless of how the network nodes transition and change, the total number of nodes in the four types of security status at the time t remains constant, as shown in Eq. (10).

$$S(t) + I(t) + R(t) + D(t) = N \quad (10)$$

Network node density refers to the proportion of a certain type of node to the total number of nodes. The higher the density of network nodes, the more dominant that type of node is in network attack-defense confrontations. The density of different types of nodes reflects their distribution in the network system at a specific moment, characterizing the network attack-defense situation.

Definition 9. The network attack-defense situation at time t is composed of four types of network node densities $x(t) = (\rho_S, \rho_I, \rho_R, \rho_D)$, which is represented by Eq. (11).

$$\left\{ \begin{array}{l} \rho_S(t) = \frac{S(t)}{N} \\ \rho_I(t) = \frac{I(t)}{N} \\ \rho_R(t) = \frac{R(t)}{N} \\ \rho_D(t) = \frac{D(t)}{N} \\ \rho_S(t) + \rho_I(t) + \rho_R(t) + \rho_D(t) = 1 \end{array} \right. \quad (11)$$

The network nodes in different states are regarded as intelligent agents, respectively, and the phenomenon of network attack-defense situation evolution at the macro level is analyzed through the micro level network attack-defense game behaviors. In the zero-day virus attack-defense situation simulation, the node's behavior rules are set based on the real network attack-defense scenarios, aiming to simulate the node's state changes under the effect of attack-defense strategies. Due to the game behaviors between attackers and defenders, the SIRD model has five node security state transition paths, as shown in Fig. 2.

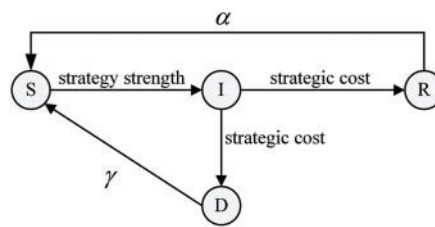


Figure 2: Node security state transition path

$S \rightarrow I$: The susceptible state S node comes in contact with the infected state I node and the average strategy strength of the attacker is higher than that of the defender, the network node cannot resist the attack.

$I \rightarrow R$: According to the strategic cost of attack and defense game, if the defender can afford the defense cost, the node will transition from an infected state to a removal state.

$R \rightarrow S$: In the process of propagation of zero-day virus, it will continuously mutate, causing the removal nodes to lose the ability of immunity to the mutated virus, and α represents the conversion rate from a removal state to a susceptible state.

$I \rightarrow D$: According to the strategy cost of the attack-defense game, if the defender cannot afford the defense strategy's cost, nodes transition from an infected state to a damaged state.

$D \rightarrow S$: Due to some core computers being controlled, the service performance of the entire network will be degraded, and the operation and maintenance personnel will renovate some damaged nodes, and γ represents the recovery rate from the damaged state to the susceptible state.

4 Simulation Analysis of Network Zero-Day Virus Attack-Defense Cases

4.1 Analysis of Network Zero-Day Virus Attack-Defense Behavior

The zero-day virus is one of the frequently appearing forms of network attacks in recent years, with significant impacts including WannaCry, Bash Shellshock, Log4Shell, and Spring4Shell. The zero-day viruses first use common viruses such as Trojans and worms to hide malicious code for illegal activities and implant it into the target host. Then, they exploit zero-day vulnerabilities to self-replicate and spread to other target hosts. Once a host is infected, attackers can remotely execute malicious code, steal or destroy data, and even take full control of the system. Unlike traditional viruses, zero-day viruses exhibit diverse types, rapid mutation rates, complex propagation mechanisms, strong concealment, and high destructiveness. If defense measures are not updated promptly, it is difficult to defend against them effectively. Therefore, preventing zero-day viruses requires efforts from both technical and management aspects, defense measures include real-time patch updates, vulnerability fixes, strengthening authentication and audit processes, and establishing comprehensive emergency response plans. This paper takes zero-day viruses as an example, constructs the ADGM, and analyzes network attack-defense behaviors.

In the zero-day virus game model, the participants are the zero-day virus attacker N_A and the network security defender N_D . The attackers are divided into two types $\theta_A = (\theta_{AH}, \theta_{AL})$, representing strong attack types and weak attack types. There are various types of zero-day viruses, each with different attack capabilities. For example, remote code execution (RCE) can execute malicious code on the target host and gain full control of the system. Memory exploitation (ME) uses buffer overflow vulnerabilities in memory to execute malicious code, bypass security mechanisms, and gain system permissions. Cross-site scripting (XSS) attacks steal user sessions by injecting malicious scripts, but cannot directly control the server. Cross-site request forgery (CSRF) performs unauthorized operations by forging legitimate user requests, but cannot

directly execute malicious code. This paper considers RCE and ME as strong attack types, and XSS and CSRF as weak attack types. The defenders are divided into two types $\theta_D = (\theta_{DH}, \theta_{DL})$, representing strong defense types and weak defense types. Anomaly detection (AD) can promptly identify and respond to anomalies. Updating patches (UP) can fix known vulnerabilities and reduce the attack surface. Real-time software updates (RTSU) are effective only against known vulnerabilities and cannot detect zero-day vulnerabilities. Deleting useless accounts (DUA) can reduce potential attack entry points. This paper considers AD and UP as strong defense types, and RTSU and DUA as weak defense types. Referring to the classification method of reference [24], the attack strategy is divided into $AS = \{AS_1, AS_2, AS_3, AS_4\}$ and the defense strategy is divided into $DS = \{DS_1, DS_2, DS_3, DS_4\}$. The relevant attributes of the attack-defense strategies for zero-day virus are presented in Tables 3 and 4.

Table 3: Attack strategy attribute description

Action	Attack action	AL	AC	Attack strength	Strategy type	Strategy strength
AS_1	RCE	10	200	0.94	θ_{AH}	0.92
AS_2	ME	10	165	0.90		
AS_3	XSS	9	110	0.56	θ_{AL}	0.52
AS_4	CSRF	9	75	0.48		

Table 4: Defense strategy attribute description

Action	Defense action	DC	Defense strength	Strategy type	Strategy strength
DS_1	AD	300	0.72	θ_{DH}	0.71
DS_2	UP	220	0.70		
DS_3	RTSU	170	0.24	θ_{DL}	0.21
DS_4	DUA	120	0.18		

Based on the zero-day virus attack-defense practice, the importance of the resources attacked by (AS_1, AS_2, AS_3 and AS_4) is in the order of (6, 5, 4, 4) and the safety attribute damage is (30, 30, 25, 25), respectively. According to the China National Vulnerability Database of Information Security (CNNVD), the effectiveness of the defense strategy $\eta(AS_i, DS_j)$ is listed as shown in Eq. (12).

$$\eta(AS_i, DS_j) = \begin{bmatrix} & AS_1 & AS_2 & AS_3 & AS_4 \\ DS_1 & 0.35 & 0.4 & 0.7 & 0.9 \\ DS_2 & 0.25 & 0.3 & 0.6 & 0.8 \\ DS_3 & 0.15 & 0.2 & 0.4 & 0.6 \\ DS_4 & 0.1 & 0.1 & 0.3 & 0.5 \end{bmatrix} \quad (12)$$

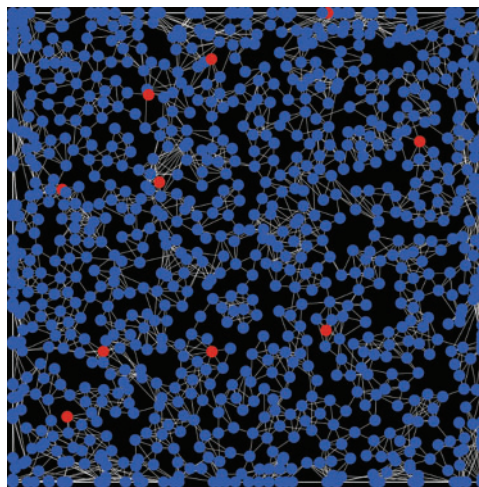
Based on historical data and regression analysis, combined with the experience of security experts, the defense payoff $U_D(AS_i, DS_j)$ and attack payoff $U_A(AS_i, DS_j)$ under different combinations of attack-defense strategies (AS_i, DS_j) are calculated using Eqs. (1) and (2), as shown in Table 5.

Table 5: Attack-defense payoff under different strategy combinations

Attack-defense strategy	AS_1	AS_2	AS_3	AS_4
DS_1	(330, 1060)	(360, 825)	(487, 227)	(510, 75)
DS_2	(230, 1240)	(275, 990)	(455, 340)	(500, 105)
DS_3	(100, 1330)	(160, 1155)	(280, 565)	(370, 285)
DS_4	(60, 1420)	(90, 1320)	(217, 677)	(330, 375)

4.2 Network Zero-Day Virus Attack and Defense Situation Simulation

The network information system consists of numerous nodes, and the attack-defense game behaviors of a single node makes it difficult to effectively show the overall network attack-defense situation, simulation is an effective way to solve the problem. NetLogo is an open-source multi-agent simulation tool capable of simulating intelligent interaction behaviors among numerous nodes simultaneously. In the field of cybersecurity, there are many researches on the characteristics of virus propagation, according to the possibility that the zero-day virus may have behavior such as mutation or user updating the system in the process of spreading, the simulation experiment sets the transformation rate from removal node to susceptible node $\alpha = 0.2$. In order to compare with the adoption of various active defense strategies (e.g., releasing false signals, dynamically adjusting the attack surface, etc.), the simulation experiments set the interference coefficients $\beta = 1$ for initially not adopting any active defense strategy. In the actual network operation and maintenance, when some of the core computers are controlled to cause network performance degradation, the operation and maintenance personnel will take a series of measures to refurbish the damaged equipment, simulation experiments set the recovery rate from the damaged node to the susceptible node $\gamma = 0.03$. To prevent more subjectivity, the total number of nodes is set to $N = 1000$. The average node degree is set to 6 based on the average of node connections in common enterprise network topologies. The initial number of S , I , R and D nodes are 990, 10, 0 and 0, respectively. The initial main interface is generated as shown in Fig. 3, where blue nodes represent the susceptible state S and red nodes represent the infected state I .

**Figure 3:** Initial main interface

By setting different simulation parameters, we can dynamically simulate the evolution trend of attack-defense situations over time in scenarios with different strategy combinations, different interference methods, and different initial numbers. When the count of infected nodes in the network system is zero, the count of damaged nodes cannot intuitively reflect the attack-defense situation, while the density of damaged nodes can display attack-defense status at a specific moment. Therefore, the density of damaged nodes is defined as the network destruction rate.

4.2.1 Simulation Experiments on the Impact of Strategy Selection on Attack-Defense Situation

Scenario 1: When the selection probabilities of attack and defense strategies are $P_A(t) = \{0.7, 0.3\}$ and $P_D(t) = \{0.2, 0.8\}$, respectively. The attack success rate $p = 0.49$ can be calculated by Eqs. (6)–(9). The simulation results are shown in Fig. 4.

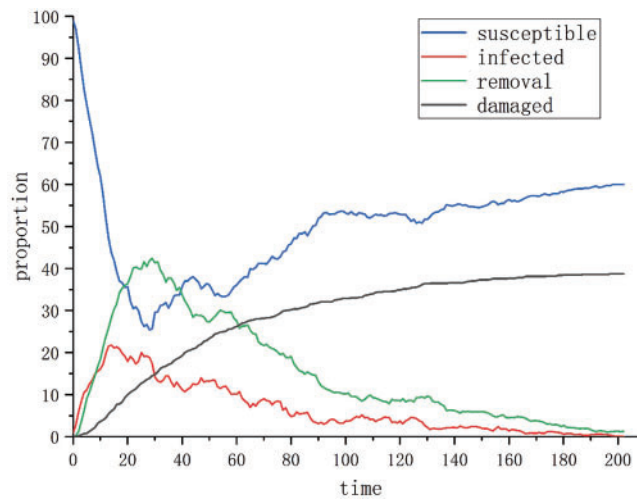


Figure 4: Evolution of the attack-defense situation when $p = 0.49$

Scenario 2: When the selection probabilities of attack and defense strategies are $P_A(t) = \{0.7, 0.3\}$ and $P_D(t) = \{0.6, 0.4\}$, respectively. The attack success rate $p = 0.29$ can be calculated by Eqs. (6)–(9). The simulation results are shown in Fig. 5.

4.2.2 Simulation Experiments on the Impact of Active Defense on the Attack-Defense Situation

Scenario 3: For the comparison experiment, the attacker and defender's strategy selection probabilities follow the setting of Scenario 1. In this case, the defender employs a weak active defense strategy by releasing false signals to disrupt with the attacker's judgment, with the interference coefficient $\beta = 0.9$. The simulation results are shown in Fig. 6.

Scenario 4: The attacker and defender's strategy selection probabilities follow the setting of Scenario 1. In this case, the defender opts for a strong active defense strategy, dynamically adjusting the attack surface to reduce the success rate of the attacker, with the interference coefficient $\beta = 0.7$. The simulation results are shown in Fig. 7.

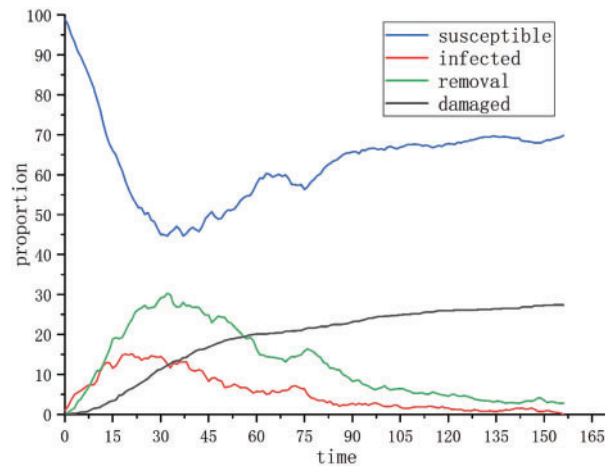


Figure 5: Evolution of the attack-defense situation when $\rho = 0.29$

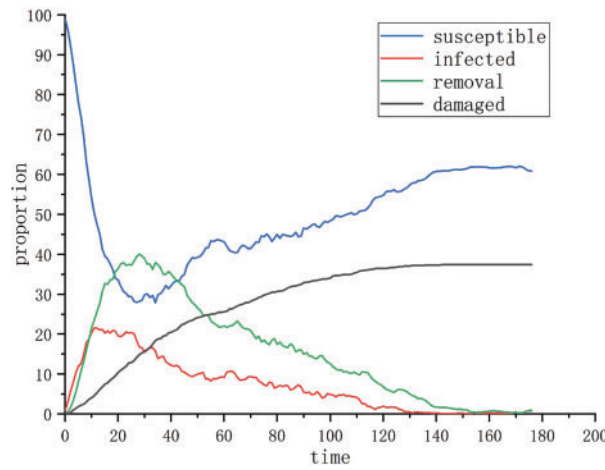


Figure 6: Evolution of the attack-defense situation when $\beta = 0.9$

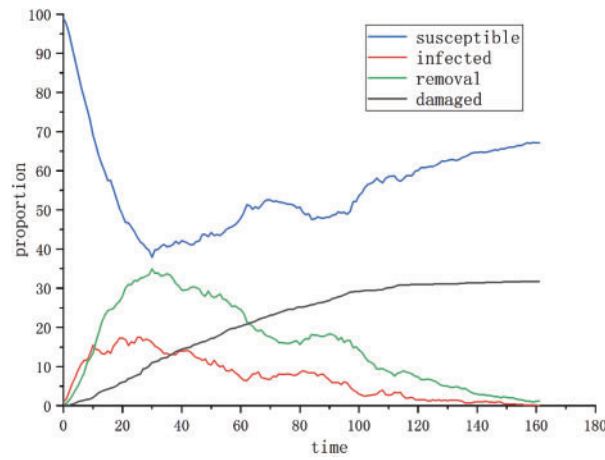


Figure 7: Evolution of the attack-defense situation when $\beta = 0.7$

4.2.3 Simulation Experiment on the Impact of the Initial Number of Nodes in Different States on the Attack-Defense Situation

Scenario 5: For the control experiment, the control variable method is adopted, the attacker and defender's strategy selection probabilities follow the setting of Scenario 1, and the initial number of infected state I nodes is set to 20. The simulation results are shown in Fig. 8.

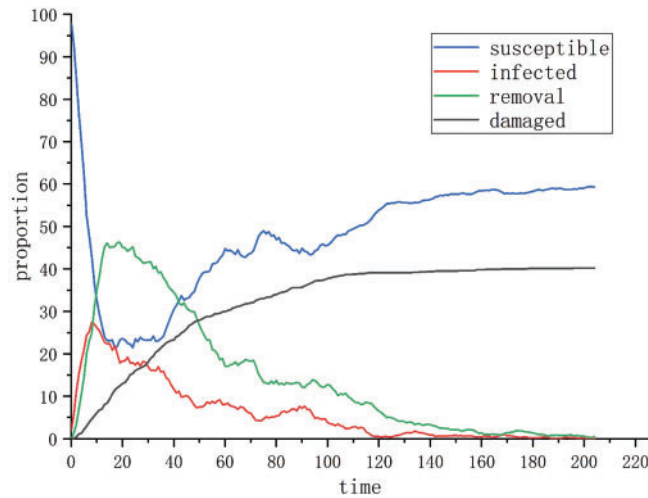


Figure 8: Evolution of the attack-defense situation when $I = 20$

Scenario 6: The attacker and defender's strategy selection probabilities follow the setting of Scenario 1, and the initial number of infected state I nodes is set to 30. The simulation results are shown in Fig. 9.

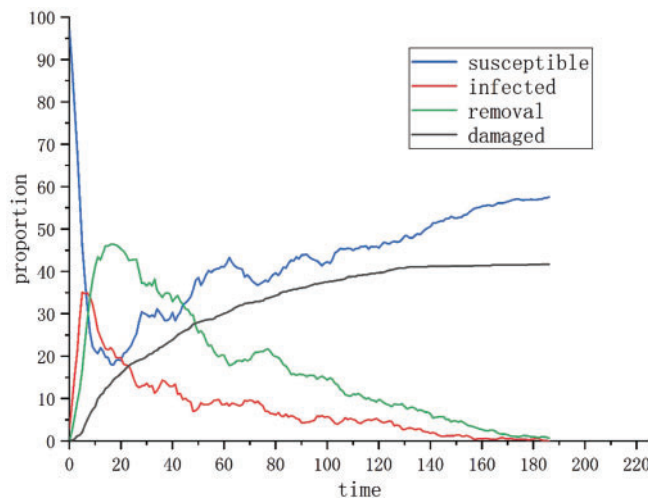


Figure 9: Evolution of the attack-defense situation when $I = 30$

4.3 Simulation Results Analysis

By analyzing the simulation results in the different scenarios mentioned above, the following three countermeasure suggestions to enhance network defense effectiveness can be obtained:

(1) Strengthening the defense capabilities of individual nodes is crucial to reversing the network attack-defense situation. Comparing the experimental results of Scenario 1 and Scenario 2, when $p = 0.49$, the network destruction rate is 38.7%. When $p = 0.29$, the network destruction rate is 27.4%. The comparison results show that the game between attackers and defenders depends solely on the attack success rate in the absence of other factors interfering, as the attack success rate decreases, the network destruction rate also decreases. Therefore, from the perspective of actual network security scenarios, network defenders should enhance their attention to network security and improve the defense capabilities of individual nodes. Enterprise networks usually have a complex organizational structure covering multiple departments and business systems, with significant differences in network security requirements across departments. With this model, the enterprise security team can divide the network into multiple security zones based on the business importance of different departments and the distribution of network nodes, and develop personalized defense strategies for each zone. For example, for servers and critical network equipment in core business departments, the model can guide the deployment of intrusion detection systems, set up firewalls, regularly update system patches, and implement strict access control policies. These measures can effectively lower the success rate of attacks, thereby reducing overall network security risks and enhancing defense capabilities against potential threats.

(2) Utilizing active defense technologies can effectively reduce the network destruction rate. Comparing the experimental results of Scenarios 1, 3, and 4, when the interference coefficient $\beta = 1$, the network destruction rate is 38.7%. When the interference coefficient $\beta = 0.9$, the network destruction rate is 37.4%. When the interference coefficient $\beta = 0.7$, the network destruction rate is 31.7%. The comparison results indicate that as the interference coefficient decreases, the network destruction rate also declines. Therefore, defenders should make comprehensive use of new active defense technologies such as mobile target defense and mimetic defense, and increase the difficulty of attackers in identifying and attacking the target system by deploying dynamic defense mechanisms, to effectively safeguard network security. Cloud computing environments are characterized by dynamic allocation of resources and multi-tenant sharing. This model helps cloud service providers optimize resource allocation by quantitatively analyzing attacker and defender strategy strengths and their benefits. For example, in cloud computing environments, using dynamic resource allocation and virtualization technology, a moving target defense strategy can be implemented to increase the difficulty of locating attackers by continuously adjusting the network resource allocation and service deployment location, thus improving the security and defense capability of the system.

(3) The initial number of infected nodes will affect the macro-level evolution trend of the network attack-defense situation. Comparing the experimental results of Scenario 1, Scenario 5, and Scenario 6, the higher the initial number of infected nodes, the more unfavorable the attack-defense scenarios are to the defender, while the overall number of nodes remains the same. When the initial infected node $I = 10$, the network destruction rate is 38.7%. When the initial infected node $I = 20$, the network destruction rate is 40.1%. When the initial infected node $I = 30$, the network destruction rate is 41.7%. In the IoT environment, the large and widely distributed number of devices, along with the complex network structure and diverse device types, complicates the situation. If employees' lack of security awareness (e.g., clicking on a malicious link) leads to the initial infection of some nodes with viruses, the viruses may spread rapidly and destroy the entire network service. Through this model, it is possible to monitor the changes in the status of network nodes, discover the initially infected nodes in time, reduce the number of attackers from the source, and thus effectively change the network attack-defense posture. Therefore, there is an urgent need to strengthen the popularization of network security awareness, improve the network security skills of the whole society, establish a sound network defense system, and focus on measures such as device authentication, encrypted communication, and abnormal traffic monitoring to enhance overall security.

The model and methodology of this paper are compared with the relevant references, as shown in Table 6. The following can be seen:

(1) In terms of model assumptions, the literatures [5,6] are based on the complete information assumption. However, in real-world network attack-defense scenarios, the information on both sides is uncertain. This paper adopts the assumption of incomplete information, making it more aligned with the realities of network attack-defense.

(2) In the analysis of situation evolution, the literature [8] models the attacker and defender as agents and represents the network attack-defense situation through the number of agents. However, this method lacks intuitive visualization. Drawing on the theory of infectious disease dynamics, this paper defines the network attack-defense situation based on the density of network nodes in various security states, providing a more intuitive representation of situational evolution.

(3) In terms of attack-defense experimental scenarios, the literatures [5,6,10] all use physical attack and defense environments with a few number of nodes, strong subjectivity, and a large amount of calculation. This paper uses the NetLogo multi-agent body simulation tool to simulate the evolutionary trend of network attack-defense situations over time. With numerous nodes and low computational requirements, it is well-suited for large-scale scenarios.

Table 6: Model and method comparison

References	Model assumption	Situation evolution analysis	Attack-defense experiment scenarios	Node number	Situation display effect
[5]	Complete information	No	Physical attack-defense environment	Few	No
[6]	Complete information	No	Physical attack-defense environment	Few	No
[10]	Incomplete information	No	Physical attack-defense environment	Few	No
[8]	Incomplete information	Simple	NetLogo multi-agent simulation	Many	Non-intuitive
This paper	Incomplete information	Detailed	NetLogo multi-agent simulation	Many	Intuitive

5 Conclusion

With the development of 5G networks, the frequency of cybersecurity incidents has increased, and traditional passive defense is unable to meet the ever-changing cybersecurity needs. Modeling methods can effectively analyze network attack-defense processes and improve network defense capabilities. However, existing network attack-defense models lack the analysis of the relationship between micro-level attack-defense game behaviors and macro-level network attack-defense situations from the game perspective. To

address these issues, this paper proposes a network attack -defense game model (ADGM), proposes the SIRD model which introduces the damage state node based on the SIR model, defines the network attack-defense situation by the density of different security state nodes, analyzes the network node security state transition paths by the game results which are used to analyze the network attack-defense situation evolution phenomenon from the network attack-defense behavior level, conducts experiments on the evolution trends of network attack-defense situations over time in different scenarios were using the NetLogo multi-agent simulation tool, and finally provides recommendations for enhancing network defense effectiveness by analyzing and summarizing the experimental results.

Based on the above theoretical modeling, although our method can effectively analyze the evolution trend of network attack-defense situations, it still has the following limitations: firstly, the assumption of static strategy space fails to adequately reflect the actual network environment; secondly, the computational complexity of the Bayesian Nash equilibrium in large-scale network systems has not yet been effectively addressed. To address the above limitations, future work will introduce Asynchronous Advantage Actor-Critic (A3C) technology. A3C combines the advantages of policy gradient and value function, enabling agents to dynamically adjust attack and defense strategies according to changes within network conditions. Additionally, approximation algorithms and distributed computing techniques will be employed to enhance computational efficiency by decomposing large-scale computational tasks into smaller sub-tasks that can be processed in parallel.

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