



Efficient Group Blind Signature for Medical Data Anonymous Authentication in Blockchain-Enabled IoMT

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Abstract: Blockchain technology promotes the development of the Internet of medical things (IoMT) from the centralized form to distributed trust mode as blockchain-based Internet of medical things (BIoMT). Although blockchain improves the cross-institution data sharing ability, there still exist the problems of authentication difficulty and privacy leakage. This paper first describes the architecture of the BIoMT system and designs an anonymous authentication model for medical data sharing. This BIoMT system is divided into four layers: perceptual, network, platform, and application. The model integrates an anonymous authentication scheme to guarantee secure data sharing in the network ledger. Utilizing the untampered blockchain ledger can protect the privacy of medical data and system users. Then, an anonymous authentication scheme called the group blind signature (GBS) scheme is designed. This scheme can provide anonymity for the signer as that one member can represent the group to sign without exposing his identity. The blind property also can protect the message from being signed as it is anonymous to the signer. Moreover, this GBS scheme is created with the lattice assumption, which makes it more secure against quantum attacks. In addition, the security proof shows that this GBS scheme can achieve the security properties of dynamical-almost-full anonymity, blindness, traceability, and non-frameability. The comparison analysis and performance evaluation of key size show that this GBS scheme is more efficient than similar schemes in other literature.

Keywords: Blockchain; Internet of medical things; signature; privacy-preserving

1 Introduction

Internet of medical things (IoMT) is the direction for traditional healthcare service systems with the increasing number of wearable and mobile medical devices [1]. IoMT establishes a medical network that aggregates dispersive medical data created by many smart medical devices. Although these massive amounts of medical data can contribute much to patient treatment, drug discovery, and medical equipment manufacturing, they also face many security issues as they contain sensitive information



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about the patient and medical institution. Therefore, the security of medical data and user privacy is more important for data sharing through IoMT [2].

Blockchain technology brings new vitality to traditional IoMT and helps to establish the distributed medical data management platform called blockchain-based Internet of medical things (BIO-MT) [3]. The public blockchain ledger guarantees that data and operation records are not tampered with, which can well solve the centralized management problem in traditional IoMT [4]. Through this distributed platform, the patient can freely choose the needed medical institution and get more precise treatment with historical medical data, the doctor can improve the efficiency of diagnosis with more comprehensive medical data, and the researcher can develop the level of drug discovery and medical equipment manufacturing with massive amounts of medical data. By focusing on these goals, more and more BIO-MT frameworks and proposes are emerging in recent years, such as Healthchain, Fortified-chain, and so on [5–15]. Meanwhile, some AI-powered methods also appear to improve data-handling capacity and analysis efficiency, such as machine learning and federated learning [16,17]. However, these works mainly focus on medical data management and utilization but rarely care about the security of medical data and user privacy using the cryptographic algorithm [18].

Privacy-preserving is the main challenge for BIO-MT [19]. As identity privacy is generally inserted in medical data, it can be divulged easily with centralized management forms, insecure data transmission, or man-made sabotage. Meanwhile, medical data are indicators of patients' physical condition, which are also personal privacies, especially for important persons. Blockchain transactions contain the operator's signature, essential in verifying transaction legitimacy, confirming the operator's identity, and data traceability for medical disputes [20]. For the privacy security of medical data in BIO-MT, the signer's anonymity is a more critical issue. A group signature allows one member to represent the group for signing, and the verifier can verify the signature's legitimacy but not confirm which one is the real signer [21–26]. Meanwhile, a blind signature utilizes a blind factor to blind the message to be signed [27–30]. Some protocols with these two properties have been proposed, which can guarantee anonymous of the user identity and data information [31–33]. Therefore, this paper plans to combine these two signatures to design a GBS scheme and establish an anonymous authentication model for privacy-preserving in BIO-MT.

This paper mainly focuses on the problems of authentication difficulty and privacy leakage in the medical data-sharing process. It contributes to the privacy-preserving method for medical data and users in the BIO-MT system. A four-ledger architecture for the BIO-MT system has been introduced first, and an anonymous authentication model has been designed to strengthen the security of the data-sharing process in the network ledger. Then, a GBS scheme has been proposed to achieve anonymous authentication. The detailed contributions of this work are as follows:

- A four-ledger architecture for the BIO-MT system has been introduced, which contains four layers of the perceptual, network, platform, and application. From data collection to application, this distributed peer-to-peer platform can guarantee the transparency and integrity of medical data. Meanwhile, an anonymous authentication model has been designed, which can strengthen the security of the data-sharing process in the network ledger.
- A GBS scheme has been proposed to achieve anonymous authentication. It provides anonymity for the signer as the group can be represented by one member for signing. The blind property can protect the message to be signed as it is anonymous to the signer, but the signer cannot deny a valid signature signed by himself. Meanwhile, this scheme is based on lattice assumption, which can also guarantee the security of anti-quantum attacks.

- The correctness analysis and security proof have been given, which show that the GBS scheme can capture properties of blindness, traceability, and non-flammability. The comparison analysis and performance evaluation of key size show that the GBS scheme is efficient.

In the following, Section 2 presents the reviews of related work, Section 3 gives an anonymous model for BIoMT, Section 4 proposes a new GBS scheme, Section 5 shows the security proof and analysis, section 6 presents the efficiency comparison and performance, and Section 7 concludes.

2 Related Work

2.1 *Blockchain-Enabled Internet of Medical Things*

The distributed BIoMT platform and application are constructed by blockchain, Hyperledger, management model, cryptographic algorithm, etc. Xu et al. proposed a double chain Healthchain system for large-scale medical data management, which contains the userchain and doctorchain [5]. Using blockchain and Hyperledger Fabric, Chenthara et al. constructed a Healthchain system to protect patient privacy and medical data [6]. Li et al. established a novel peer-to-peer platform for medical data management and proposed a Stackelberg pricing algorithm to promote medical data sharing between different medical institutions [7]. Moreover, Hylock et al. presented a Healthchain system around the patient, which can help patients participate in medical data curation and dissemination [8]. Rahoof et al. established a Healthchain system using private and consortium blockchain technology for intra-regional and inter-regional communication [9]. Egala et al. proposed a Fortified-chain for security and privacy-assured IoMT based on blockchain, which mainly focuses on the access control mechanism for medical data [10]. These distributed peer-to-peer platforms give new directions to realize secure medical sharing among different medical users and institutions.

Some new frameworks are also based on blockchain and artificial intelligence (AI) technologies. Singh et al. designed a privacy-preserving model for IoT healthcare data based on federated learning and blockchain [11]. Qahtan et al. focused on security in IoT healthcare industry 4.0 systems and presented a multi-security and privacy benchmarking framework with blockchain [12]. AI-Sumaidae et al. utilized the Hyperledger fabric to perform the distributed healthcare platform with private blockchain [13]. Zhao et al. established a Brooks-Iyengar quantum Byzantine agreement-centered blockchain networking for smart healthcare [14]. Baucas et al. gave a federated learning and blockchain-enabled fog-IoT platform for wearables in predictive healthcare [15]. Although these platforms based on blockchain and AI has certain security capabilities for medical data, they cannot resist attacks from malicious adversaries with high computing power. There is also a need the cryptographic protocols, such as encryption schemes, signature schemes, and key agreement schemes, to strengthen the system security of BIoMT.

2.2 *Anonymous Authentication Protocols*

Many anonymous authentication methods exist to blind the signer's identity or message. The group signature and blind signature are standard protocols that can achieve this function. In the group signature (GS) scheme, one group member can serve as the representative to perform the signing operation. The signature can be verified valid without knowing who signs it [21]. Perera et al. gave a GS scheme with lattice assumption, which can achieve verifier-local revocation with time-bound keys [22]. Xie et al. presented a GS scheme to strengthen the security of anonymous authentication for IoT users [23]. Şahin et al. proposed dynamic GS scheme based on lattice assumptions, and applied the quantum random oracle model to show that the proposed scheme could achieve of anonymity,

traceability, and non-fremability [24]. Zhang et al. gave a GS scheme with the verifier-local revocation mechanism based on lattice assumption [25]. Tang et al. designed a GS scheme with multiple managers, which can achieve privacy-preserving for BIoMT [26]. Then, the blind signature (BS) scheme utilizes the blind factor to blind the message to be signed by the signer, which can provide anonymity for this message. Vora et al. proposed a BS scheme that depends on the hardness of big integer decomposition to protect medical data in an e-health system [27]. Li et al. constructed a BS scheme and a proxy BS scheme with lattice assumption, which can strengthen the anti-quantum property for blockchain-based systems [28,29]. Xu et al. introduced a certificateless signcryption scheme with blockchain technology to improve privacy security in an edge computing environment [30]. GS or BS only provides individual security properties for information systems, so it cannot satisfy the demands for group anonymity and message blinding.

Moreover, there also exist some group blind signature schemes, which aggregate the merits of the former two kinds of signature schemes. Kong et al. introduced a practical GBS scheme for privacy-preserving in smart grids [31]. Fan et al. applied the fast GBS scheme to construct a refreshing algorithm of dynamic nodes [32]. Kastner et al. proposed a pairing-free blind signature scheme based on the Algebraic group model. They proved it could reduce to the weakest possible assumption compared with known reduction techniques [33]. These schemes can provide both group anonymity and message blinding and improve the privacy security for users and data in information systems. However, considering the difficult authentication problems and privacy leakage in the medical data-sharing process, these protocols are unsuitable for anonymous authentication for privacy-preserving in the BIoMT system.

3 Anonymous Model for BIoMT System

This section first describes the architecture of BIoMT. Then, the anonymous authentication model is presented for BIoMT system.

3.1 Architecture of BIoMT

Fig. 1 shows the architecture of BIoMT, which mainly contains four layers for medical data management. Here, the layers are divided according the four life cycle phases of data collection, storage, share and analyze. Therefore, from the medical data generation to expiration, it generally needs to pass four layers of the perceptual, network, platform, and application. Detail function introductions of every layer are as follows:

- Perceptual layer: This layer contains the smart medical device, such as the clinical thermometer, digital blood pressure monitor, cardio kickboxing, and glucose meter. The patient's physical condition data will be collected by these devices and uploaded to the BIoMT network. This layer is the edge data collection network, which also preprocesses the data to improve their interoperability for cross-institutional data sharing. Then, First, the data transmission mode generally contains Bluetooth, WIFI, and Zigbee, and these modes upload the medical data to the data management network in the network layer.
- Network layer: This is a distributed IoMT network based on blockchain technology, and it can solve the centralized problem compared with the traditional IoMT system. An anonymous authentication model has been introduced to protect the patient's privacy. After the collection process, the medical data will be signed with the signer's private key. This model also adds the function of GBS signature to strengthen the anonymity of medical data. Here, real medical data will be stored in a native storage server, and storage address and operation behavior will

be recorded onto the blockchain ledger. Here, the user must first visit the public blockchain ledger, and then he can get the storage address and obtain real medical data. This mechanism will prevent the problems of data loss and privacy leakage by direct access to data. Meanwhile, the lightweight storage of address and operation behavior will provide data traceability and audit links and decrease the redundancy of the public blockchain ledger. This layer guarantees the security of storage and sharing processes by utilizing the distributed peer-to-peer network and untampered blockchain ledger.

- Platform layer: medical workers can access and operate the medical data from BIoMT servers through these platforms. The watch, desktop, telephone, and other mobile medical devices and apps can all link to the BIoMT network. Note that the current smartwatch can serve as a medical data management platform and a perceptual device to collect medical data. This layer connects the medical in-network layer and the application layer. A valid user can access medical data from these platforms. Meanwhile, this layer takes responsibility for presetting access control privileges, which can protect users' and medical data privacy more refined.
- Application layer: This layer contains different kinds of medical workers, such as doctors, nurses, researchers, insurance salespeople, and supervisors. These medical data can be used for disease diagnosis, scientific research, and drug development. They also provide evidence for market regulation and medical dispute tracing. Medical workers take responsibility for data management and can utilize these data for disease diagnosis and scientific research. For a piece of medical data, the signature embedded in it can help check its validity. The GBS scheme allows one group member to perform a signing operation on behalf of the group. This signature can be verified as legitimate without knowing who the signer is. Meanwhile, the blind function makes the signature anonymous to the signer.

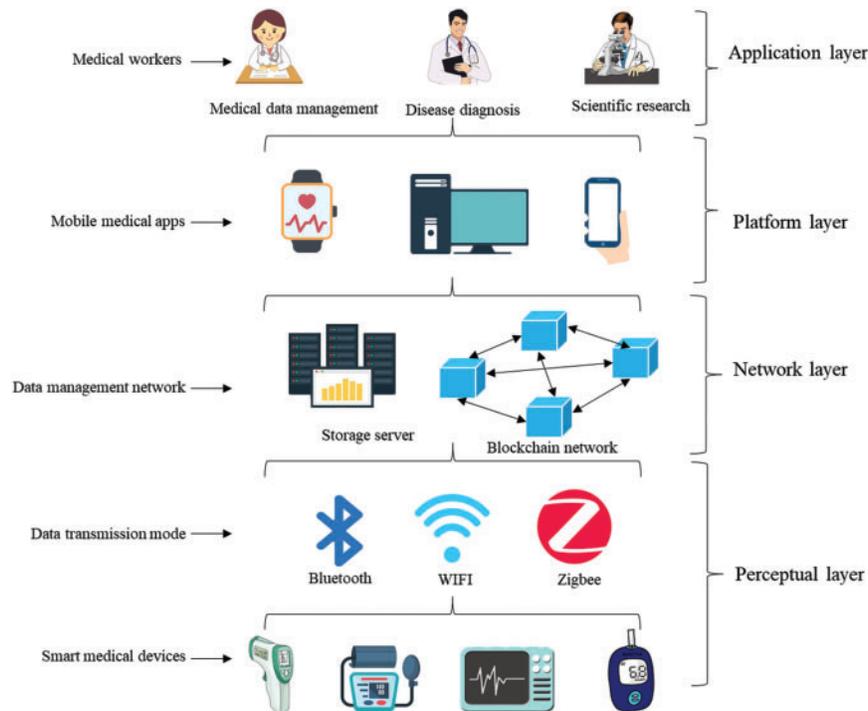


Figure 1: The architecture of BIoMT

This BIoMT performs data acquisition, storage, and management roles to support data sharing between medical institutions. The medical data are collected by the smart medical device, stored in the native storage server, shared by the distributed blockchain ledger, managed by different medical platforms, and used by different medical workers. Blockchain technology guarantees transparency and integrity, but user authentication and privacy security are still the weak aspects of BIoMT. There always exist some problems of authentication difficulties and privacy leakage in the medical data sharing process. Especially in the face of quantum computation attacks, current mathematic hard problems-based cryptographic protocols are vulnerable. An anonymous authentication model is introduced for BIoMT in the following subsection, focusing on privacy security in the network layer.

3.2 The Anonymous Authentication Model for BIoMT

The framework of the model is shown in Fig. 2. This model mainly contains an anonymous authentication scheme and an IoMT blockchain ledger. Here, the anonymous authentication scheme is established with a GBS scheme which can ensure the anonymous verifiability of the signer and the authenticity of medical data. The IoMT blockchain ledger takes responsibility for recording the data store address and operation records to guarantee storage security and traceability.

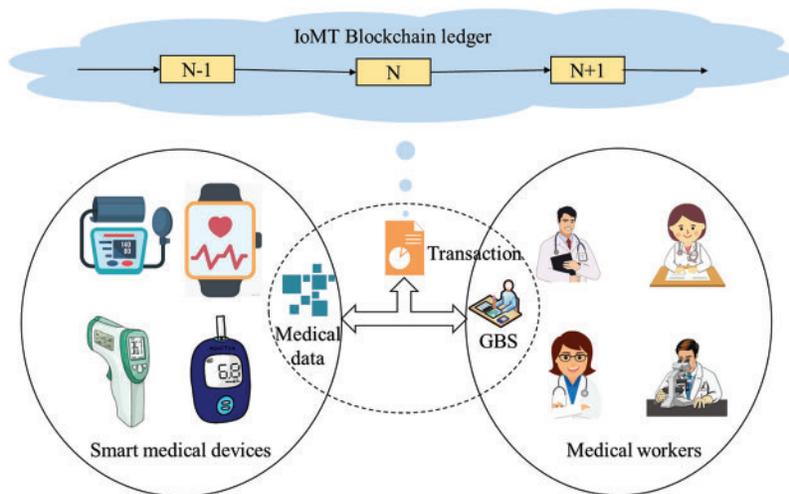


Figure 2: Anonymous authentication model for BIoMT

- **Anonymous authentication scheme:** This scheme establishes an anonymous authentication mechanism for cross-institutional medical data sharing. This scheme is a GBS scheme based on lattice assumption. When smart medical devices collect medical data, they will be signed by the corresponding medical workers. Then, the signed medical data will be uploaded and packaged into the blockchain transaction. Here, as the patient's condition needs to synthesize various detection results for comprehensive judgment, it generally needs various detection equipment to cooperate. There is also a need for some medical workers to consult together when the patient's condition is very complex. The GBS improves the security of medical data and allows one group member to sign messages. The message to be signed is also blind to the signer, which can improve medical data security. Moreover, the medical store address and operations are recorded as transactions and uploaded into the ledger. This scheme establishes an anonymous authentication mechanism for cross-institutional medical data sharing.

- **IoMT blockchain ledger:** This is a unified ledger for the whole network of BIoMT, which establishes a secure cross-institutional medical data-sharing platform. This ledger only contains lightweight messages as the storage addresses and operations records, which can improve the data sharing efficiency by a more lightweight ledger. When medical workers want to view some medical data, they can derive the original data from the storage address by obtaining access control permission. Meanwhile, they will form a hinged record ledger with time stamps and establish permanent, immutable records. This ledger can provide evidence and traceability for verifying medical data when a medical dispute arises. Every valid user can check the validity of medical data without losing any private information.

4 The Proposed Anonymous Authentication Protocol

To protect the sensitive information security, a GBS scheme based on lattice cryptography has been designed for anonymity authentication. This GBS scheme is based on lattice assumption $\mathfrak{R} - SIS_{q,n,m,\beta}^\kappa$, where κ is a uniform distribution. Meanwhile, the algorithms for $\mathfrak{R} = \mathbb{Z}$ is performed by the same work way in rings $\mathfrak{R} = \mathbb{Z}[x]/(x^n + 1)$. Although the work way becomes simple, the hardness of this lattice assumption $\mathbb{Z} - SIS_{q,n,m,\beta}^\kappa$ has not decreased. Here, the GM represents the group manager, the GG represents group guest (Signer), the GU represents group user (Message owner), the SV represents signature verifier, and the SO represents signature opener. To generate a valid group signature, these four parties perform the following six algorithms, such as **KeyGen.**, **Join**, **Blind Sign**, **Verify**, **Open**, and **Revoke**. This GBS scheme can also realize that the group members free join and revoke.

Moreover, the bimodal Gaussian distribution has been applied into the GBS scheme, which can improve the efficiency of reject sampling [34] and make the GBS scheme more efficient. Following are the detailed step descriptions of the GBS scheme.

Key Gen.: According to the rules in Ref. [35], parameters n, m, q, κ, σ are defined, where κ is security parameter, and $m = O(n \log q)$. Then, the system parameters are generated by the following steps:

- Choose a short matrix $S_A \in \mathbb{Z}_{2q}^{m \times n}$, as $\|\tilde{S}\| \leq O(\sqrt{n \log q})$;
- Generate matrix $A \in \mathbb{Z}_{2q}^{n \times m}$ such that $AS_A = A(-S_A) = qI_n \pmod{2q}$;
- Choose a short matrix $S_B \in \mathbb{Z}_{2q}^{m \times n}$;
- Generate the matrix $B \in \mathbb{Z}_{2q}^{n \times m}$ which satisfies $BS_B = B(-S_B) = qI_n \pmod{2q}$;
- Derive (U_i, S_{U_i}) according the former principle;
- Output $gpk = (A, B)$ as group public key, $gmsk = S_A$ as group master secret key, $tmsk = S_B$ as tracing manager's (opener's) secret key, $(upk_i = U_i, usk_i = S_{U_i})$ as guest i 's key pair.

Join algorithm: This algorithm contains two parts: one is that GG sends a registration message to GM, the other is that GM generates a member certificate to GG. GG also sets a leaving date and time for registration to prevent pretending by some malicious adversaries.

(1) GG performs:

- Selects vectors $x_{i_1}, x_{i_2} \leftarrow D_{\sigma_1}^m$, as $D_{\sigma_1}^m$ is the bimodal Gaussian distribution;
- Computes $y_{i_1} = S_{U_i} x_{i_1}$ and $y_{i_2} = B x_{i_2}$;
- Computes $z_i = x_{i_1} + x_{i_2}$;
- Sets a leaving date and time t_{r_i} ;
- Sends $(y_{i_1}, y_{i_2}, z_i, t_{r_i})$ to group manager.

(2) GM performs:

- Samples $r_i \leftarrow \text{SampleD}(S_A, A, qz_i, \sigma_2)$;
- Sets the revocation token $\text{Token}_i = A \cdot r_i$;
- Computes $c_{i_1} \leftarrow H(Ay_{i_1} \bmod 2q, \text{Token}_i)$ with the received y_{i_1} ;
- Selects $a \in \{0, 1\}^n$ randomly;
- Computes $w_{i_1} \leftarrow y_{i_1} + (-1)^a S_A c_{i_1}$;
- Derives (w_{i_1}, c_{i_1}) with probability $\min\left(\frac{D_{\sigma_1}^{\text{Token}_i}(w_{i_1})}{M_1 D_{c_{i_1}, \sigma_1}^{\text{Token}_i}(w_{i_1})}, 1\right)$; otherwise, restart;
- Records GG i 's registration $\text{reg}[i] \leftarrow (i, y_{i_1}, t_{r_i}, r_i, 1)$, here "1" represents this GG i is active;
- Outputs the member certificate $mc_i = (w_{i_1}, c_{i_1}, \text{Token}_i)$ for GG i .

Blind sign algorithm: This algorithm contains four parts: GG verifies the date and sends the commitment to GU, GU blind the message to be signed and sends it to GG, GG signs the blind message and returns it back to GU, and GU recover the signature for original message. GG i first verifies the validation of his member certificate $mc_i = (w_{i_1}, c_{i_1}, t_{r_i})$. Here, $\|w_{i_1}\| > T_1$ with the conditions of $T_1 = \eta\sqrt{m}\sigma_1$, and η can be verified with probability $1 - 2^{-\kappa}$ for the security parameter κ (in practice $\eta \in [1.1, 1.4]$). Next is the detailed steps of this blind sign algorithm.

1) GG performs:

- Verifies the validity of member certificate mc_i ;
- If $\|w_{i_1}\| > T_1$ or $\|w_{i_1}\|_{\infty} > q/4$, terminates and restarts Join algorithm;
- Continues iff $c_{i_1} \leftarrow H(Aw_{i_1} + qc_{i_1} \bmod 2q, A \cdot r_i)$;
- Sends (y_{i_1}, y_{i_2}) to the user.

2) GU performs:

- Selects a blind vector $y_{i_3} \leftarrow D_{\sigma_2}^m$;
- Computes $c_{i_2} \leftarrow H(Ay_{i_1} + y_{i_2} + Ay_{i_3} \bmod 2q, M)$ with the former computed (y_{i_1}, y_{i_2}) ;
- Selects $b \in \{0, 1\}^n$ randomly;
- Computes $\mu \leftarrow (-1)^b c_{i_2}$;
- Drives μ with probability $\min\left(\frac{D_{\sigma_2}^M(\mu)}{M_2 D_{c_{i_2}, \sigma_2}^M(\mu)}, 1\right)$, and sends it to GG; otherwise, restart.

3) GG performs:

- Confirms the signature expiration date $t_s < t_{r_i}$, Otherwise restart;
- GG computes $w_{i_2} \leftarrow w_{i_1} + x_{i_2} + \mu S_A$ with w_{i_1} and the former selected vector x_{i_2} ;
- Derives the blind signature (w_{i_2}, c_{i_1}, t_s) of μ with probability $\min\left(\frac{D_{\sigma_1}^m(w_{i_2})}{M_1 D_{\mu S_A, \sigma_1}^m(w_{i_2})}, 1\right)$, and sends it to GU; otherwise, restart;

4) GU performs:

- GU computes $e_i \leftarrow y_{i_3} + w_{i_2}$ with the former selected blind vector y_{i_3} .

- Recovers signature $(e_i, c_{i_1}, c_{i_2}, t_{r_i}, t_s)$ with probability $\min\left(\frac{D_{\sigma_2}^m(e_i)}{M_2 D_{y_{i_3}, \sigma_2}^m(e_i)}, 1\right)$; Otherwise, restart;

Verify algorithm: SV performs verification process and gives *Accept* or *Reject*.

- SV checks the date and time $t_v < t_s$ and $t_s < t_{r_i}$, otherwise restart;
- If $\|e_i\| > T_1$ or $\|e_i\|_{\infty} > q/4$, *Reject*
- If $c_{i_2} \leftarrow H(Ae_i + qc_{i_1} + qc_{i_2} \bmod 2q, M)$, *Accept*.

Open algorithm: Though this algorithm, it can confirm who is the real signer in the group.

- Samples $r'_i \leftarrow \text{SampleD}(S_A, A, U_i y_{i_1} + S_B y_{i_2}, \sigma_2)$;
- If $r'_i = r_i$, returns GG's index i ; Otherwise, restart.

Revoke algorithm: GM executes the following steps to change group member and records the revocation information to a list *RL*.

- Queries on $reg[i]$ to get $Token_i = A \cdot r_i$;
- Updates state (1) to inactive (0), and records $(A \cdot r_i)$ into *RL*;

5 Security Analysis

5.1 Correctness

(1) Member certificate correctness: The member certificate mc_i is valid when it satisfies three conditions. First is $\|w_{i_1}\| < T_1$, as T_1 is defined in the **Sign algorithm**. Second is $\|w_{i_1}\|_{\infty} < q/4$, as this condition is restricted system security reason. Third is $c_{i_1} \leftarrow H(Aw_{i_1} + qc_{i_1} \bmod 2q, A \cdot r_i)$, as that it is based on the following Eq. (1) holds.

$$\begin{aligned}
 Aw_{i_1} + qc_{i_1} &= A(y_{i_1} + (-1)^a S_A c_{i_1}) + qc_{i_1} \\
 &= Ay_{i_1} + (-1)^a AS_A c_{i_1} + qc_{i_1} \\
 &= Ay_{i_1} + (-1)^a qc_{i_1} + qc_{i_1} \\
 &= Ay_{i_1} \bmod 2q
 \end{aligned} \tag{1}$$

(2) Signature correctness: The signature e_i is valid for message M which also needs those three conditions holds. As in the **Verify algorithm**, the former two conditions are $\|e_i\| < T_1$ and $\|e_i\|_{\infty} < q/4$, and the third is $c_{i_2} \leftarrow H(Ae_i + qc_{i_1} + qc_{i_2} \bmod 2q, \mu)$ as the following Eq. (2) holds.

$$\begin{aligned}
 Ae_i + qc_{i_1} + qc_{i_2} &= A(y_{i_3} + w_{i_2}) + qc_{i_1} + qc_{i_2} \\
 &= Ay_{i_3} + A(w_{i_1} + x_{i_2} + \mu S_A) + qc_{i_1} + qc_{i_2} \\
 &= Ay_{i_3} + A(y_{i_1} + (-1)^a S_A c_{i_1}) + Ax_{i_2} + (-1)^b qc_{i_2} + qc_{i_1} + qc_{i_2} \\
 &= Ay_{i_3} + Ay_{i_1} + Ax_{i_2} + (-1)^a qc_{i_1} + qc_{i_1} + (-1)^b qc_{i_2} + qc_{i_2} \\
 &= Ay_{i_1} + y_{i_2} + Ay_{i_3} \bmod 2q
 \end{aligned} \tag{2}$$

Meanwhile, the signature is correct, which also needs the following conditions to hold. Firstly, a user with a fake expiration date cannot pass verification as the new guest has set a leaving date and time t_{r_i} for the member certificate. Secondly, the signature generation time t_s is verified at step 1 of **Sign algorithm**, only the no expired group member can perform the following signing steps. Thirdly, the verification time t_v is compared with signature generation time t_s . If the user does not have a correct

signature expiration date, he will be rejected. Moreover, the signature cannot be accepted, created by the revoked group member whose revocation token is in list RL .

(3) Opening correctness: On inputting $tmsk = S_B$, the signature is generated by guest i if $r'_i = r_i$, where $r'_i \leftarrow \text{SampleD}(S_A, A, U_i y_{i_1} + S_B y_{i_2}, \sigma_2)$. The correctness of that open algorithm is based on the following Eq. (3).

$$U_i y_{i_1} + S_B y_{i_2} = U_i S_{U_i} x_{i_1} + B S_B x_{i_2} = q x_{i_1} + q x_{i_2} = q (x_{i_1} + x_{i_2}) = q z_i \text{mod} 2q \quad (3)$$

5.2 Security Proof

This section provides the security proof of the proposed GBS scheme to show it can achieve dynamical-almost-full anonymity, blindness, traceability and non-frameability.

(1) Dynamical-almost-full anonymity: With the free joining and revoking mechanism, one signature cannot be confirmed which group member is the signer, and two different signatures cannot be distinguished who is the real signer between two different signers without the information of group muster's secret key.

Theorem 1: *In random oracle model, this GBS scheme can capture dynamical-almost-full anonymity with the hardness of $\mathfrak{R} - SIS_{q,n,m,\beta}^k$.*

Proof: A query-respond game has been established between the adversary A and challenger C , and challenger can utilize the forged signature created by adversary to solve $\mathfrak{R} - SIS_{q,n,m,\beta}^k$ instance with non-negligible probability. Detailed proving processes are shown as follows.

Game 0: Suppose adversary A can get some information of usk . Based on the hardness of $\mathfrak{R} - SIS_{q,n,m,\beta}^k$, A cannot distinguish that one signature's real signer is user i_0 or user i_1 by the query-respond game with C . Meanwhile, A can add new user into the group, and perform queries on the opened signatures and member's revocation token. If A asks to add a new user, C first confirms whether this user's identity is registered or not. C performs registration process to generate the registration information when this identity does not exist and returns it back. C also establish an empty registration list $List_{RU}$ to store the registration information. Here, the returned registration information does not contain the revocation token and key-expiration time. When A asks to reveal the revocation token for user i , C checks $List_{RU}$ and finds out user i 's registration information. He returns member certificate mc_i back, and updates $List_{RU}$. Then, C gives two challenge indices (i_0, i_1) with relate to M , and derives signature $(e_i^*, c_{i_1}^*, c_{i_2}^*, t_{r_i}^*, t_s^*)$ with a random $\tau \leftarrow \{0, 1\}$ when he confirms that (i_0, i_1) are newly recorded in $List_{RU}$. After that, A gives his guess $\tau' \leftarrow \{0, 1\}$. It will derive 1 when $\tau' = \tau$, and 0 when $\tau' \neq \tau$. Moreover, A needs to give two different expiration dates for indices i_0 and i_1 . A cannot pass validation process if he does not provide a right key-expiration date which should satisfy $t_{r_i} > t_s \geq t_v$. Even worse, A provides two correct expiration dates, C will derive challenging signature for verification. A will attack the anonymity of signer in this GBS scheme with time-bound keys.

Game 1: C executes **KeyGen.** and derives key pair $(U_i^*, S_{U_i}^*)$ for the challenging signature. If A performs query on an opened signature (e_i, M) , C will quit and select a random bit as response. Note that it cannot distinguish this game with **Game 0**. Next, C performs the following games.

Game 2: C executes **Join algorithm** to answer for the query on random oracle H . If A performs query on an opened signature (e_i, M) , C calculates $c_{i_2} \leftarrow H(Ay_{i_1} + y_{i_2} + Ay_{i_3} \text{mod} 2q, M)$. Meanwhile, C executes **Join algorithm** and calculates $H(Ay_{i_1} \text{mod} 2q, A \cdot r_i)$ to get c_{i_1} . Next, C derives signature $(e_i, c_{i_1}, c_{i_2}, t_{r_i}, t_s)$ as response. Here, A cannot get anything from this collision-resistant random oracle

as he has nothing about the newly registered user. Note that it cannot distinguish this game with the former two games.

Game 3: As $e_i \leftarrow y_{i_3} + w_{i_2}$ is related with y_{i_3} and w_{i_2} . C randomly chooses a blind vector for y_{i_3} , and executes the **Blind sign algorithm** to generate w_{i_2} . Meanwhile, C can compute w_{i_1} from the following

Game 4, and derives (e_i, c_{i_1}, c_{i_2}) with probability $\min\left(\frac{D_{\sigma_2}^m(e_i)}{M_2 D_{y_{i_3}, \sigma_2}^m(e_i)}, 1\right)$. Note that it cannot distinguish

this game with the former games.

Game 4: C randomly selects a vector r_i^* and calculates $Token_i = Ar_i^*$. Then, C calculates $w_{i_1} \leftarrow y_{i_1} + (-1)^a S_A c_{i_1}$ with y_{i_1} and c_{i_1} , here c_{i_1} is derived with $Token_i^*$ from **Game 2**. The generation probability of (w_{i_1}, c_{i_1}) is $\min\left(\frac{D_{\sigma_1}^{Token_i}(w_{i_1})}{M_1 D_{c_{i_1}, \sigma_1}^{Token_i}(w_{i_1})}, 1\right)$.

Game 5: As C generates $Token_i$ with challenging bit τ , e_i is derived uniformly. C chooses a random vector $\eta \in \mathbb{Z}_q^n$ and sets $e_i = \eta$. Here, (e_i, c_{i_1}, c_{i_2}) is a proper $\mathfrak{R} - SIS_{q,n,m,\beta}^k$ instance. If A can find a solution for this hard problem, he can make a correct distinction between e_i and η . Note that it cannot distinguish this game with the former games.

Game 6: e_i^* is generated independently with τ . Note that it cannot distinguish this game with the former games. Therefore, it is impossible for A to forge a valid signature as $\mathfrak{R} - SIS_{q,n,m,\beta}^k$ is hard.

Now, it can say that this GBS scheme can capture dynamical-almost-full anonymity.

(2) Blindness

Blindness: The signer cannot deny his signature inserted in one message which he does not know what it is, here this signature can be verified to be true.

Theorem 2: *In random oracle model, this GBS scheme can capture statistically blind with the hardness of $\mathfrak{R} - SIS_{q,n,m,\beta}^k$.*

Proof: Suppose adversary $Adv_{BS}^{blind}(S^*)$ can interact with two different users u_0 and u_1 , it can prove that signatures e_0 and e_1 generated by two users cannot be distinguished. The blind message μ_0 and

μ_1 are generated with probability $\min\left(\frac{D_{\sigma_1}^m(w_{i_2})}{M_1 D_{\mu S_A, \sigma_1}^m(w_{i_2})}, 1\right)$. As $\mu \leftarrow (-1)^b c_{i_2}$, it tailors

μ_0 and μ_1 to be distributed according to the same distribution $D_{\sigma_2}^m$ by rejection sampling lemma [34]. Therefore, it can derive $\Delta(\mu_0, \mu_1) = 0$, and these two blind messages are distributed independently from the original message. Then, from the blind sign and revoke steps, the blind signature (w_{i_2}, c_{i_1}, t_s)

is generated by $w_{i_2} \leftarrow w_{i_1} + x_{i_2} + \mu S_A$ with probability $\min\left(\frac{D_{\sigma_1}^m(w_{i_2})}{M_1 D_{\mu S_A, \sigma_1}^m(w_{i_2})}, 1\right)$, and the signature

$(e_i, c_{i_1}, c_{i_2}, t_{r_i}, t_s)$ generated by $e_i \leftarrow y_{i_3} + w_{i_2}$ with probability $\min\left(\frac{D_{\sigma_2}^m(e_i)}{M_2 D_{y_{i_3}, \sigma_2}^m(e_i)}, 1\right)$. It can derive two

signatures e_0 and e_1 which also satisfy $\Delta(e_0, e_1) = 0$. Meanwhile, they are independent from the original message to be signed. Now, it can say that this GBS scheme can capture statistically blind to the attacks from adversary S^* .

(3) Traceability

Traceability: The signer with relate to one valid signature can be confirmed by the open algorithm, and he cannot deny this signature.

Theorem 3: *In random oracle model, this GBS scheme is traceable with the hardness of $\mathfrak{R} - SIS_{q,n,m,\beta}^k$.*

Proof: Suppose adversary A can forge a valid signature, and he has ability to add new group user by replacing user's upk . Meanwhile, the revocation token can also be queried by A . Next, challenger C_1 utilizes a pseudo polynomial time (PPT) algorithm to perform a query-answer game with A to solve $\mathfrak{R} - SIS_{q,n,m,\beta}^k$ instance. A can execute queries on the **KeyGen.**, **Join**, and **Blind sign algorithms** with enough times, and C_1 responds them one by one. Then, A can forge a signature $(e'_i, c'_{i_1}, c'_{i_2}, t'_{r_i}, t'_s)$ for M' with enough queried information. With the former hypothesis, this signature (e'_i, M') derived by A is valid. Now, C_1 can create a new valid signature (e_i^*, M) with $(e_i^*, c_{i_1}^*, c_{i_2}^*, t_{r_i}^*, t_s^*)$ by Forking Lemma [36]. Hence, C_1 obtains two equations $U_i y'_{i_1} + S_B y'_{i_2} = qz'_i \text{ mod } 2q$ and $U_i y_{i_1}^* + S_B y_{i_2}^* = qz_i^* \text{ mod } 2q$, and then generates two vectors z'_i and z_i^* ($z'_i \neq z_i^*$) respectively. There also has $A(r'_i - r_i^*) = q(z'_i - z_i^*) \text{ mod } 2q$. Here, it has $r'_i - r_i^* \neq 0 \text{ mod } 2q$ as $z'_i \neq z_i^*$, and $v = r'_i - r_i^*$ is a solution for $\mathfrak{R} - SIS_{q,n,m,\beta}^k$ instance as $Av = 0 \text{ mod } 2q$. However, this is impossible with current computation. So the hypothesis for adversary A fails, and the GBS scheme is traceable.

(4) Non-frameability

Non-frameability: It cannot generate a legitimate signature by impersonating other people, no matter the group manager and other members.

Theorem 4: *In random oracle model, this GBS scheme can capture non-frameability with the hardness of $\mathfrak{R} - SIS_{q,n,m,\beta}^k$.*

Proof: Suppose adversary A can forge a valid signature. This signature also opens to user i , but this user has never generated the signature. Then, there exists a challenge PPT algorithm C_2 which can solve SIS problem from the query-answer game with A . A signs up a new user i by working as the corrupted group member, and makes some queries to the main algorithms in the GBS scheme. C_2 answers the queries with the system keys gpk , $gmsk$ and $tmsk$. When A asks for a signature with relate to message M , C_2 generates and sends back the corresponding signature $(e'_i, c'_{i_1}, c'_{i_2}, t'_{r_i}, t'_s)$. A makes these queries for many times, and obtains enough information for the system keys. Next, A forges a signature $(e''_i, c''_{i_1}, c''_{i_2}, t''_{r_i}, t''_s)$ for the target message C_2 which opens to user i^* . Based on the former assumption for A , (e'_i, M') is a legitimate signature with overwhelming probability. As C_2 also can generate a legitimate signature (e_i, M) , it can derive $H(Ae''_i + qc''_{i_1} + qc''_{i_2} \text{ mod } 2q, M'') = H(Ae_i + qc_{i_1} + qc_{i_2} \text{ mod } 2q, M)$. Then, there will exist $Ae''_i + qc''_{i_1} + qc''_{i_2} = Ae_i + qc_{i_1} + qc_{i_2}$ because it does exist hash collision. Meanwhile, it also can derive $A(e''_i - e_i) = 0 \text{ mod } 2q$ as $c''_{i_1} = c_{i_1}$ and $c''_{i_2} = c_{i_2}$. Until now, C_2 finds out a solution for the $\mathfrak{R} - SIS_{q,n,m,\beta}^k$ instance.

6 Efficiency Comparison

This section provides the efficiency comparison between the proposed GBS with the other three similar schemes. Key size is an essential index to reflect the scheme performance as that more small

key size leads to more efficient scheme performance. Here, the parameters n, m, q, σ in [22,23], and the proposed GBS are unified and the parameter k and l in [24] are converted with the principle of $k = 0.96n$ and $l = m$. Then, the key comparison results with some other similar schemes are shown in Table 1. As for the gpk and $gmsk$, the proposed GBS is a little bigger than those in the other two schemes. But the keys' distribution with bimodal Gaussian by modeling $2q$ can make the scheme more secure. As for the $tmsk$, its size in the proposed GBS is nearly half of that in Ref. [23]. As for the signature size, the proposed GBS has a great advantage in the signature verification efficiency with more small size.

Table 1: Key size comparison

Protocol	gpk	$gmsk$	$tmsk$	Signature
Perera et al. [22]	$mnlogq$	$m \cdot nlogq$	$mnlogq$	$mlogq + 3m \log(12\sigma)$
Xie et al. [23]	$mnlogq$	$mnlogq$	$2mnlogq$	$(n + 2m) \log q$
Şahin et al. [24]	$0.96mnlogq$	$0.96mnlogq$	$0.96mnlogq$	$(0.96mn + 2m) \log q$
This GBS scheme	$mnlog2q$	$mnlog2q$	$mnlog2q$	$2m \log(12\sigma)$

Then, to clearly view the difference between the proposed GBS scheme with similar three schemes. The performance environment is a Windows 10 desktop with Intel(R) Core (TM) i7 CPU 3.2 GHz and 16G RAM. The key size is performed on Matlab R2016a with two security levels of 80-bit and 192-bit, where the parameters n and q are setting as $n = 512, q = 2^{23}$ and $n = 1024, q = 2^{27}$ respectively. The parameter $m = 3545$ for 80-bit and $m = 8323$ for 192-bit as it satisfies $m \geq n \lceil \log q \rceil$, the message length is preset to $l = 80$, and $\sigma = 2^{30}$ is set according the principle in [29]. From the performance results in Fig. 3, gpk is almost the same, and $tmsk$ in GBS scheme is smaller than [23]. Furthermore, the signature size comparison is shown independently in Fig. 4, and the signature size in the GBS scheme has more advantages than the other two similar schemes. As the $gpk, gmsk,$ and $tmsk$ can be pre-generated to save algorithm time, the signature size makes essential effects on the signature generation and verification. Therefore, the small signature size in the GBS scheme can improve the efficiency.

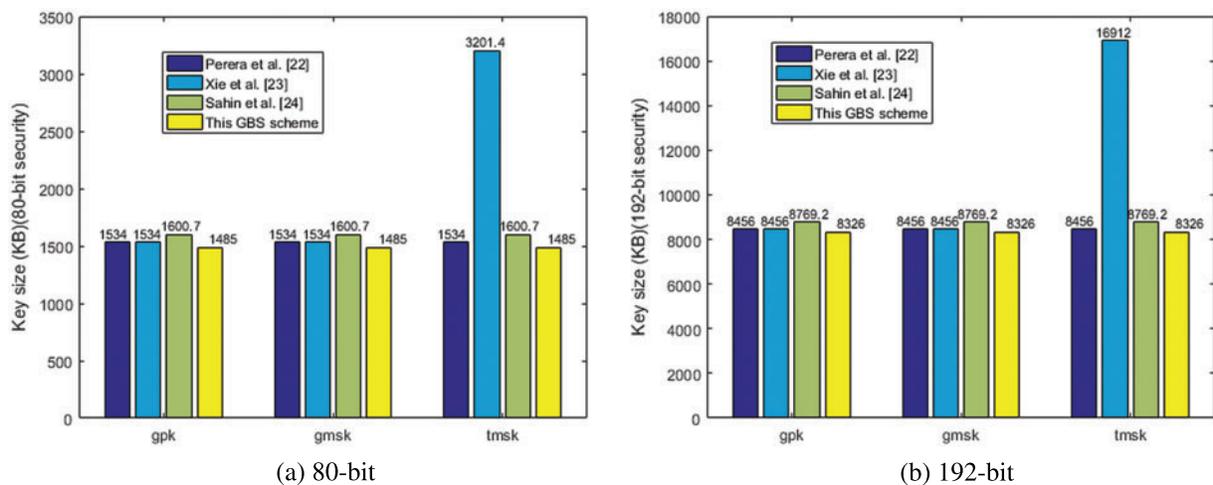


Figure 3: Key size comparison with two different security level

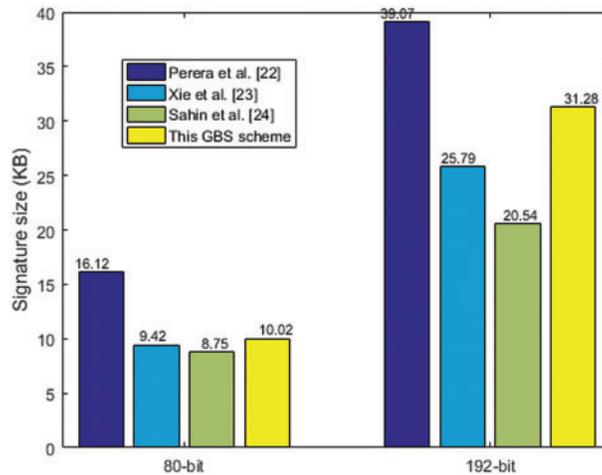


Figure 4: The signature size comparison

7 Conclusion

This paper solves the problems of authentication difficulty and privacy leakage in the BIoMT system. A four-ledger architecture for the BIoMT system is introduced first, which contains the perceptual, network, platform, and application. Meanwhile, an anonymous authentication model has been designed to strengthen the security of the data-sharing process in the network ledger. This model integrates the anonymous authentication scheme and untampered blockchain ledger, which can guarantee the traceability of the signature and the anonymity of the signer's identity privacy at the same time. Then, a GBS scheme has been proposed to achieve anonymous authentication. It keeps the signer's anonymity through the group representative signing mechanism and protects data privacy with the message binding mechanism. Moreover, the security proof and analysis show that this GBS scheme can capture the needed security properties of dynamical-almost-full anonymity, blindness, traceability, and non-frameability. The efficiency comparison and performance evaluation of key size show that the proposed anonymous authentication model and signature scheme are efficient and practical.

With the number of smart medical devices increasing, the security problems of privacy leakage, data loss, and unauthorized access have become more and more serious. To maximize the value of medical data, privacy security, identity authentication, and access control are the main security issues that should be put into continuous efforts. Therefore, there still exist some exciting research directions in BIoMT, such as the data fine-grained access control, anonymous authentication, and lightweight storage in the cross-institutional sharing process.

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