



Numerical Computation of SEIR Model for the Zika Virus Spreading

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Abstract: The purpose of this study is to present the numerical performances and interpretations of the SEIR nonlinear system based on the Zika virus spreading by using the stochastic neural networks based intelligent computing solver. The epidemic form of the nonlinear system represents the four dynamics of the patients, susceptible patients $S(y)$, exposed patients hospitalized in hospital $E(y)$, infected patients $I(y)$, and recovered patients $R(y)$, i.e., SEIR model. The computing numerical outcomes and performances of the system are examined by using the artificial neural networks (ANNs) and the scaled conjugate gradient (SCG) for the training of the networks, i.e., ANNs-SCG. The correctness of the ANNs-SCG scheme is observed by comparing the proposed and reference solutions for three cases of the SEIR model to solve the nonlinear system based on the Zika virus spreading dynamics through the knacks of ANNs-SCG procedure based on exhaustive experimentations. The outcomes of the ANNs-SCG algorithm are found consistently in good agreement with standard numerical solutions with negligible errors. Moreover, the procedure's constancy, dependability, and exactness are perceived by using the values of state transitions, error histogram measures, correlation, and regression analysis.

Keywords: SEIR nonlinear system; Zika virus; artificial neural networks; scaled conjugate gradient; statistical measures

1 Introduction

The coronavirus is known as one of the quickly spreading diseases. Adequate and appropriate processes and proper treatment are required to avoid its spread and control. To manage the affected



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population's probability, the epidemic with the function of therapy is displayed. Prospects reveal how many individuals based on the afflicted classes have gone for the cure. Few of the traditional samples provide the treatment ratios, which are proportional to the affected number of patients [1]. The medical possessions indicate the treatment of such viruses, which are moderately controlled in the whole world [2]. Concludingly, the lack of preparedness and resources for any unexpected outbreak reasons the deaths. The Zika virus was discovered by the Uganda Rhesus macaques group in the mid of the last century [3]. The vectors of the mosquito are responsible for the Zika transmission using the "Aedes". The clinical indications of the Zika-based virus are familiar to individuals suffering from dengue fever. The progression ratio of dengue fever in the humans between 3 to 12 days. Almost 1/4 individuals suffer a Zika virus infection with the use of its common symptoms [4,5]. The human infection is dangerous during the transplacental transmission or child transfer through mother to kids [6]. Few features of the Zika virus are linked to the Chikungunya virus and dengue [7].

Currently, there is no definitive treatment for the Zika virus with the exclusion of controlling the vectors by using insecticide spray along with the extinguishing habitats of the larval breeds. In recent investigations, pregnant women, particularly present vulnerable to the infection of Zika virus infection [8–10]. The mathematical form of the models has become a growing factor in this work by using disease epidemiology and its control [11–15]. Lee et al. [16] designed a Zika virus model to consider human and vector population dynamics. He concluded the digital investigations to reduce the disease spreading. Sun et al. [17] proposed and discovered a mathematical system based on sheep brucellosis, which is used in the process of proportion and immigration. Li et al. [18] suggested that cattle and sheep use the multiple groups of the brucellosis system to avoid cross-infection with a better way to evade the undulant fever.

Moreover, the researchers considered indirect/direct transmission forms through diseased animals and environmental viruses. The best control policies are vaccination, elimination, reduction in migration, and disinfection. Xing et al. [19] proposed a mathematical model for the avian influenza spread dynamics. Temperature cycling is the primary reason for the sickness and dealers. Alternatively, Sun et al. [20] established the transmission cholera system to highlight the virus dynamics in China. The researcher's community investigated the increasing immunization coverage rate and the managing environment to prevent disease spreading. Yu et al. [21] presented the sophisticated behavior based on the biological systems due to the numerous limit cycle bifurcation along with the predator-prey simple system. Li et al. [22] proposed the SIR nonlinear system using the recovery and incidence rates.

The performances of computations are based on the SEIR nonlinear system using the Zika virus spreading through the computational artificial neural networks (ANNs) and the scaled conjugate gradient (SCG), ANNs-SCG scheme. Recently, stochastic solvers have been famous due to the variety of stiff-natured problems [23–25]. The computing solvers have been used to present the solutions of various complicated models, e.g., food supply systems [26], dynamical HIV nonlinear systems [27,28], periodic differential models [29–31], thermal explosion networks [32], a corneal form of the eye surgery model [33,34], smoking dynamical nonlinear system [35] and singular stiff models [36]. The authors are motivated to present the stochastic applications for the SEIR nonlinear system based on the Zika virus spreading. The computing numerical performances are examined in this study using the ANNs-SCG to solve the SEIR nonlinear system of the Zika virus spreading.

1.1 Motivation and Innovative Contributions

A few motivational aspects and novel features of the SEIR nonlinear system based on the Zika virus spreading using the artificial neural networks (ANNs) enhanced by the scaled conjugate gradient (SCG), ANNs-SCG approach are presented:

- The numerical representations of the SEIR nonlinear system based on the spreading of the Zika virus have been described/presented/analyzed using the ANNs-SCG stochastic solver.
- Different cases and scenarios of the spreading of the Zika virus have been numerically simulated using the ANNs-SCG stochastic solver for a better understanding of the dynamics.
- The stochastic solver’s exactness is authenticated by comparing the obtained reference solutions.
- The values based on the absolute error for each dynamic of the SEIR nonlinear system of the Zika virus spreading have been observed in good negligible ranges by using the ANNs-SCG scheme.
- The constancy of the scheme is authenticated through the values of state transitions, error histograms measures, correlation, and regression analysis.

1.2 Organization

The other paper parts are presented: Section 2 provides the mathematical model. Section 3 shows the proposed stochastic methodology. Section 4 designates the results and discussions of the model. The conclusions along with future research studies are presented in the final Section.

2 System Model: Nonlinear Zika Virus Dynamics

This section performs both forms of infection based on vector-to-human and human-to-human transmission. This model is categorized based on the total population of the human ($N_H(y)$), vulnerable humans $S_H(y)$, exposed humans $E_H(y)$, infected humans $I_H(y)$, and recovered humans $R_H(y)$, i.e., $N_H(y) = S_H(y) + E_H(y) + I_H(y) + R_H(y)$. The mosquito total population is represented by $N_V(y)$, which is given in three vector classes: susceptible $S_V(y)$, exposed $E_V(y)$, and infected $I_V(y)$, i.e., $N_V(y) = S_V(y) + E_V(y) + I_V(y)$. The mathematical form of the model is provided as follows in Eq. (1), while the SEIR nonlinear system based on the Zika virus spreading is tabulated in Table 1 as [37]:

$$\left\{ \begin{array}{l} \frac{dS_H(y)}{dy} = A_H - S_H(y) \beta_H (I_V(y) + \rho I_H(y)) - \mu_H S_H(y), \quad (S_H)_0 = k_1, \\ \frac{dE_H(y)}{dy} = \beta_H (\rho I_H(y) + I_V(y)) S_H(y) - (\chi_H + \mu_H) E_H(y), \quad (E_H)_0 = k_2, \\ \frac{dI_H(y)}{dy} = \chi_H E_H(y) - (\eta + \mu_H + \gamma) I_H(y), \quad (I_H)_0 = k_3, \\ \frac{dR_H(y)}{dy} = -\mu_H R_H(y) + \gamma I_H(y), \quad (R_H)_0 = k_4, \\ \frac{dS_V(y)}{dy} = A_V - \beta_V I_H(y) S_V(y) - \mu_H S_V(y), \quad (S_V)_0 = k_5, \\ \frac{dE_V(y)}{dy} = \beta_V I_H(y) S_V(y) - (\mu_V + \delta_H) E_V(y), \quad (E_V)_0 = k_6, \\ \frac{dI_V(y)}{dy} = E_V(x) \delta_V - \mu_V I_V(x), \quad (I_V)_0 = k_7. \end{array} \right. \tag{1}$$

The necessary definitions of the terms in the SEIR nonlinear system (1) based on the Zika virus spreading are tabulated in [Table 1](#) as reported in [37].

While theoretical convergence and further descriptions based on the parametric values using the global and local stability can be seen in the reported study [37] for interested readers.

Table 1: Parameter descriptions of the SEIR nonlinear system based on the Zika virus

Parameters	Details
$S_H(y)$	Susceptible humans
$S_V(y)$	Susceptible vector
$E_H(y)$	Exposed humans
$E_V(y)$	Exposed vector
$I_H(y)$	Infected humans
$I_V(y)$	Infected vector
$R_H(y)$	Recovered humans
A_H	Susceptible: Humans recruiting
ρ	Susceptible: Humans to infection
β_H	Susceptible humans to infected mosquitoes
μ_H	Humans: Mortality rate
χ_H	Infected human ratio to susceptible mosquitoes
η	Treatment
γ	Natural rate
β_V	Transmission ratio of the Infected humans to susceptible vector
δ_H	Mortality rate persuaded in people
μ_V	Natural rate of mortality using the vector compartment
δ_V	Susceptible mosquitos' recruitment
$k_i, i = 1, 2, \dots, 7$	Initial conditions
y	Time

3 Methodology

The proposed computing scheme for solving the SEIR nonlinear system based on the Zika virus spreading is presented in two phases.

- The process of the artificial neural networks (ANNs) and the scaled conjugate gradient (SCG), ANNs-SCG computing scheme is provided along with extensive and critical explanations.
- The numerical representations through the ANNs-SCG computing scheme for the SEIR nonlinear system based on the Zika virus spreading are provided.

A suitable procedure based on the flow structure for the ANNs-SCG computing scheme for the SEIR nonlinear system using the Zika virus spreading is described in [Fig. 1](#). The ANNs-SCG computing scheme is applied through the 'nftool' 'MATLAB' build-in command with a single hidden

layer, single input, and output layer structure, 12 hidden neurons, activation/kernel function of log-sigmoid, n-fold cross authentication with $n = 0, 1000$ iterations and optimization of the scaled conjugate gradient algorithm for training/learning of ANNs weights. The default stoppage limits, step size, and tolerances are applied to label the data, training for targets and inputs through the standard numerical results. The dataset selection is divided into three parts, 11% for testing, 72% for training, and 17% for validation. The hidden layers and output/input layers are presented for the SEIR nonlinear system based on the Zika virus through the ANNs-SCG shown in Fig. 2.



Figure 1: Designed ANNs-SCG procedure for the SEIR nonlinear system based on the Zika virus

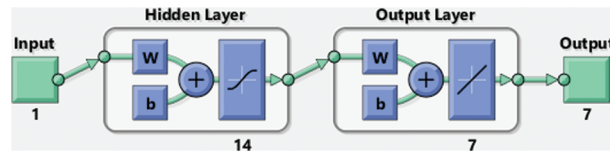


Figure 2: Layer structure of the SEIR nonlinear system based on the Zika virus

4 Numerical Simulations

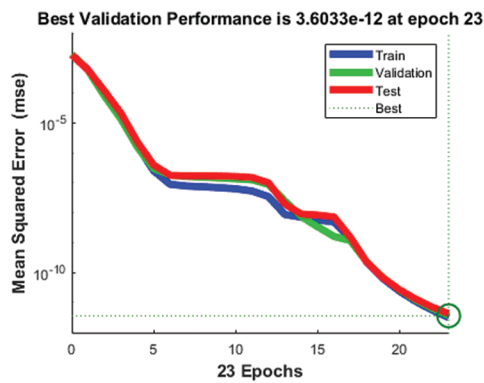
The numerical explanations are provided for solving the SEIR nonlinear system based on the Zika virus using the stochastic scheme. The mathematical form of the SEIR nonlinear systems is presented in three cases with different sets of initial conditions:

Case 1: Consider the SEIR nonlinear system based on the Zika virus with $\beta_H = 0.12$, $A_H = 0.1$, $\mu_H = 0.1$, $\chi_H = 0.13$, $\rho = 0.14$, $\eta = 0.15$, $\beta_V = 0.2$, $\gamma = 0.17$, $\delta_H = 0.22$, $\delta_V = 0.3$, $\mu_V = 0.25$, $k_1 = 0.1$, $k_2 = 0.12$, $k_3 = 0.14$, $k_4 = 0.16$, $k_5 = 0.18$, $k_6 = 0.2$ and $k_7 = 0.22$ is presented as:

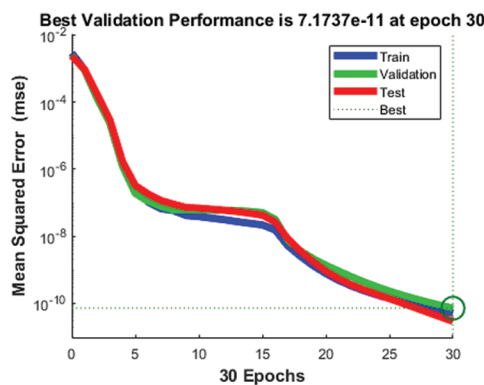
Case 2: Consider the SEIR nonlinear system based on the Zika virus with $\beta_H = 0.12$, $A_H = 0.1$, $\mu_H = 0.1$, $\chi_H = 0.13$, $\rho = 0.14$, $\eta = 0.15$, $\beta_V = 0.2$, $\gamma = 0.17$, $\delta_H = 0.22$, $\delta_V = 0.3$, $\mu_V = 0.25$, $k_1 = 0.12$, $k_2 = 0.14$, $k_3 = 0.16$, $k_4 = 0.18$, $k_5 = 0.20$, $k_6 = 0.22$ and $k_7 = 0.24$ is presented as:

Case 3: Consider the SEIR nonlinear system based on the Zika virus with $\beta_H = 0.12$, $A_H = 0.1$, $\mu_H = 0.1$, $\chi_H = 0.13$, $\rho = 0.14$, $\eta = 0.15$, $\beta_V = 0.2$, $\gamma = 0.17$, $\delta_H = 0.22$, $\delta_V = 0.3$, $\mu_V = 0.25$, $k_1 = 0.14$, $k_2 = 0.16$, $k_3 = 0.18$, $k_4 = 0.20$, $k_5 = 0.22$, $k_6 = 0.24$ and $k_7 = 0.26$ is presented as:

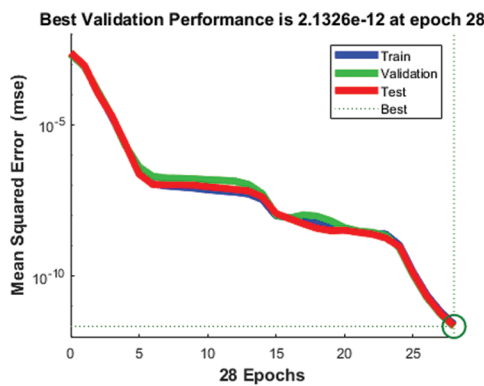
The numerical solutions of the SEIR nonlinear system based on the Zika virus are presented by using the artificial neural networks (ANNs) and the scaled conjugate gradient (SCG), ANNs-SCG with input intervals 0 and 1. Figs. 3 to 7 indicate the graphical performances of the SEIR nonlinear system based on the Zika virus spreading through the ANNs-SCG approach. The capable performances of each dynamic based on the SEIR nonlinear system based on the Zika virus are presented in Fig. 3 by taking the states of transitions and performances. The obtained measures based on mean square error (MSE) using the performances of best curves, authentication, testing, and training are presented in Figs. 3a–3c. The state transitions measures are derived in Figs. 3d–3f for the SEIR nonlinear system based on the Zika virus. The best measures based on different performances to present the solutions of the SEIR nonlinear system of the Zika virus at iterations 23, 30, and 28 were found as 3.60328×10^{-12} , 7.17372×10^{-11} , and 2.13257×10^{-12} . The gradient measures of the SEIR nonlinear system based on the Zika virus, are calculated as 7.7856×10^{-08} , 9.0585×10^{-08} , and 6.7981×10^{-08} . These graphical plots provide the convergence measures, exactness, and accuracy performances of the designed ANNs-SCG approach to solving the SEIR nonlinear system of the Zika virus spreading. The fitting curve performances are presented in Figs. 5a–5c for each dynamic of the SEIR nonlinear system of the Zika virus spreading through the ANNs-SCG. The values based on the maximum error are derived based on the training, authentication, and testing for the Zika virus spreading through the ANNs-SCG. Fig. 4d–4f is provided the SEIR nonlinear system based on the Zika virus spreading using the ANNs-SCG. The EHs performances for respective cases are performed as 2.82×10^{-07} , 2.27×10^{-06} , and 2.86×10^{-07} , respectively.



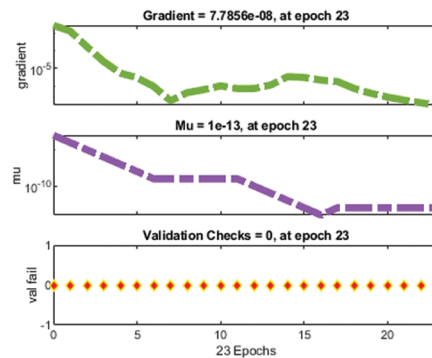
(a) Case 1: MSE



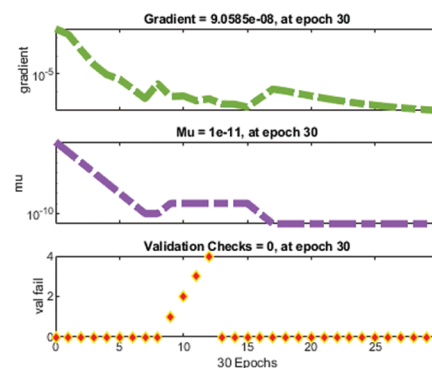
(b) Case 2: MSE



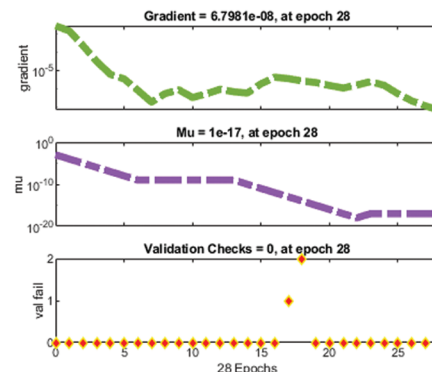
(c) Case 3: MSE



(d) STs: Case 1

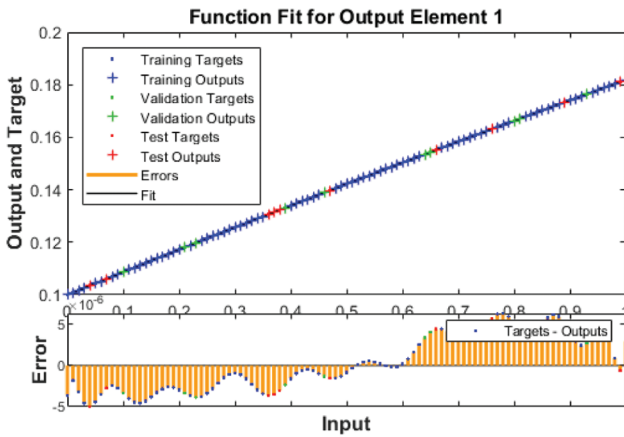


(e) STs: Case 2

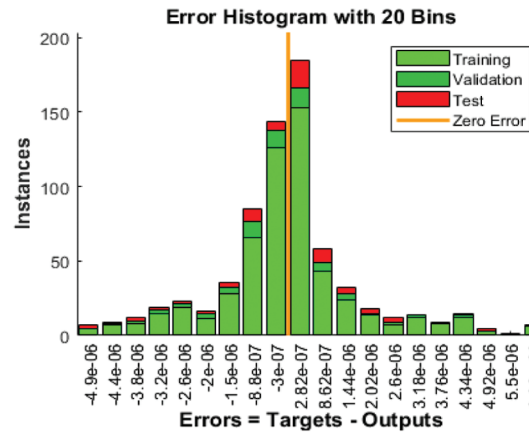


(f) STs: Case 3

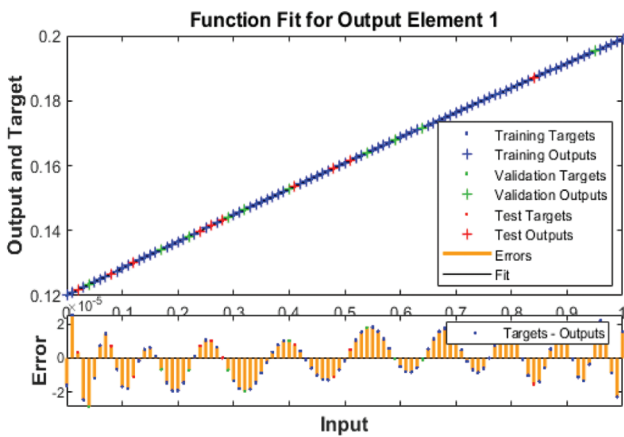
Figure 3: MSE and STs of the SEIR nonlinear system based on the Zika virus spreading



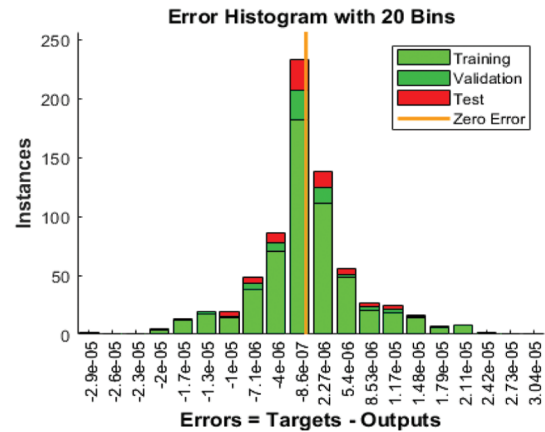
(a) Case 1: Results



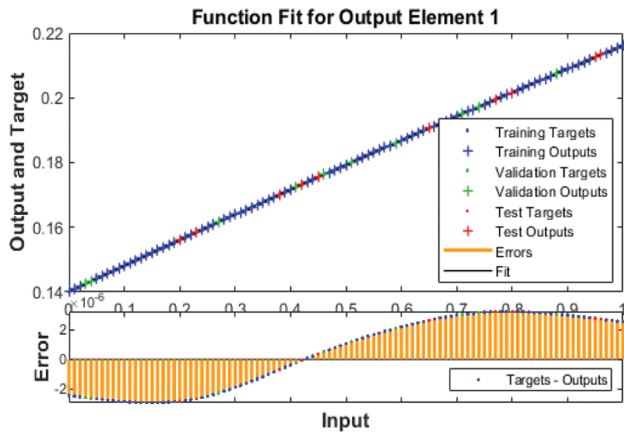
(d) EHs: Case 1



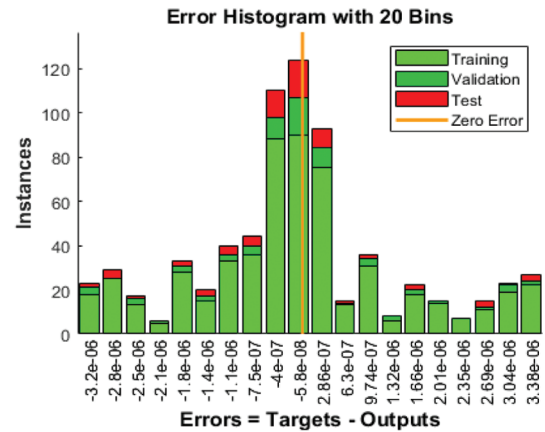
(b) Case 2: Results



(e) EHs: Case 2



(c) Case 3: Results



(f) EHs: Case 3

Figure 4: Result performances and EHs based on the SEIR nonlinear system of the Zika virus spreading

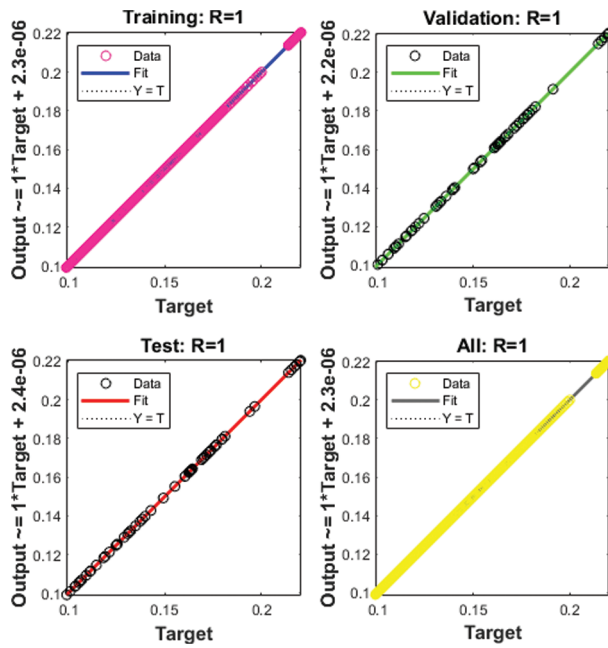


Figure 5: Regression for Case 1

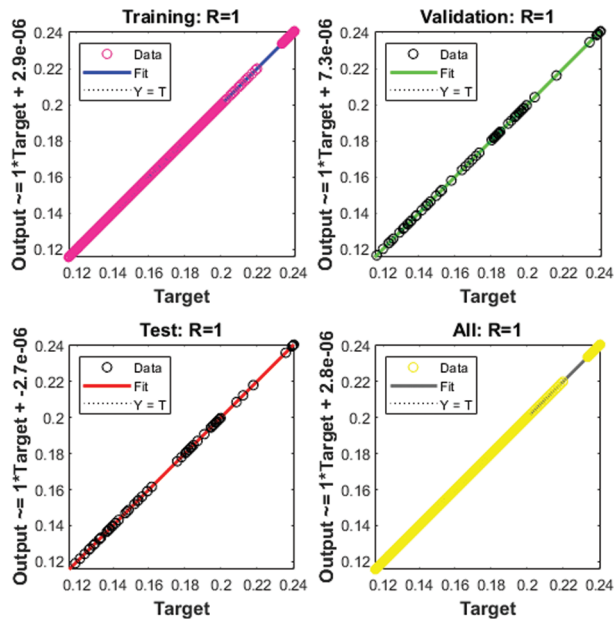


Figure 6: Regression for Case 2

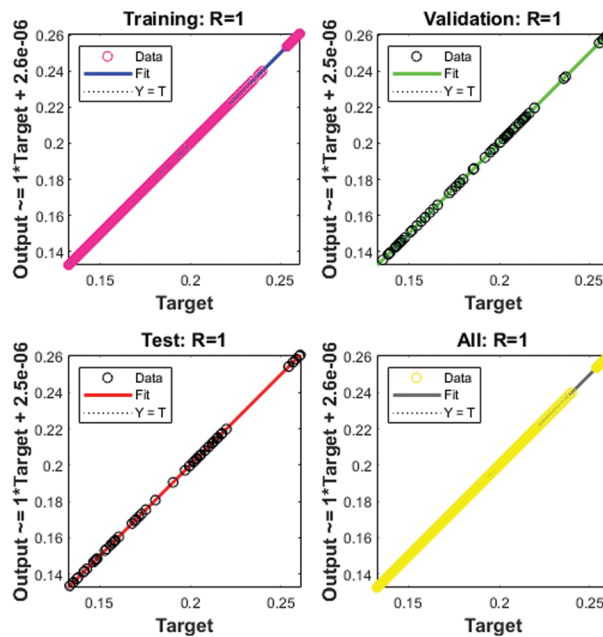


Figure 7: Regression for Case 3

The correlation plots are provided in Figs 5–7, which authenticates the performances of the regression. The correlations based on the determination coefficient, i.e., performances of R^2 found as 1 to solve the SEIR nonlinear system of the Zika virus spreading using the ANNs-SCG. The best plots of the training, testing, and corroboration authenticate the performances of the ANNs-SCG and are found correct for the SEIR nonlinear system of the Zika virus spreading. Table 2 represents the SEIR nonlinear system based on the Zika virus spreading through the MSE convergence of training, iterations, substantiation, testing and complexity measures. The complexity performances of the ANNs-SCG scheme are provided for the training of the systems, i.e., execution cost based on the 1000 iterations and SEIR nonlinear system based on the Zika virus spreading. The complexity is presented in Table 2 based on the ANNs-SCG approach, which takes around 5 ± 2 s in each case of the SEIR nonlinear system.

Table 2: ANNs-SCG procedure for the SEIR nonlinear system based on the Zika virus

Case	MSE			Performance	Gradient	Mu	Iterations	Complexity
	Training	Confirmation	Testing					
1	3×10^{-12}	3×10^{-12}	4×10^{-12}	3.15×10^{-12}	7.8×10^{-8}	1×10^{-13}	23	2
2	5×10^{-11}	7×10^{-11}	2×10^{-11}	5.22×10^{-11}	9.0×10^{-8}	1×10^{-11}	30	2
3	2×10^{-12}	2×10^{-12}	2×10^{-12}	2.44×10^{-12}	6.8×10^{-8}	1×10^{-17}	28	2

The result comparison plots and AE (obtained and reference results) to solve the SEIR nonlinear system based on the Zika virus spreading are illustrated in Figs. 8 and 9. The derived and reference outputs for each class of the SEIR nonlinear system based on the Zika virus spreading are overlapped. The excellence, and perfection of the proposed ANNs-SCG are observed with the overlapping of the results. Fig. 9 authenticates the AE measures for each variation of the SEIR nonlinear system of the Zika virus spreading. The AE results are performed as 10^{-05} to 10^{-07} , 10^{-05} to 10^{-06} and 10^{-04} to 10^{-06}

for the category $S_H(y)$, 10^{-6} to 10^{-8} , 10^{-5} to 10^{-6} and 10^{-6} to 10^{-7} for class $E_H(y)$, 10^{-6} to 10^{-7} , 10^{-5} to 10^{-6} and 10^{-5} to 10^{-7} for class $I_H(y)$, 10^{-7} to 10^{-9} , 10^{-5} to 10^{-7} and 10^{-6} to 10^{-8} for class $R_H(y)$, 10^{-6} to 10^{-9} , 10^{-5} to 10^{-7} and 10^{-6} to 10^{-7} for class $S_V(y)$, 10^{-5} to 10^{-7} , 10^{-4} to 10^{-6} and 10^{-5} to 10^{-6} for class $E_V(y)$ and 10^{-6} to 10^{-7} , 10^{-5} to 10^{-7} and 10^{-7} to 10^{-8} for class $E_H(y)$ of the SEIR nonlinear system. These performances of the SEIR nonlinear system of the Zika virus spreading are performed exactly and accurately.

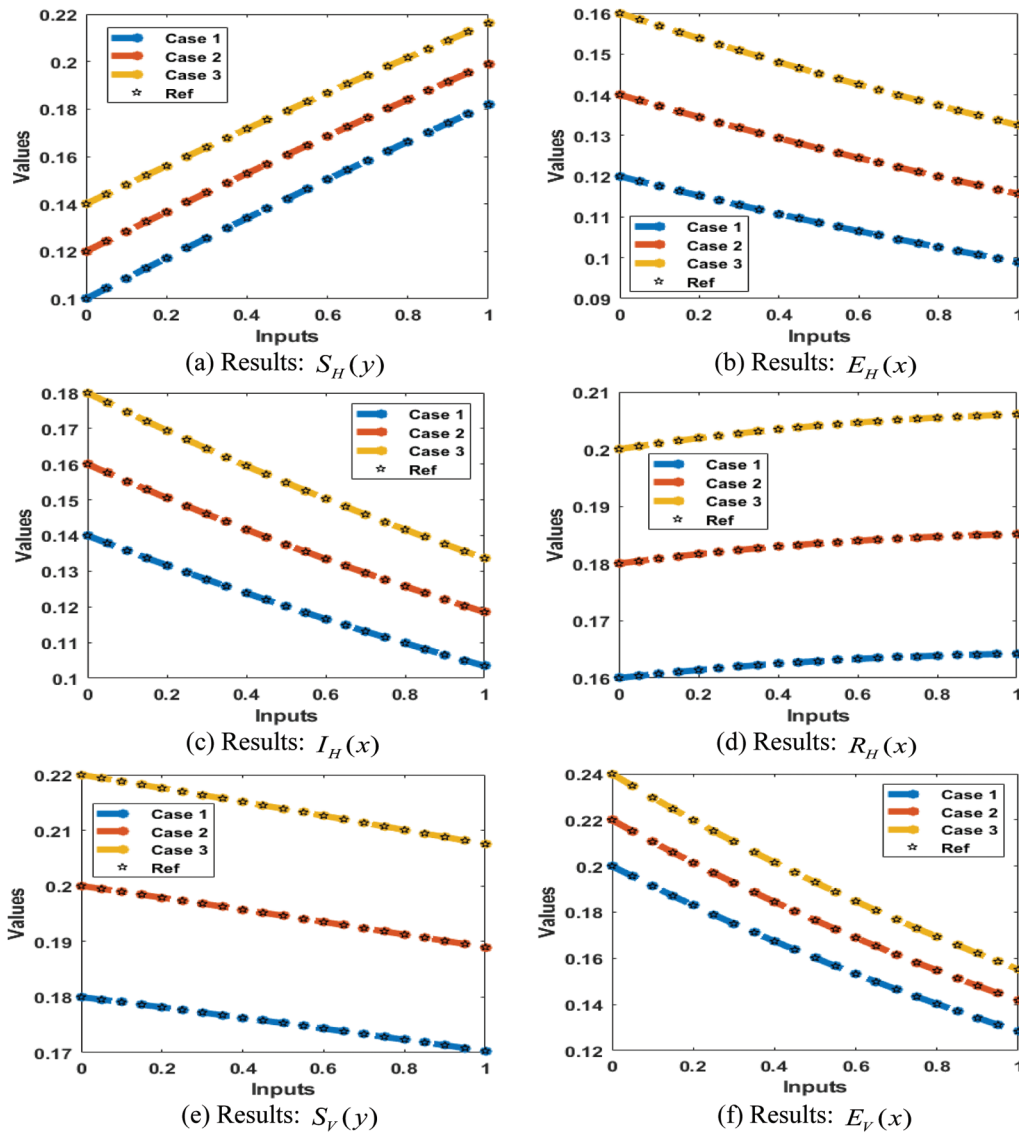
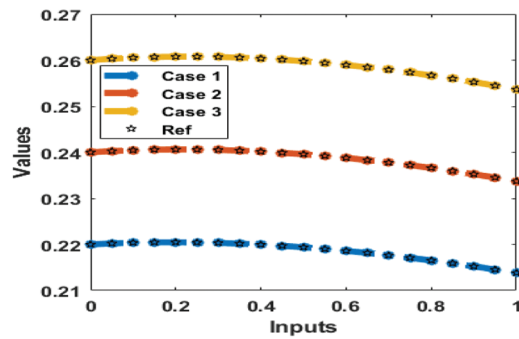


Figure 8: (Continued)



(g) Results: $I_V(x)$

Figure 8: Results for the SEIR nonlinear system based on the Zika virus spreading

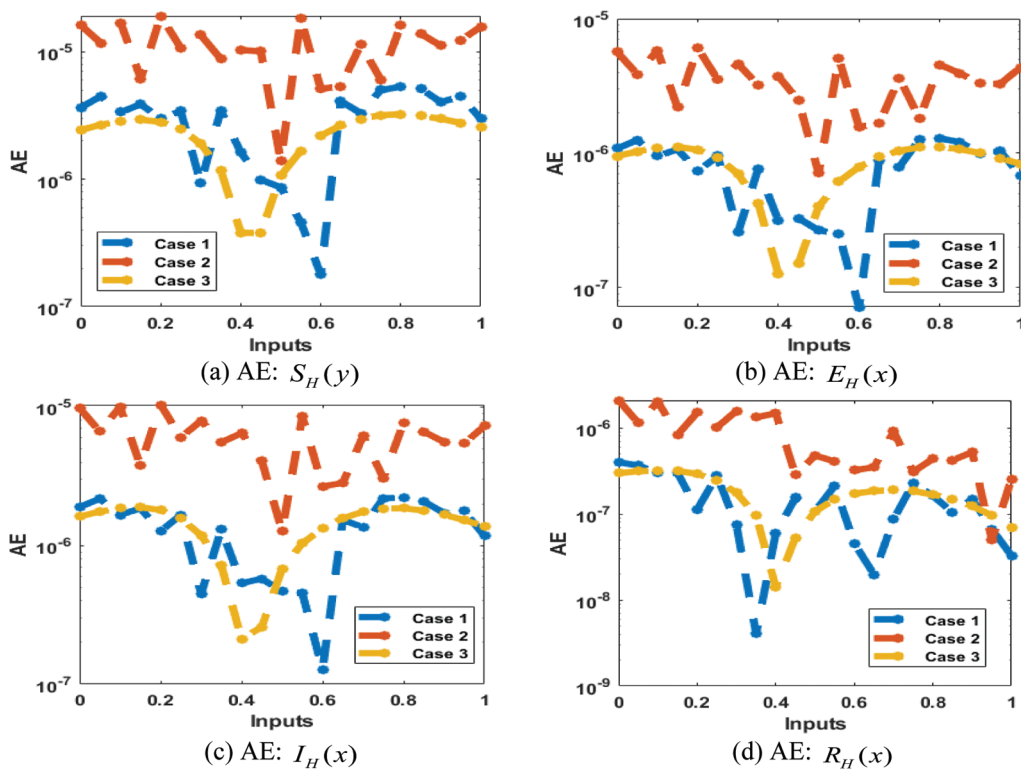


Figure 9: (Continued)

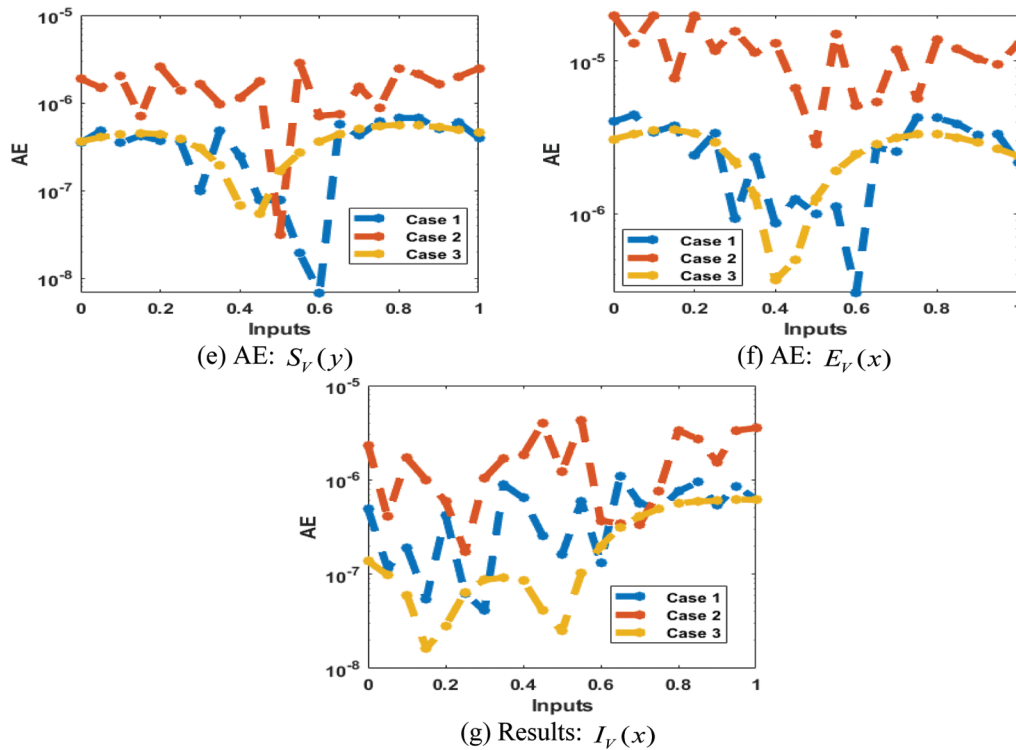


Figure 9: AE for the SEIR nonlinear system based on the Zika virus spreading

5 Conclusion

The purpose of the current work is to present the numerical performances of the SEIR nonlinear system based on the Zika virus spreading by using stochastic procedures. The epidemic form of the SEIR nonlinear system is divided into four dynamics of the patients, susceptible patients $S(y)$, exposed patients hospitalized $E(y)$, infected patients $I(y)$ and recovered patients $R(y)$. The system's computing numerical performances are examined using artificial neural networks along with the scaled conjugate gradient. Few concluding remarks of this study are presented as:

- The numerical presentations based on the SEIR nonlinear system of the Zika virus spreading have been described through the stochastic scheme.
- Three variations of the Zika virus spreading have been described through the stochastic procedure and numerically stimulated using the designed computational approach.
- The exactness of the scheme is verified by using the comparison procedures of the obtained reference solutions.
- The default stoppage limits, step size, and tolerances are applied to label the data, training targets, and inputs, which have been accessed using the standard numerical result performances.
- The AE values of each dynamic of the SEIR nonlinear system of the spreading Zika virus have been performed accurately using the proposed scheme.
- The statics of the dataset has been divided into three parts, 11% for testing, 72% for measures for training and 17% for validation.
- The constancy of the computing scheme has been authenticated through the different statistical performances.

In the future, the suggested schemes can be applied to propose the numerical performances of the computational dynamics based on fluidic systems, computer virus systems, fractional kinds of systems, and biological models [38–47].

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Conflicts of Interest: The authors declare that they have no conflicts of interest to report regarding the present study.

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